
EE4280 Lecture 3: Oscillator

Ping-Hsuan Hsieh (謝秉璇)

♣ Delta Building R908

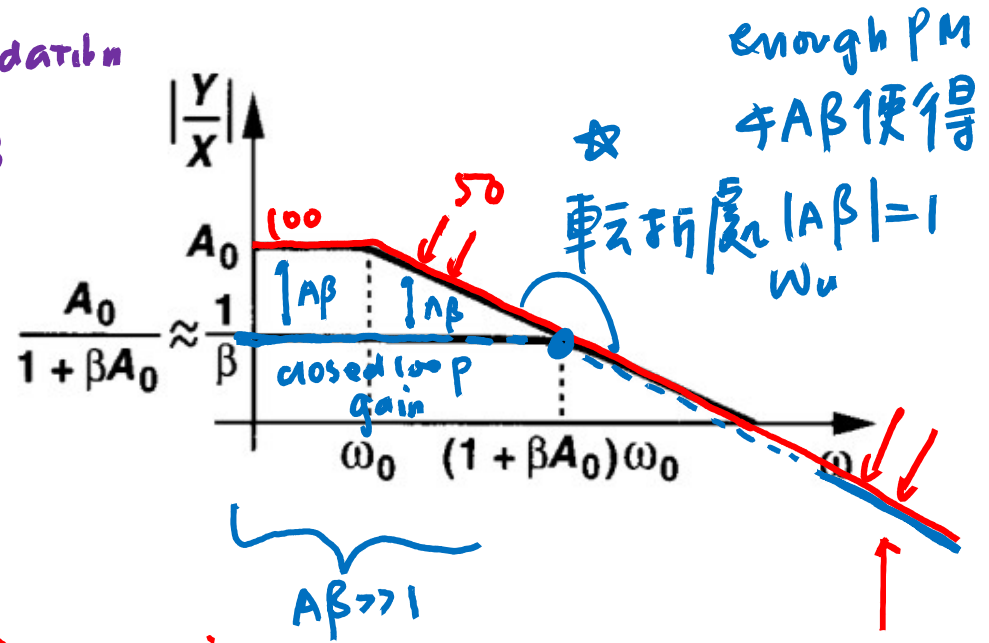
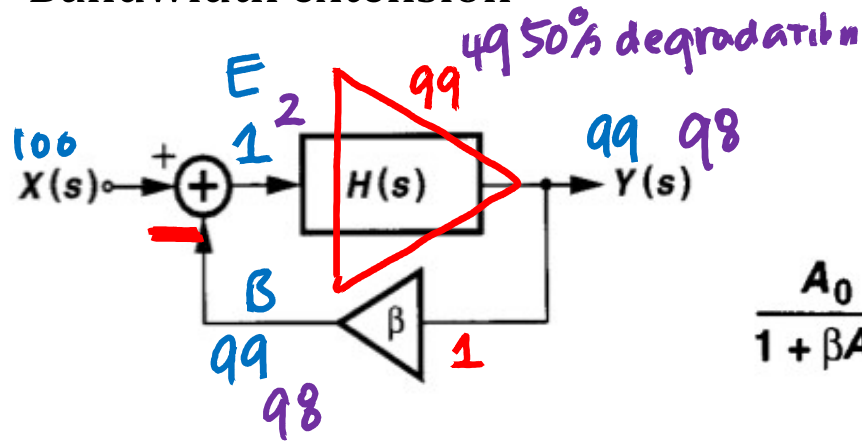
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phsieh@ee.nthu.edu.tw

Negative Feedback

Closed-loop transfer function vs. open-loop transfer function

- Gain desensitization
- Bandwidth extension



$$\frac{Y}{X}(s) = \frac{H(s)}{1 + \beta H(s)} \approx \frac{1}{\beta}$$

positive gain with subtraction
 = $\frac{\text{open-loop gain}}{1 - \text{loop gain}}$

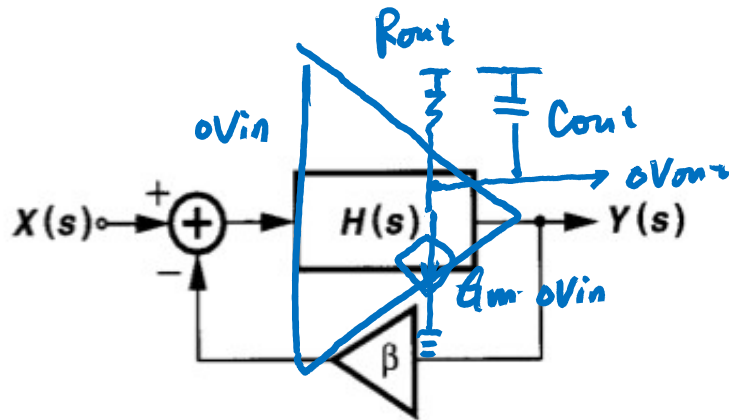
$$\frac{Y}{X} = \frac{A\beta}{1 + A\beta} \approx 1$$

$A\beta \ll 1$
 loop broken
 $\frac{Y}{X} \approx H(s)$

Stability in Negative Feedback

As the operating frequency increases

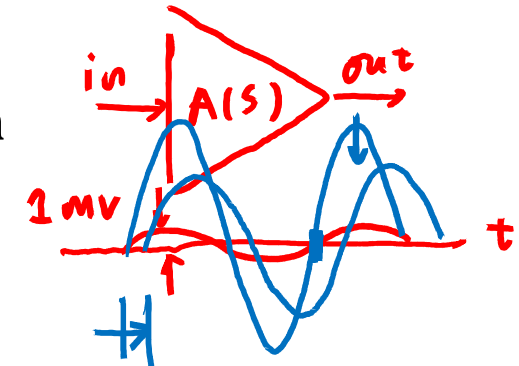
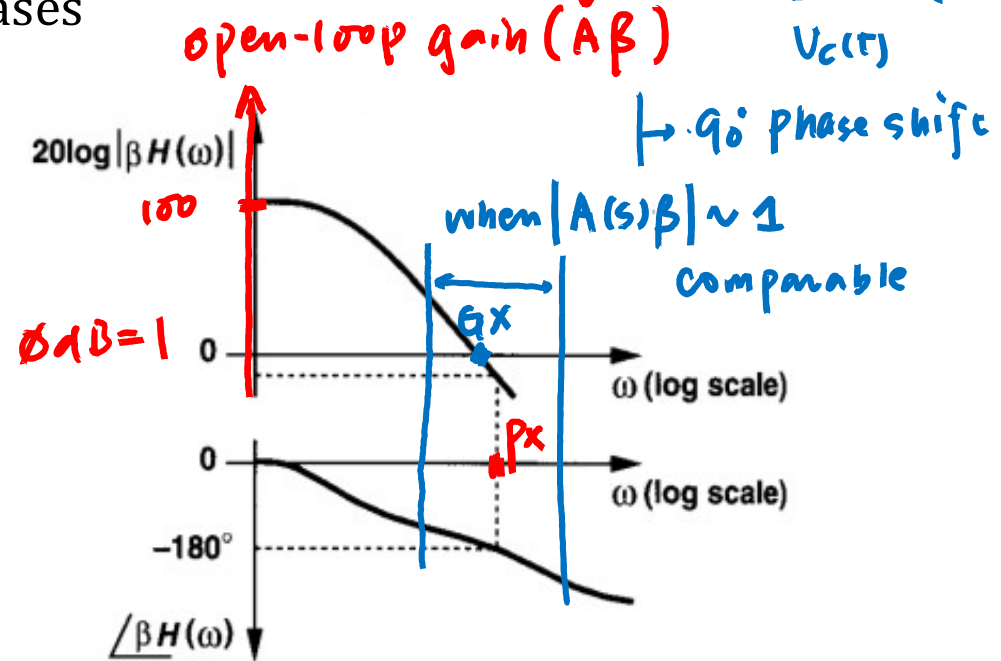
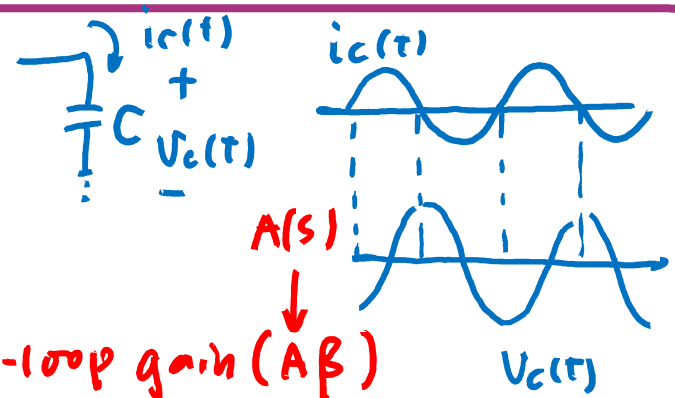
- The open-loop gain decreases
- The open-loop phase shift increases



$$\frac{Y}{X}(s) = \frac{H(s)}{1 + \beta H(s)}$$

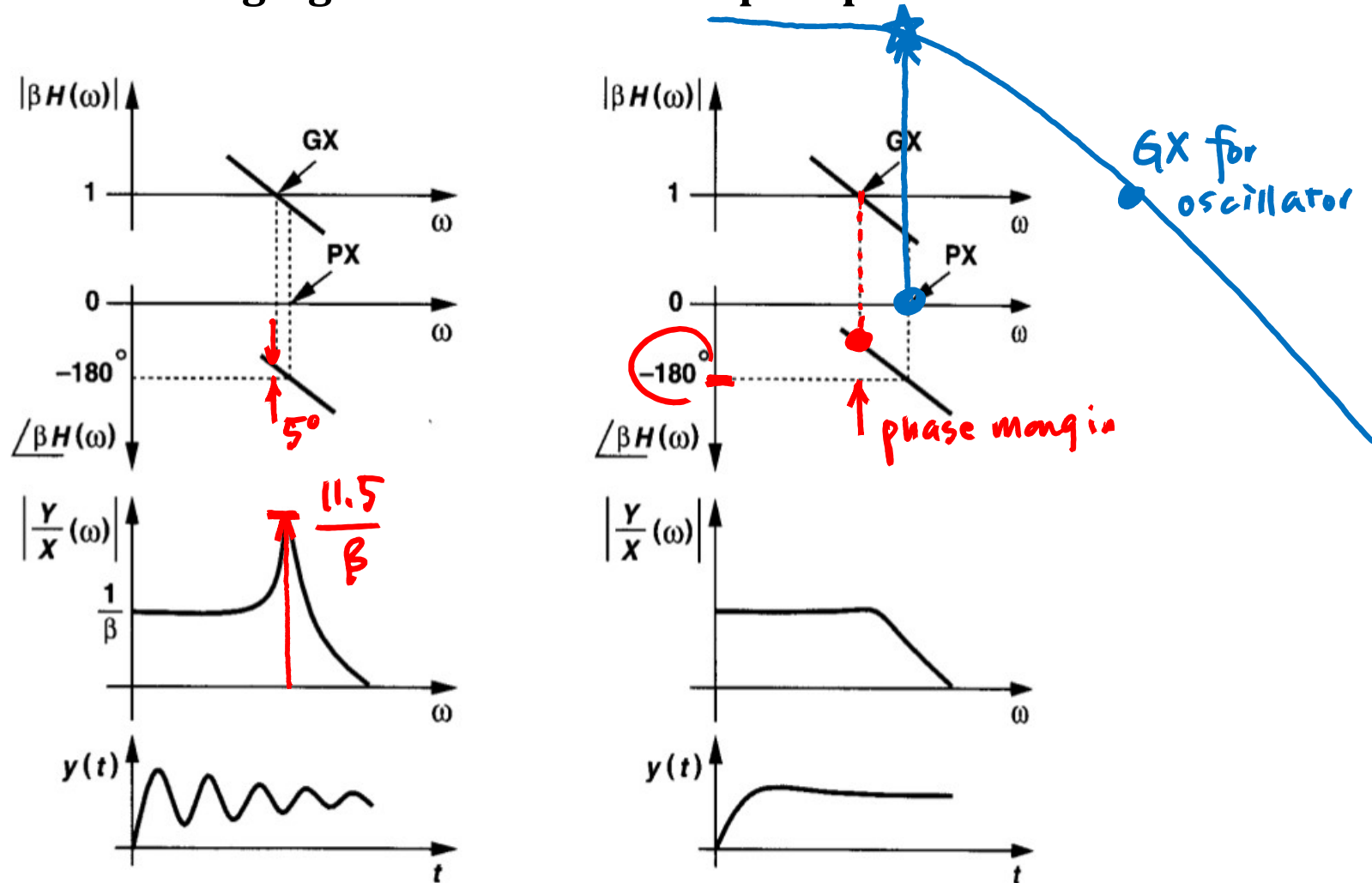
In fact, we care about the frequencies at which

- The open-loop gain drops to 0 dB
- The open-loop phase delay is 180°



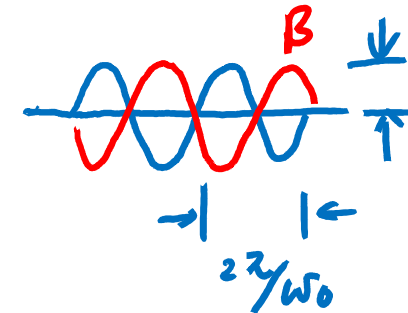
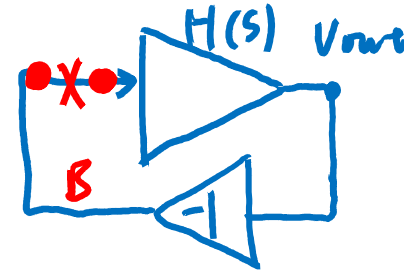
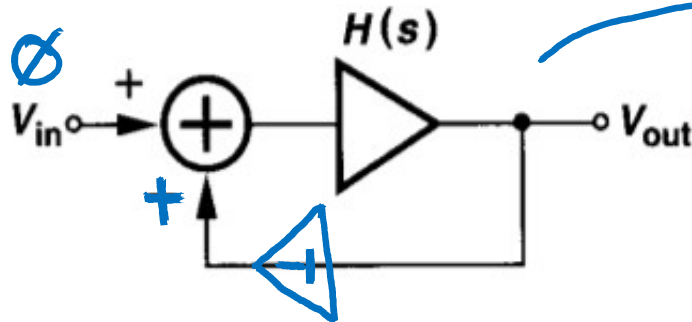
Gain Margin and Phase Margin

- ◆ Insufficient phase margin results in peaking in closed-loop transfer function and ringing in time-domain step response

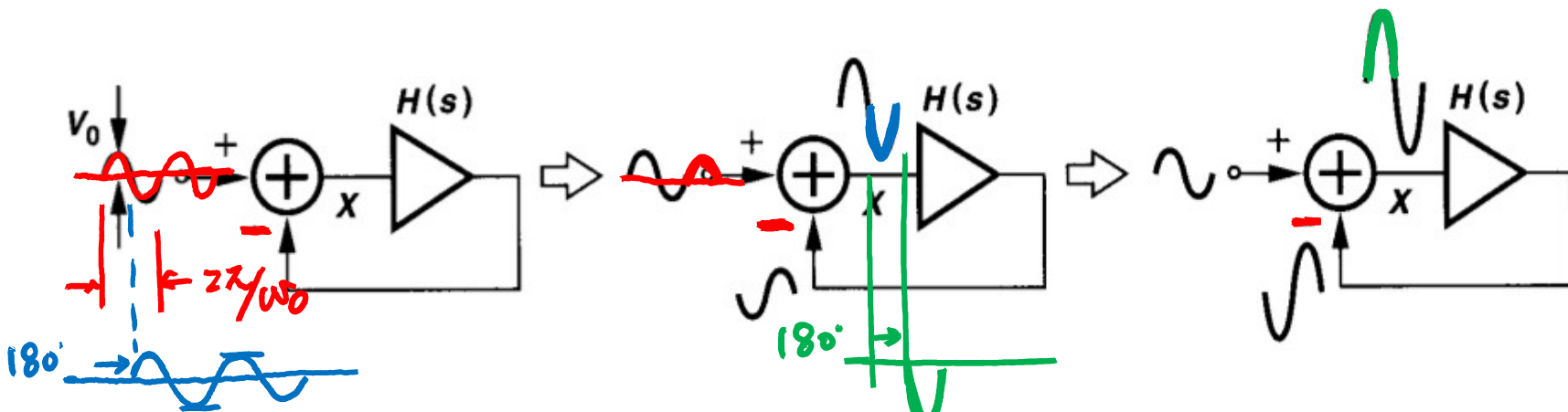


What happens with zero phase margin?

with zero input & ∞ gain @ ω_0



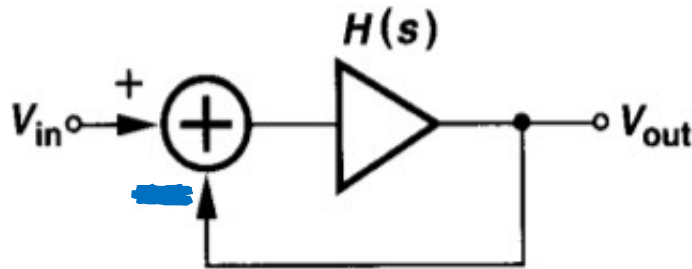
- ◆ In other words, if when $s = j\omega_0$ $H(j\omega_0) = -1$ $\frac{Y}{X}(\omega) \rightarrow \infty @ \omega_0$



- The closed-loop gain approaches infinity at ω_0
- The circuit generates an output signal without input – autonomous

Oscillator - Barkhausen Criteria

- ◆ For an open-loop transfer function that satisfies two conditions:



3, 4, 10
↑

$|H(j\omega_0)| \geq 1$ gain requirement

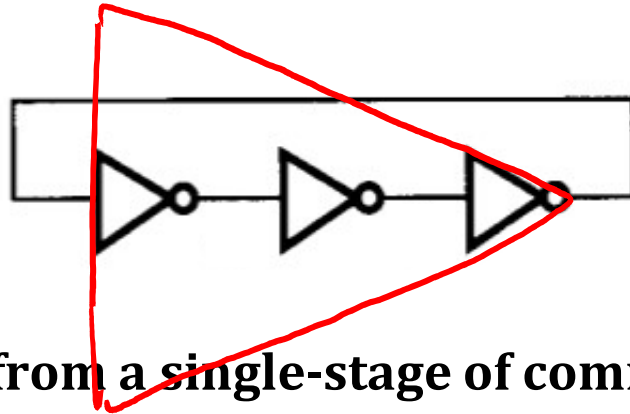
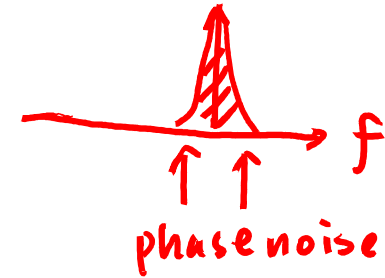
$\angle H(j\omega_0) = 180^\circ$ phase requirement

→ loop becomes positive feedback

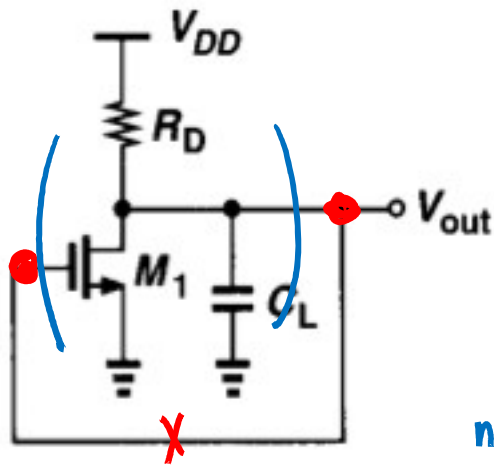
- ◆ The circuit may oscillate at ω_0
 - These conditions are necessary but not sufficient
 - In order to ensure oscillation in the presence of PVT variations, we typically choose the loop gain to be at least twice or three times the required value
- Negative feedback at low frequency to build "stable" DC bias point
- Total phase shift of 360° at $\omega_0 \rightarrow$ positive feedback at ω_0
 → additional frequency-dependent phase delay that is 180° at ω_0

Ring Oscillator (I)

- ◆ A number of gain stages in a loop – a ring



- ◆ Starting from a single-stage of common-source amplifier



Open-loop transfer function

