



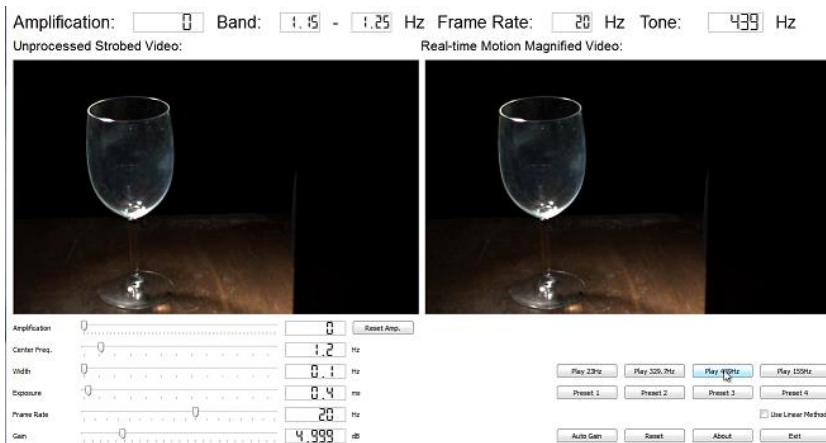
# Video Magnification

**Chao-Tsung Huang**

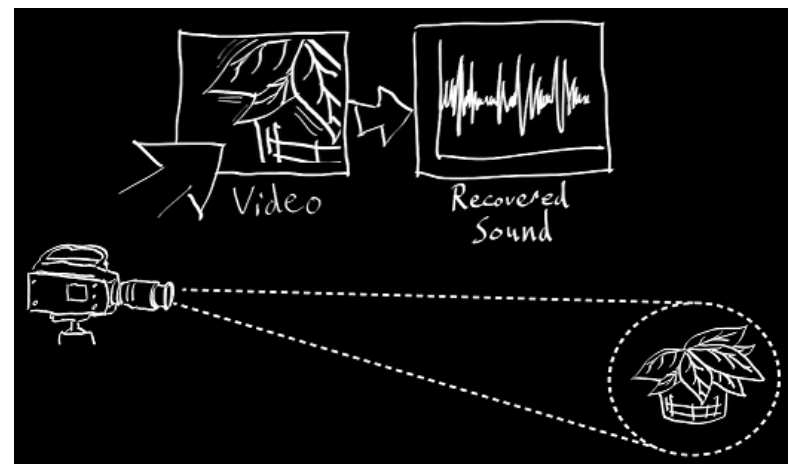
**National Tsing Hua University  
Department of Electrical Engineering**

# Video magnification

- A technique to detect tiny motion and then magnify or manipulate it
- Great resource from MIT (papers and source codes)
  - <http://people.csail.mit.edu/mrub/vidmag/>



Real-time Riesz pyramids  
(CVPR'14 best demo)



Visual microphone



# Outline

- Lagrangian motion magnification (SIGGRAPH'05)
- Linear Eulerian video magnification (SIGGRAPH'12)
- Phase-based video magnification (SIGGRAPH'13)

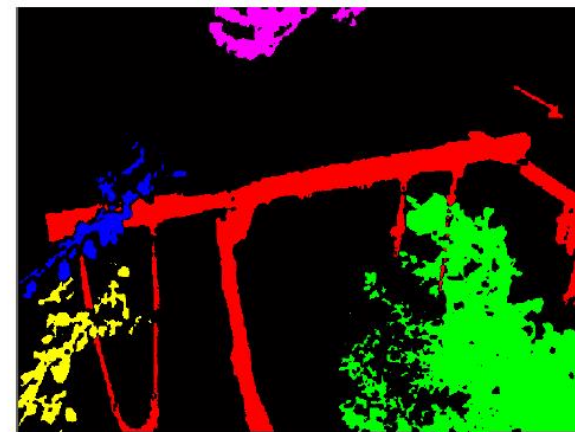
# Lagrangian motion magnification



(a) Registered input frame



(b) Clustered trajectories of tracked features



(c) Layers of related motion and appearance



(d) Motion magnified, showing holes



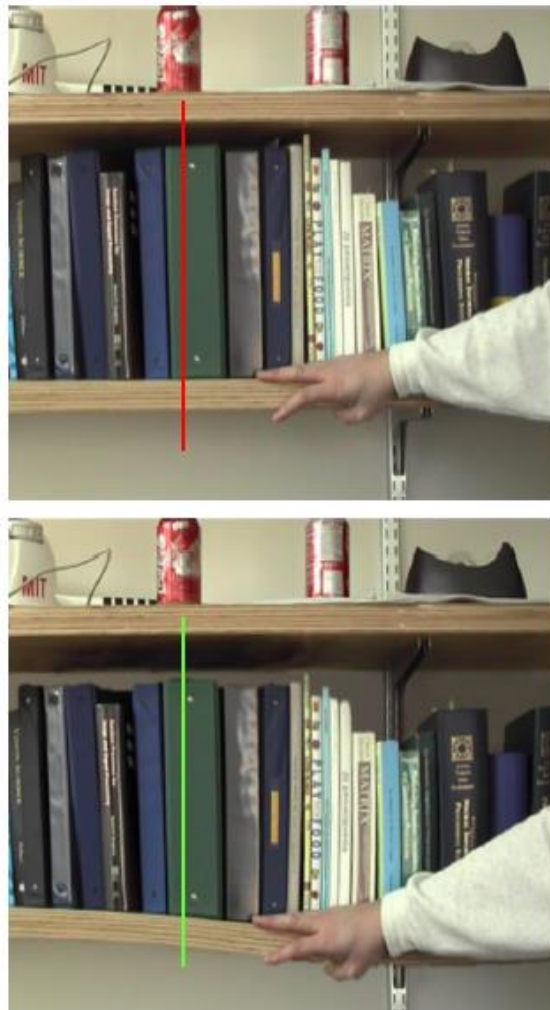
(e) After texture in-painting to fill holes



(f) After user's modifications to segmentation map in (c)

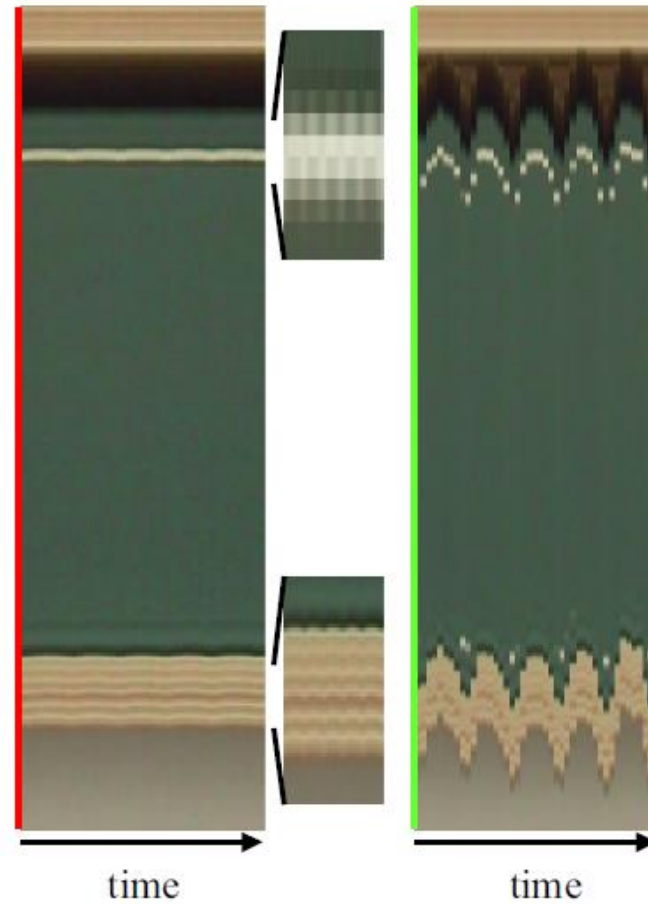
Ref: C. Liu, et. al., "Motion magnification," SIGGRAPH, 2005.

# Result

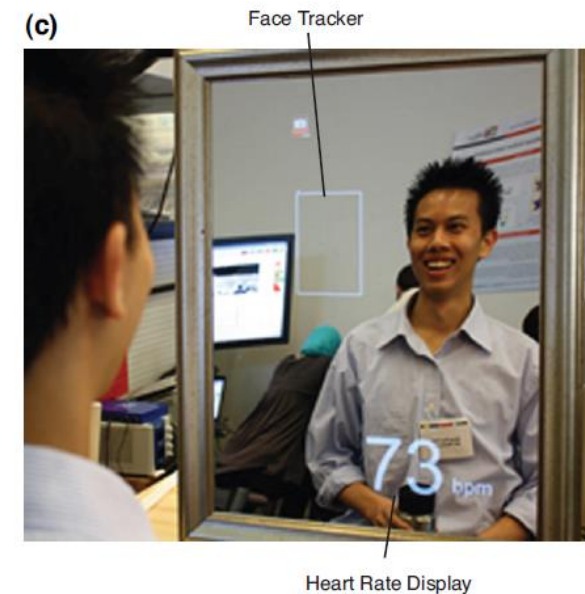
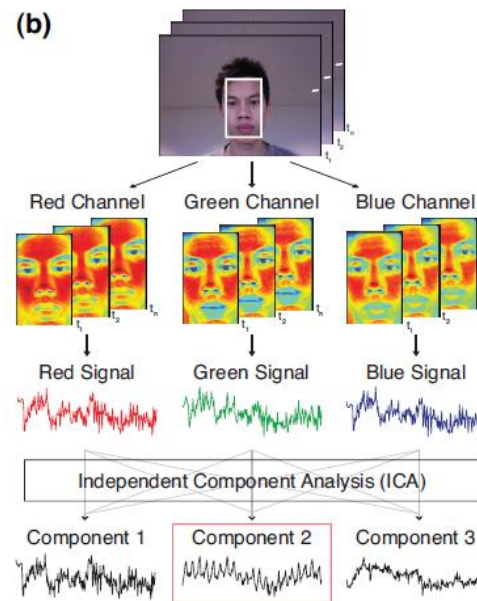
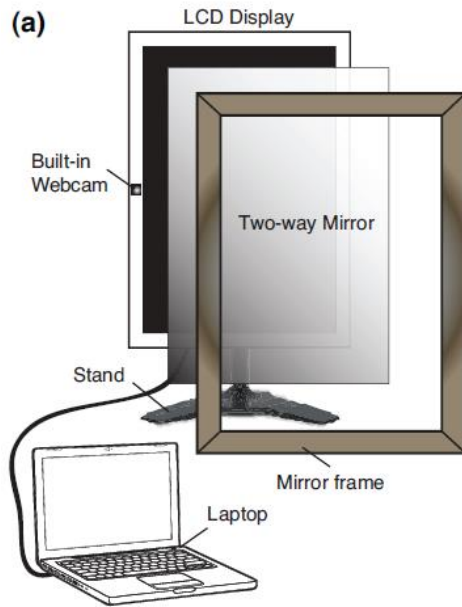


Original

Magnified



# Medical mirror (distraction)



Detect heart rate by analyzing vein color variation



# Outline

- Lagrangian motion magnification (SIGGRAPH'05)
- **Linear Eulerian video magnification** (SIGGRAPH'12)
- Phase-based video magnification (SIGGRAPH'13)

# Eulerian video magnification

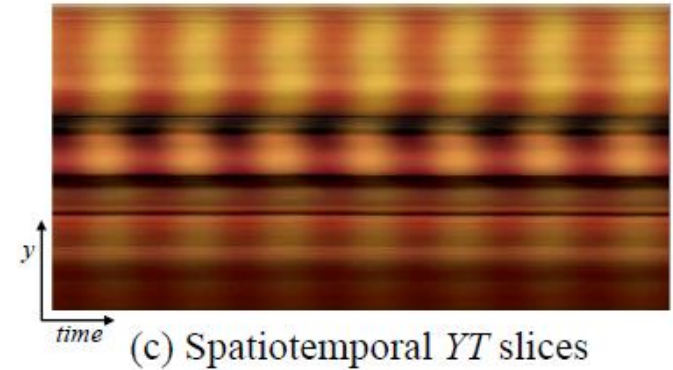
Magnify subtle color/motion changes in video



(a) Input



(b) Magnified



(c) Spatiotemporal  $YT$  slices

Ref: H.-Y. Wu, et. al., "Eulerian video magnification for revealing subtle changes in the world," SIGGRAPH, 2012.





# Eulerian motion magnification

- First-order Taylor series expansion as optical flow analysis

$$I(x, t) = f(x + \delta(t)) \text{ and } I(x, 0) = f(x)$$



First-order  
expansion

$$I(x, t) \approx f(x) + \delta(t) \frac{\partial f(x)}{\partial x}$$



Temporal filtering  
(only keep the  
interesting  $\delta(t)$ )

$$B(x, t) = \delta(t) \frac{\partial f(x)}{\partial x}$$

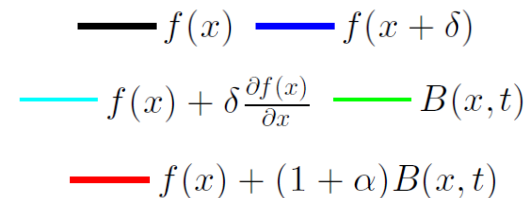
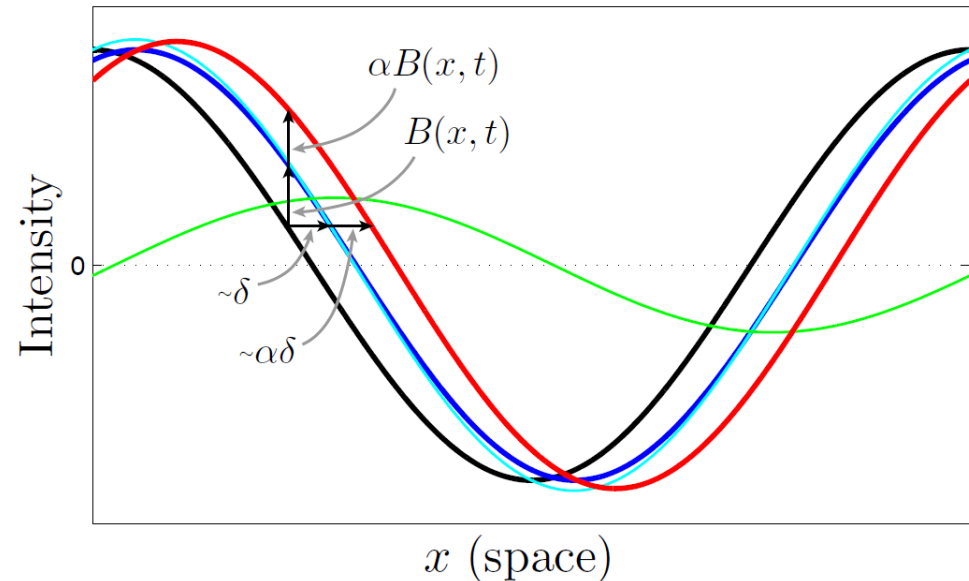


Magnification

$$\tilde{I}(x, t) = I(x, t) + \alpha B(x, t)$$

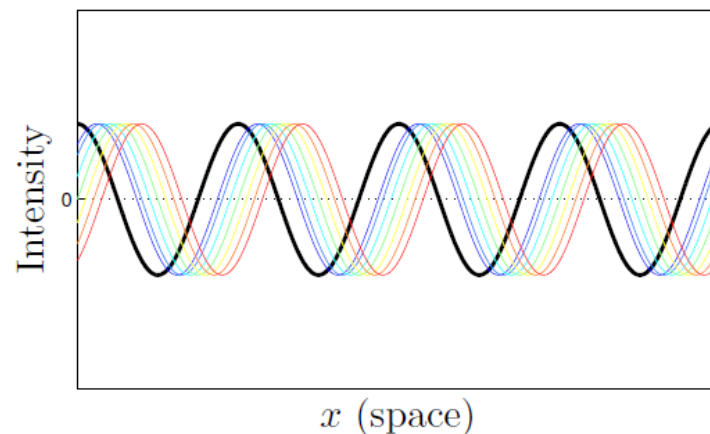
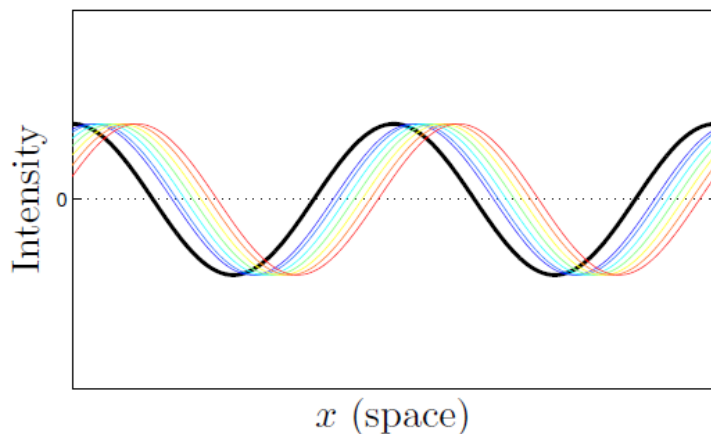
$$\tilde{I}(x, t) \approx f(x) + (1 + \alpha)\delta(t) \frac{\partial f(x)}{\partial x}$$

$$\tilde{I}(x, t) \approx f(x + (1 + \alpha)\delta(t))$$



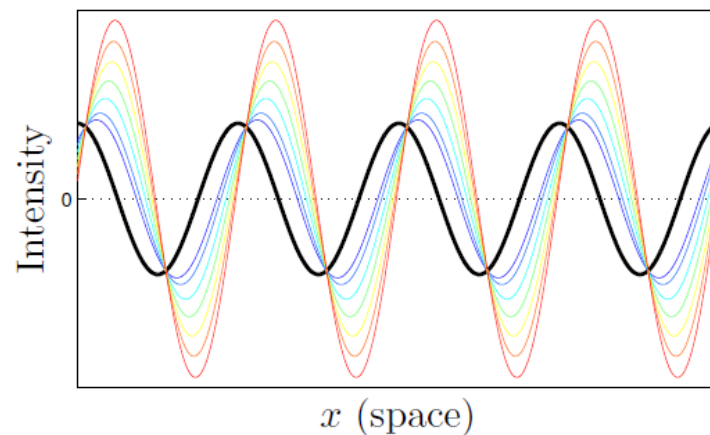
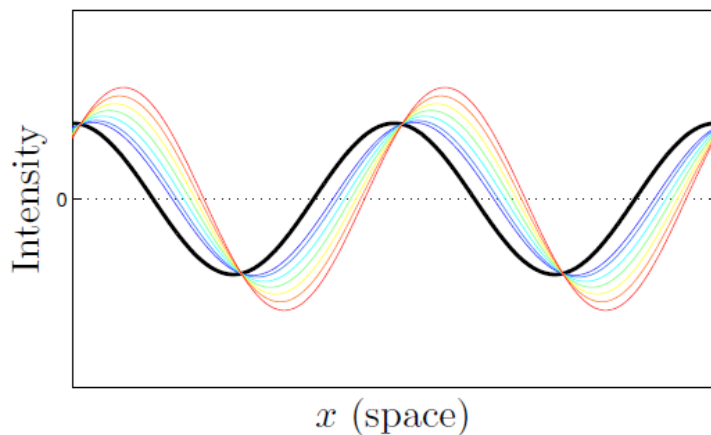
# Motion magnification bound

$$(1 + \alpha)\delta(t) < \frac{\lambda}{8}$$



(a) True motion amplification:  $\hat{I}(x, t) = f(x + (1 + \alpha)\delta(t))$ .

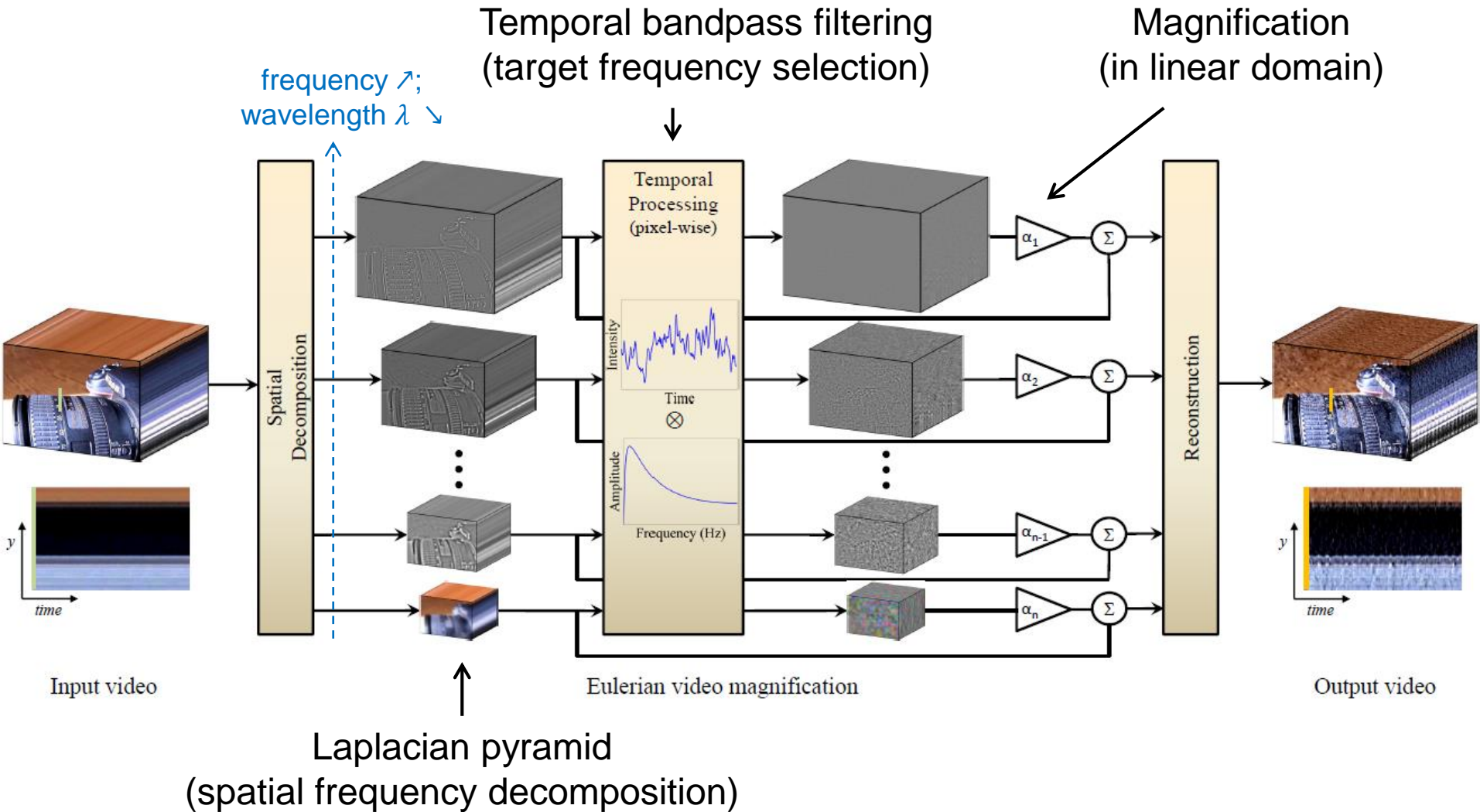
—  $\alpha = 0.2$  —  $\alpha = 0.5$  —  $\alpha = 1.0$  —  $\alpha = 1.5$  —  $\alpha = 2.0$  —  $\alpha = 2.5$  —  $\alpha = 3.0$



(b) Motion amplification via temporal filtering:

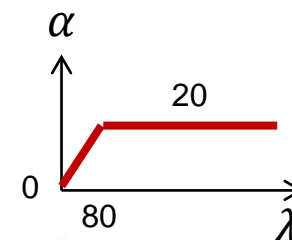
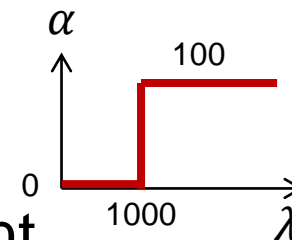
$$\tilde{I}(x, t) = I(x, t) + \alpha B(x, t).$$

# Spatio-temporal filtering framework

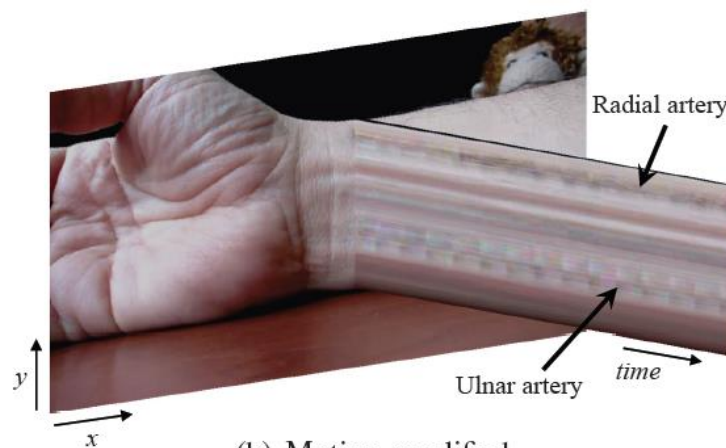


# Magnification setting

- Color magnification
  - Large  $\alpha$ , on low spatial-frequency component
  - Should register video to avoid motion magnification
- Motion magnification
  - Smaller  $\alpha$ , wavelength-bound



(a) Input (*wrist*)



(b) Motion-amplified

# Result

Revealing Invisible Changes In The World



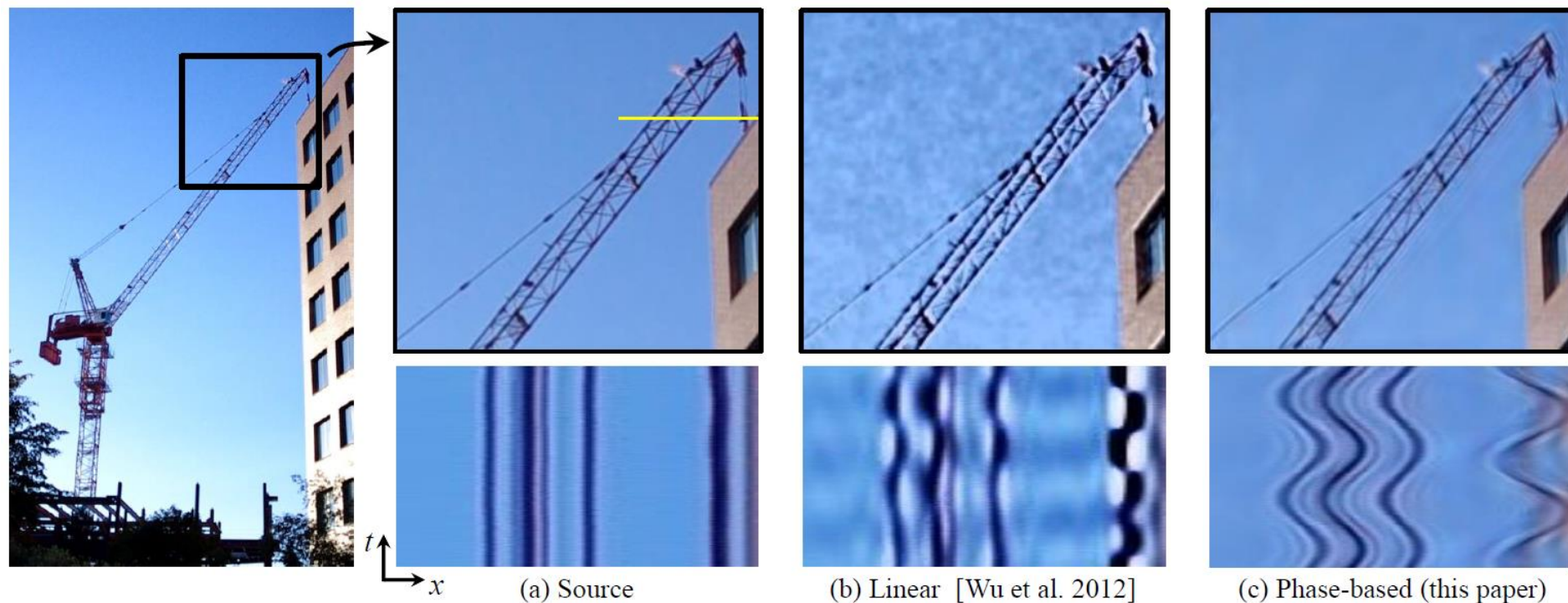


# Outline

- Lagrangian motion magnification (SIGGRAPH'05)
- Linear Eulerian video magnification (SIGGRAPH'12)
- **Phase-based video magnification (SIGGRAPH'13)**

# Phase-based video magnification

- Amplify “phase shift”, instead of amplitude (linear, Eulerian)
  - Support larger motion; less noise sensitive



Ref: N. Wadhwa, et. al., “Phase-based video motion processing,” SIGGRAPH, 2013.



# Phase magnification

for a single-frequency component

$$S_\omega(x, t) = A_\omega e^{i\omega(x+\delta(t))}$$

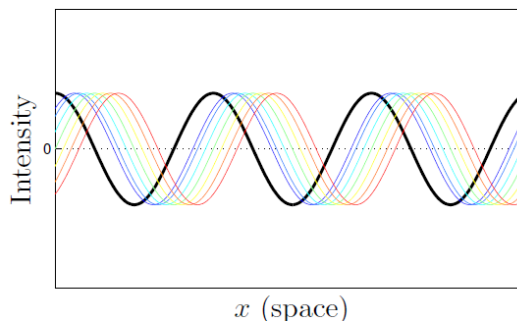


Temporal filtering  
to keep interesting  
phase shift

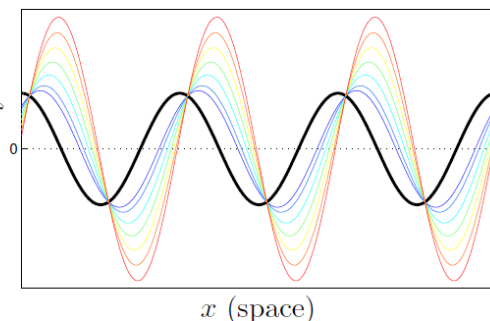
$$B_\omega(x, t) = \omega\delta(t)$$



Amplify the phase shift

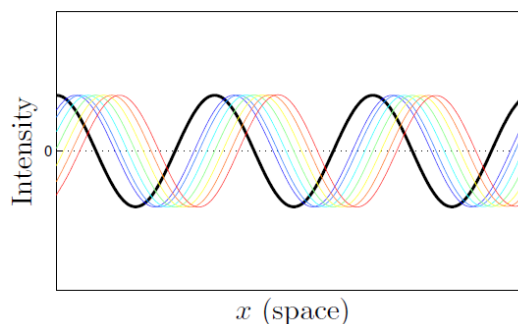


(a) True amplification

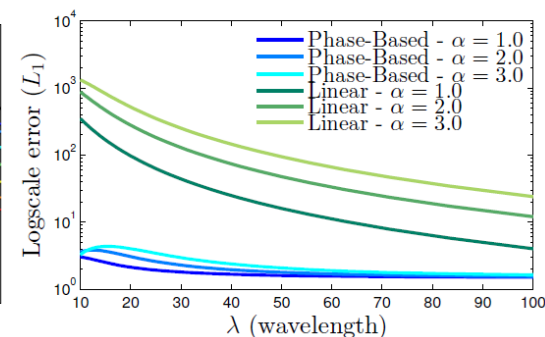


(b) [Wu et al. 2012]

—  $\alpha = 0.2$  —  $\alpha = 0.5$  —  $\alpha = 1.0$  —  $\alpha = 1.5$  —  $\alpha = 2.0$  —  $\alpha = 2.5$  —  $\alpha = 3.0$



(c) Phase-based



(d) Error as function of wavelength

$$\hat{S}_\omega(x, t) := S_\omega(x, t) e^{i\alpha B_\omega} = A_\omega e^{i\omega(x+(1+\alpha)\delta(t))}$$



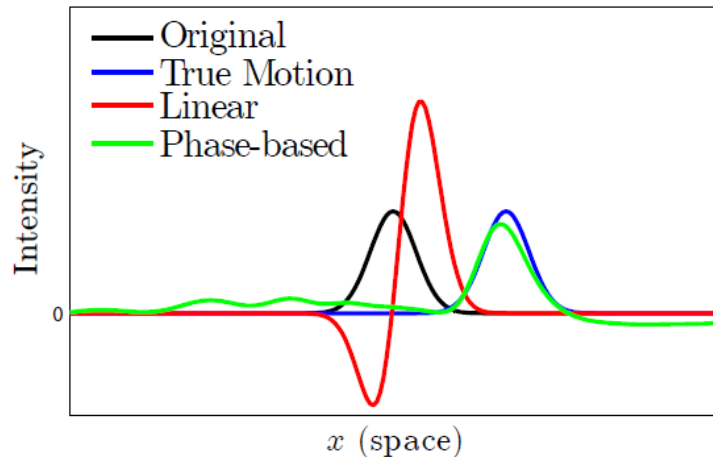


# Limitations on spatial frequency

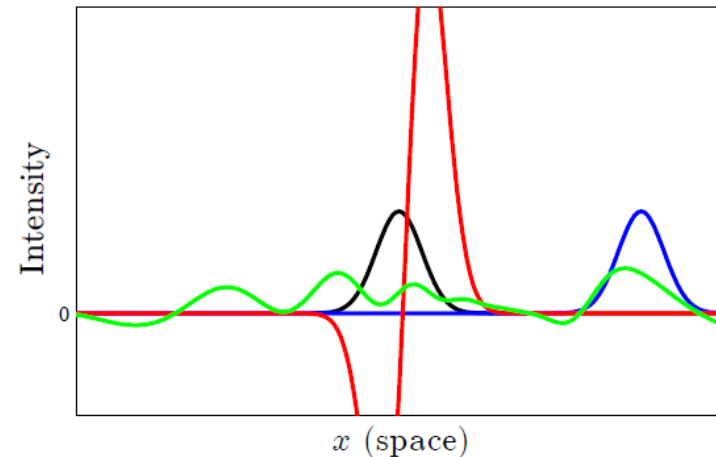
- Magnification bound

$$\alpha \delta(t) < \frac{\lambda}{4}$$

- At least two times better than linear magnification



(a)  $\alpha = 6$

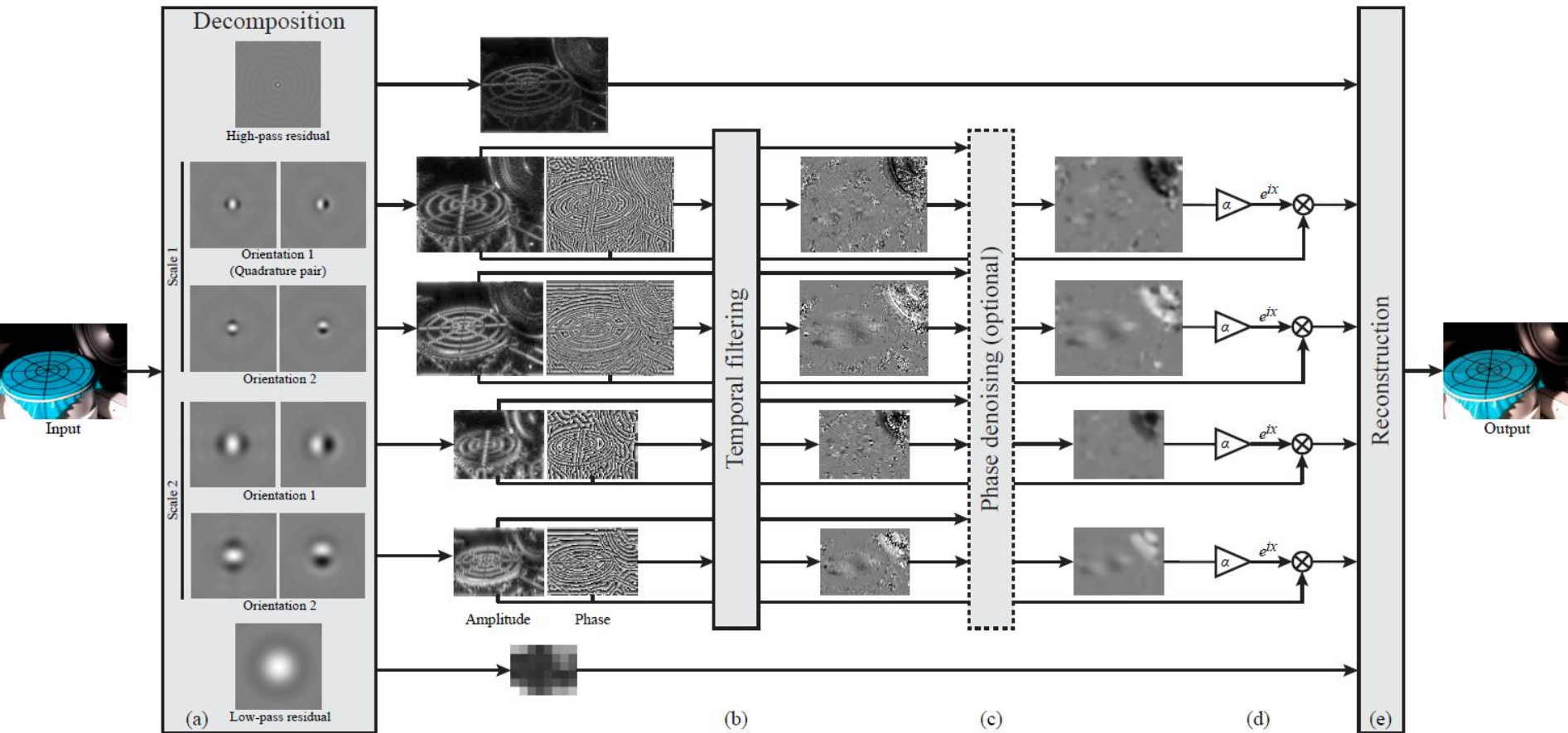


(b)  $\alpha = 14$

- Mind the single-frequency assumption

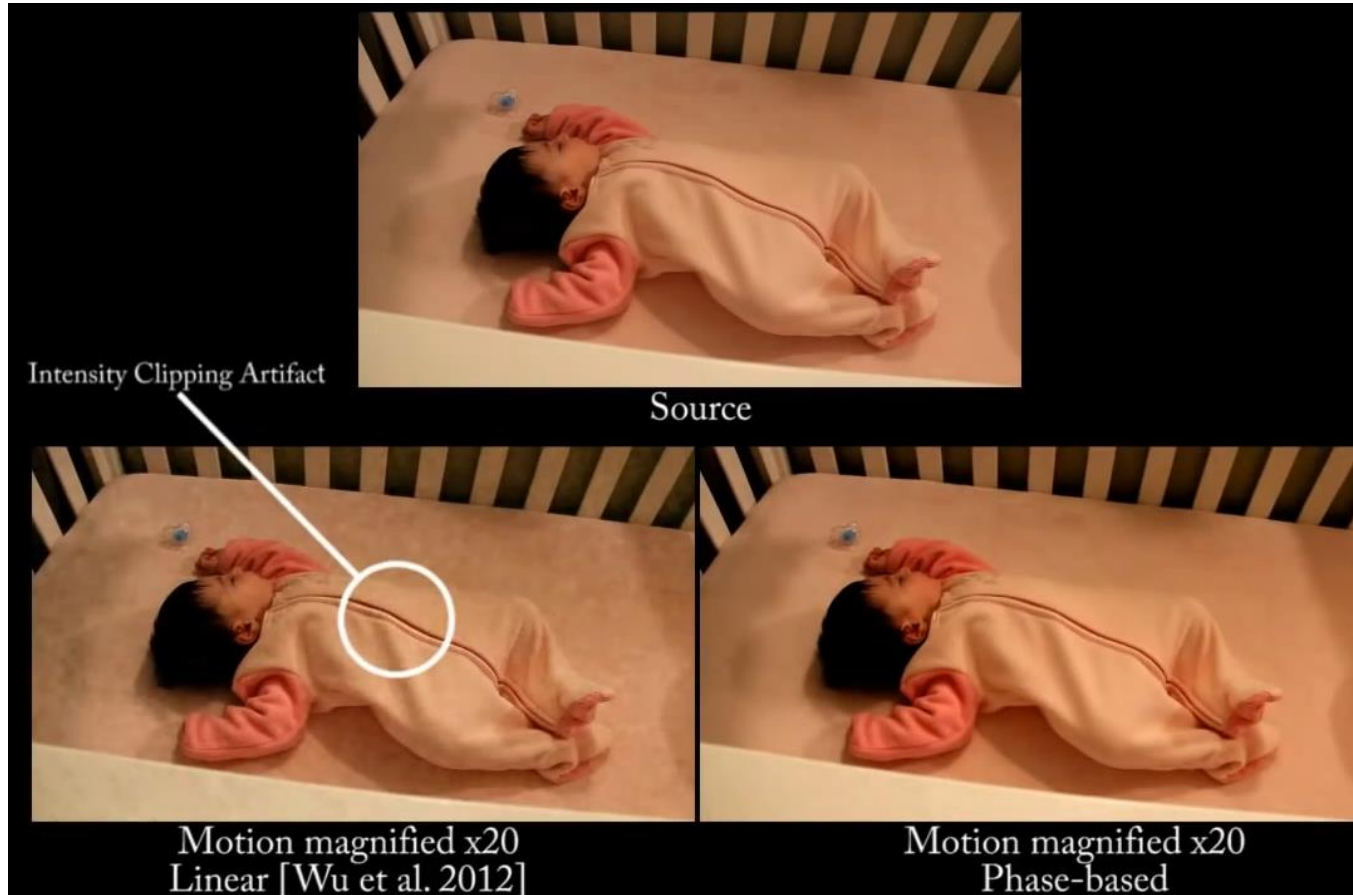
- Phase shift = motion \* spatial frequency

# Phase-based framework



Complex steerable pyramid  
(decompose localized phase/amplitude in different directions and spatial frequencies)

# Result





# Appendix

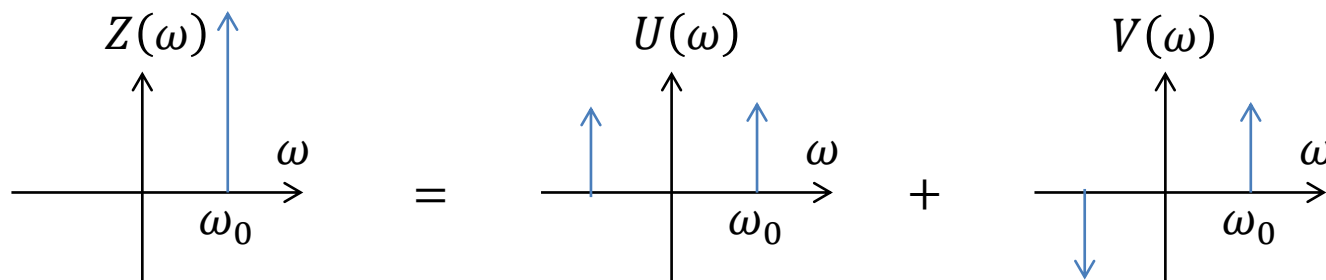


# Fourier analysis

- Simple example (note the single-frequency assumption)

$$u(t) = \cos \omega_0 t \Rightarrow \text{quadrature pair (90}^\circ \text{ shift): } v(t) = \sin \omega_0 t$$

Consider a **complex** signal  $z(t) = u(t) + i v(t)$



$$Z(\omega) = 2U(\omega)\mathbf{1}_{\{\omega \geq 0\}}$$



# Hilbert transform

$$\mathcal{H}(u)(t) = v(t) = \frac{1}{\pi t} * u(t) \Rightarrow V(\omega) = -i \operatorname{sgn} \omega \cdot U(\omega)$$

$$\therefore \text{for } z(t) = u(t) + iv(t) \Rightarrow Z(\omega) = 2U(\omega)\mathbf{1}_{\{\omega \geq 0\}}$$

Hilbert transform is to find the quadrature pair

Here we only need this simpler derivation

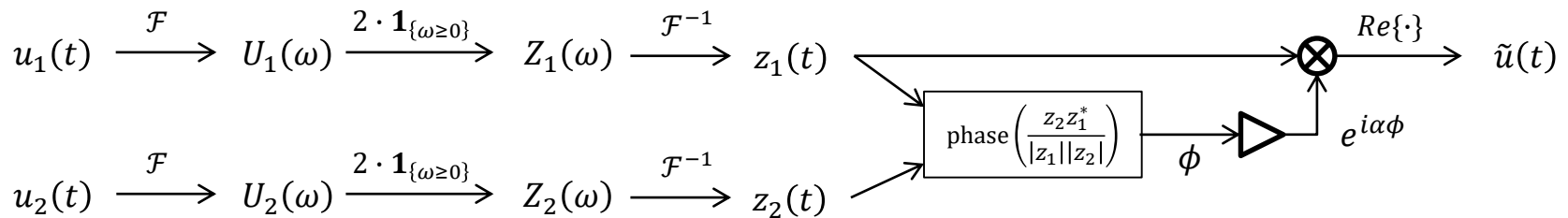
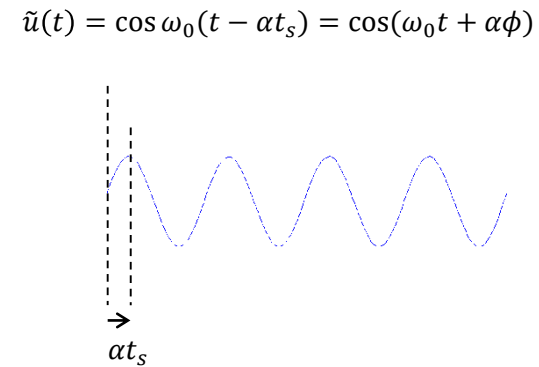
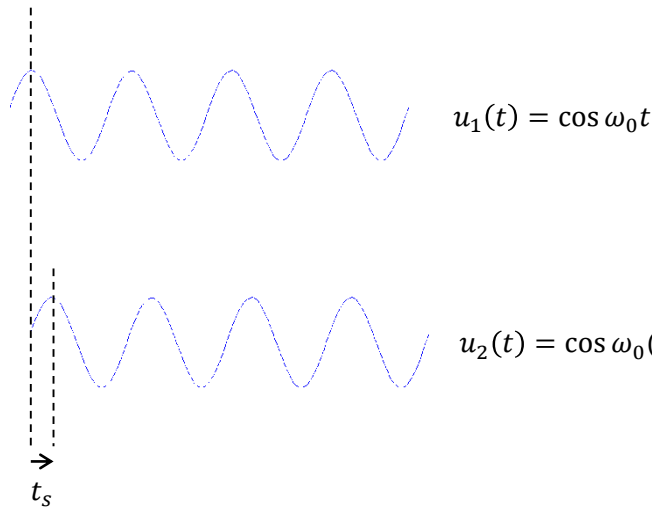
$$\text{Let } Z(\omega) = 2U(\omega)\mathbf{1}_{\{\omega \geq 0\}} \Rightarrow z(t) = u(t) + iv(t)$$

where  $u(t) = \operatorname{Re}\{z(t)\}$  and  $v(t) = \mathcal{H}(u)(t) = \operatorname{Im}\{z(t)\}$

**Q:** How to derive complex  $z(t)$  for real  $u(t)$ ? **A:**  $\mathcal{F}^{-1}\{2U(\omega)\mathbf{1}_{\{\omega \geq 0\}}\}$ .



# Toy example for phase-based signal interpolation



**Q:** How about multi-frequency signals? **A:** Filter bank decomposition.