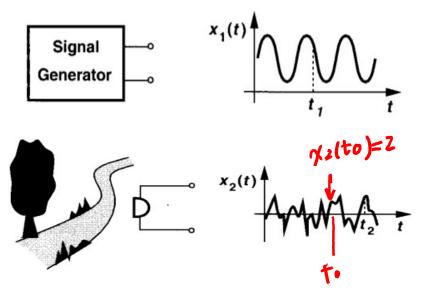
EE4280 Lecture 9: Noise

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What is Noise?

Noise is a random process. We consider a phenomenon random because we do not know everything about it, or simply because we do not <u>need</u> to know everything about it.



Since the instantaneous noise amplitude is not known, we resort to <u>'statistical'</u> models, i.e., some properties that can be predicted.

1. Mean and Average Power

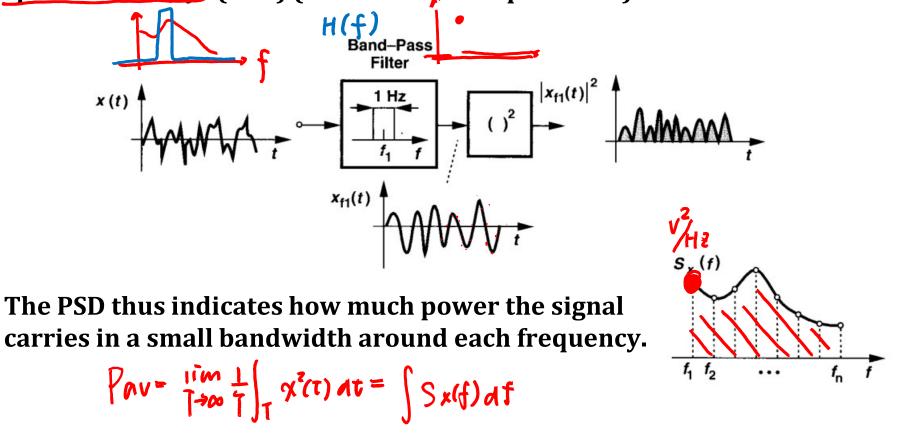
$$\sum_{n=1}^{\infty} \sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{i=1}^{n} \sum$$

Larger fluctuations mean that the noise is 'stronger'

$$M_{i}^{2} = 1$$

2. Frequency Domain

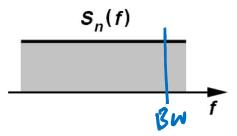
For random signals, the concept of Fourier transform cannot be directly applied. But we still know that men carry less high-frequency components in their voice than women do. We define the "power spectral density" (PSD) (also called the "spectrum") as:



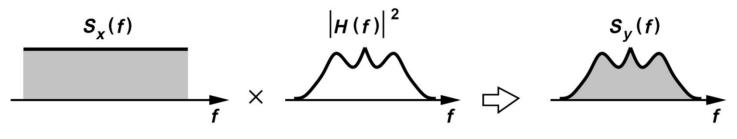
- What is the unit of S_n(f)?
- What is the total noise power?

A flat spectrum is called 'white'

• Is the total noise power infinite?



Important Theorem



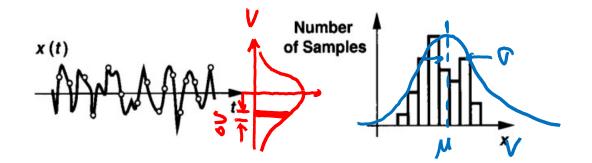
If a signal with spectrum $S_X(f)$ is applied to a linear time-invariant system with transfer function H(s), the output spectrum is given by

 $S_Y(f) = S_X(f)|H(f)|^2$

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3. Amplitude Distribution

By sampling the time-domain waveform for a long time, we can construct a "probability density function" (PDF). The PDF in essence indicates "how often" the amplitude is between certain limits.



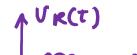
For example, a Gaussian distribution is defined by a mean and a standard deviation. We say the noise amplitude rarely exceeds 4σ .

<u>Note:</u> Generally PDF and PSD bear no relationship. Thermal Noise: Gaussian, white Flicker Noise: Gaussian, not white

Correlated and Uncorrelated Sources

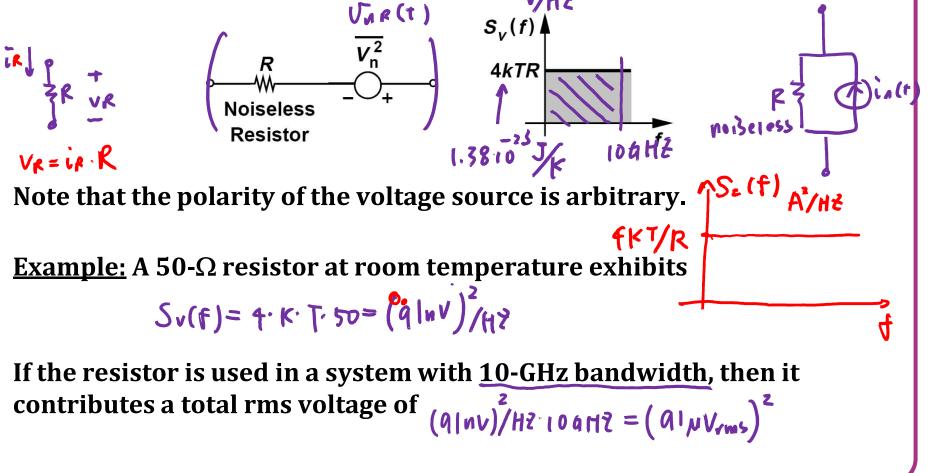
Can we use superposition for average noise power from a few noise omponents? $\begin{array}{ll}
P_{av} &= \lim_{T \to \infty} \frac{1}{T} \int_{-T/2}^{+T/2} [x_1(t) + x_2(t)]^2 dt \\
&= \lim_{T \to \infty} \frac{1}{T} \int_{-T/2}^{+T/2} [x_1(t) + x_2(t)]^2 dt \\
&= \lim_{T \to \infty} \frac{1}{T} \int_{-T/2}^{T} \left(\chi_1^{-1}(t) + Z\chi_1(T)\chi_2(t) + \chi_2^{-1}(t) \right) dt
\end{array}$ components? $\lim_{T \to \infty} \frac{1}{T} \Big|_{T} \chi(t) dt = \lim_{T \to \infty} \frac{1}{T} \int_{T} (\chi_1(t) + \chi_2(t)) dt = \operatorname{Pav}_{T \to \infty} + \operatorname{Pav}_{T}$ $\chi(t) = \chi_1(t) + \chi_2(t) = \emptyset \quad \chi_1^2(t) = (3m \, \text{vrms})^2 + 2\chi_1(t) \times 2(t)$ $\overline{\chi_{2H}^{2}} = (4mV_{MMS})^{2} \quad if \chi_{1LT} and \chi_{2(T)}$ are independent to E.O We occasionally encounter correlated sources: $x_{\rm tot}(t)$ $x_3(t)$

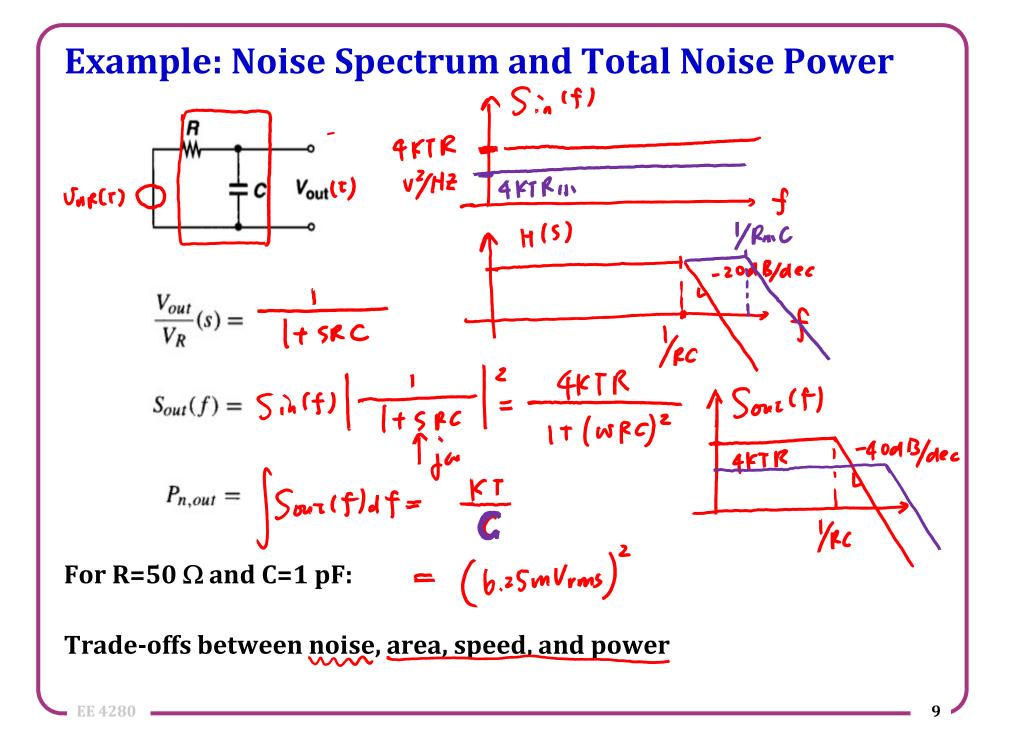
Types of Noise

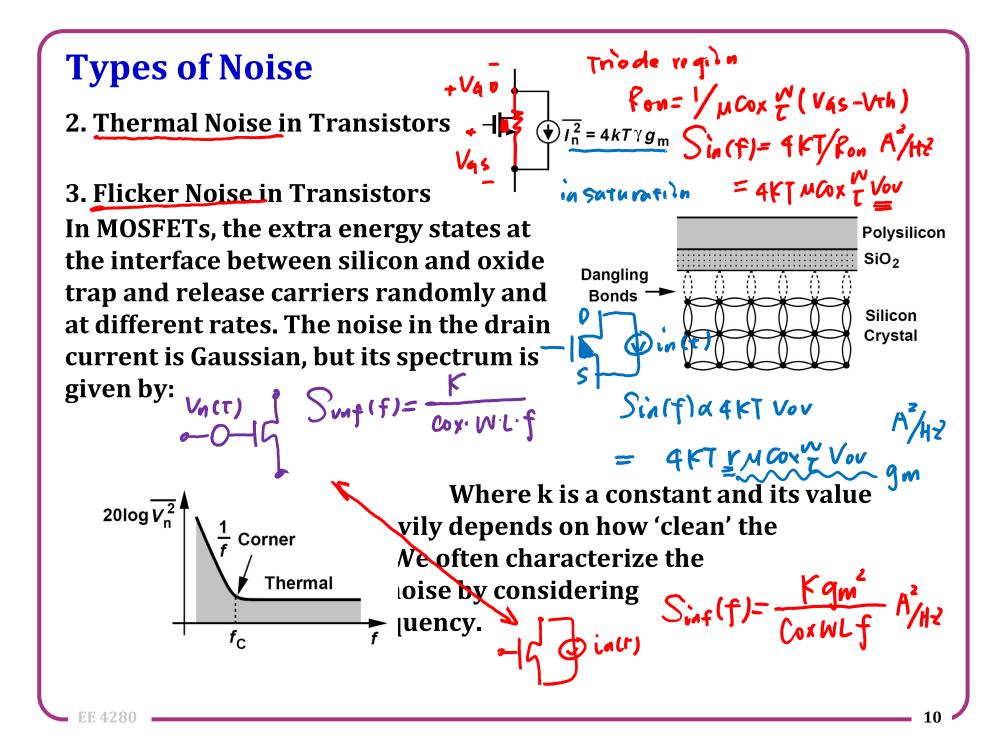


1. Thermal Noise in Resistors

Random movement of charge carriers in a resistor causes fluctuations in the current. The PDF is Gaussian because there are so many carriers. The PSD is given by: $\sqrt{2}/4$

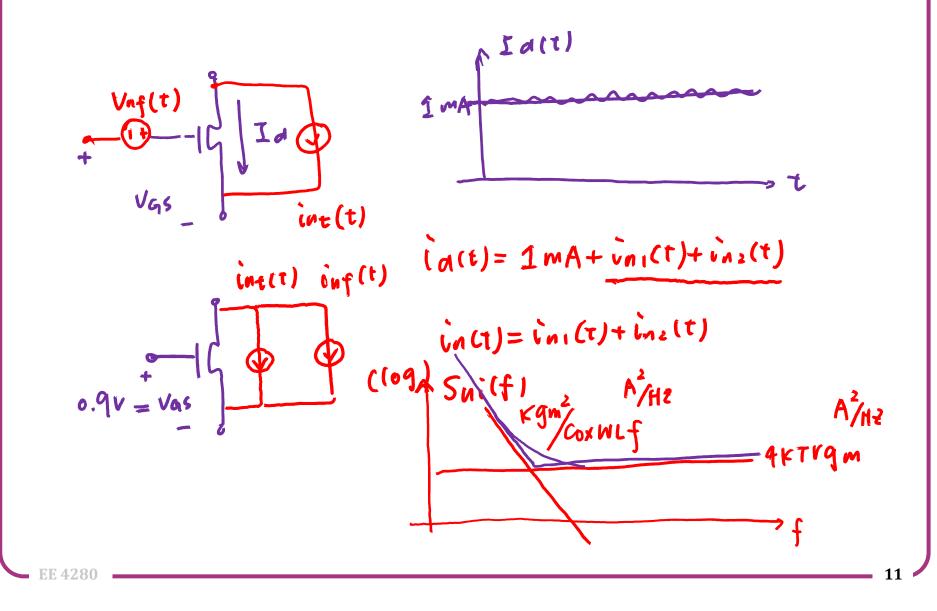






Example: A Current Source

Total noise in the drain current for a band from 1 kHz to 1 MHz



$$\int \frac{S_{in}(f)}{fr} \frac{\int \sqrt{6m^{2}/c_{kr}} dkTrgm}{fr} \frac{4kTrgm}{\sqrt{4k2}} \frac{4kTrgm}{fr} \frac{\sqrt{6}}{fr}$$

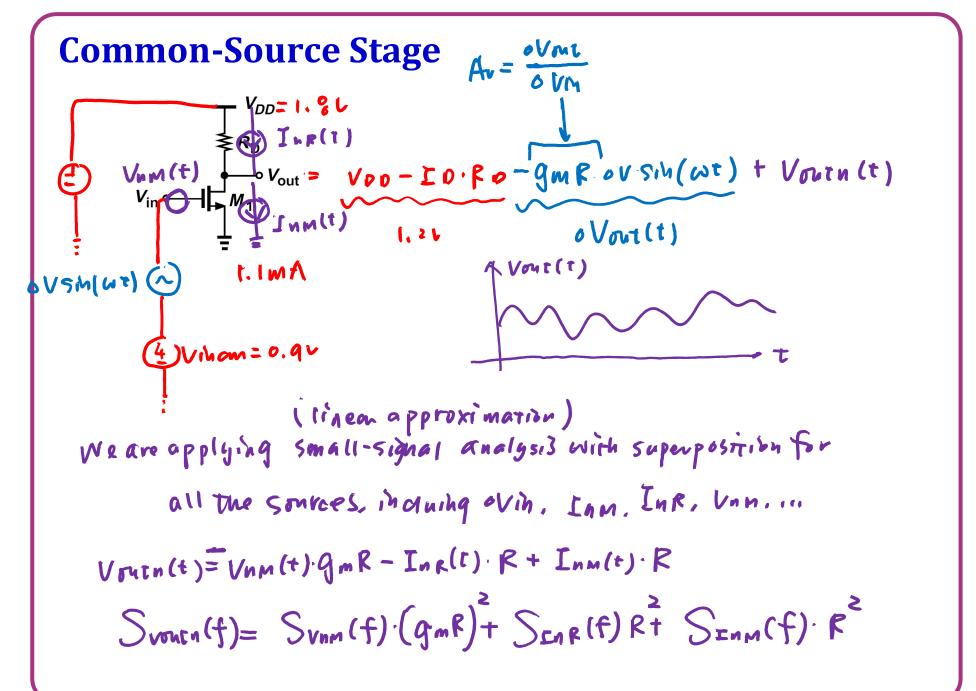
$$\int \frac{f_{ihd} one fr such that $rgm^{2}_{Cox} WL fr}{fr} = 4kTrgm$

$$\int \frac{fr}{c_{0x}WL} gm \frac{1}{4kTr}$$

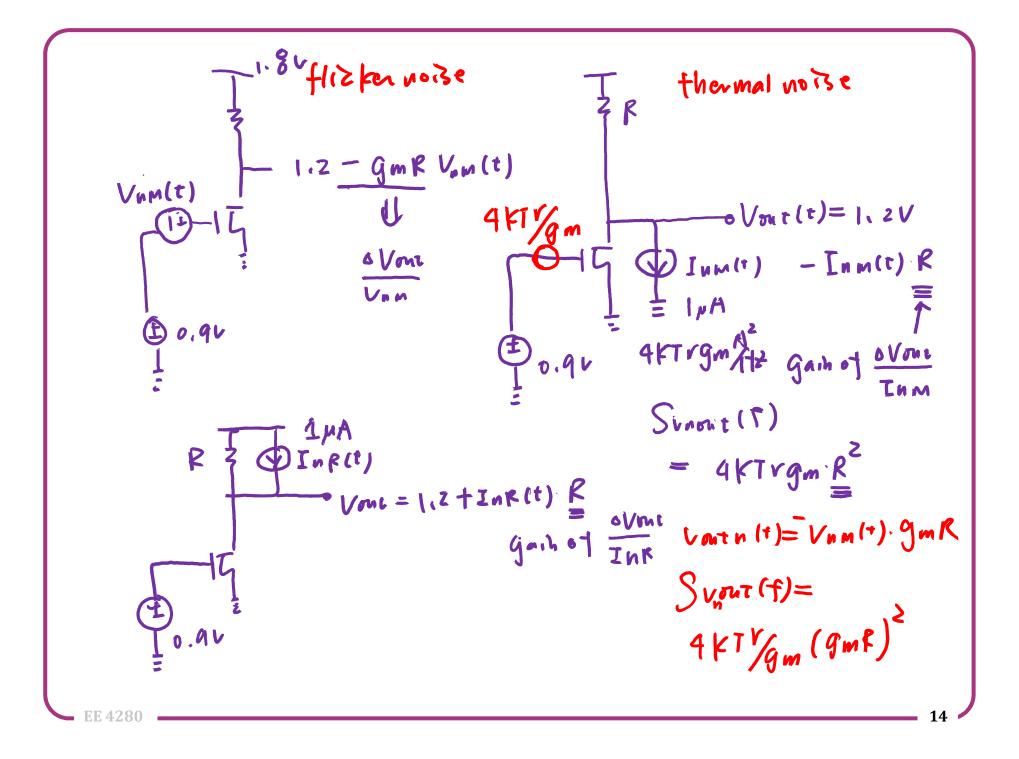
$$\int \frac{fr}{c_{0x}WL} \frac{gm}{fr} \frac{1}{4kTr}$$

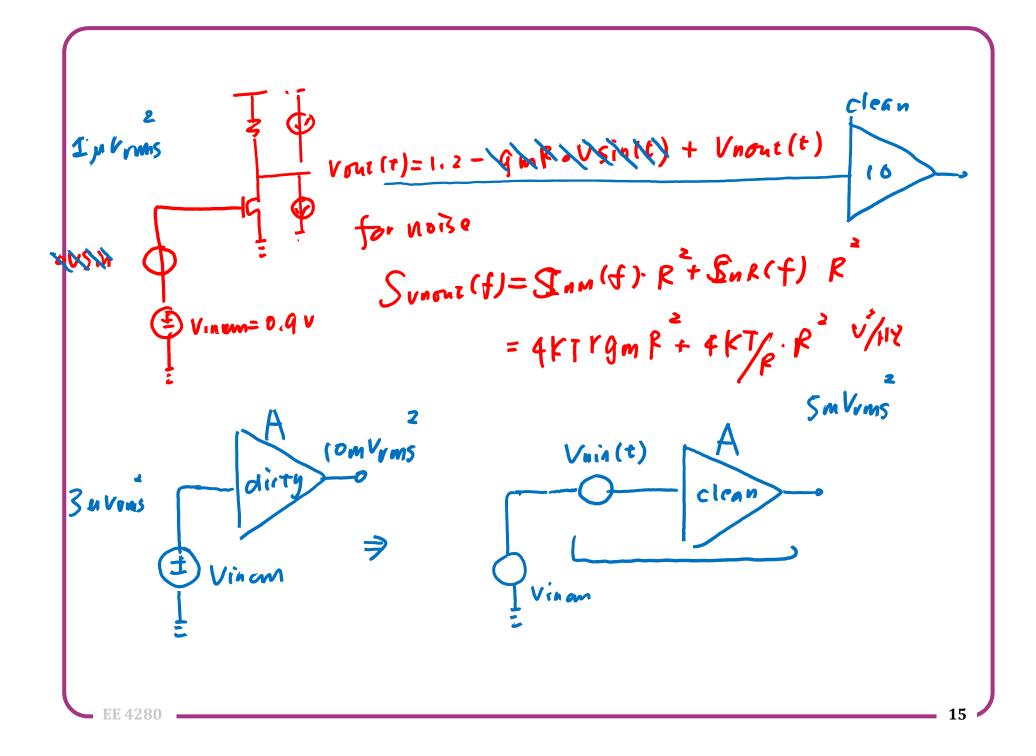
$$\int \frac{fr}{m} \frac{1}{n_{i}n_{i}} = \int \frac{fm}{fr} \frac{S_{in}(f) af}{fr} = 4kTrgm (10^{6} + 10^{3}) + \frac{Kgm^{2}}{Cox}WL (2m 10^{6} + 4m 10^{3})$$

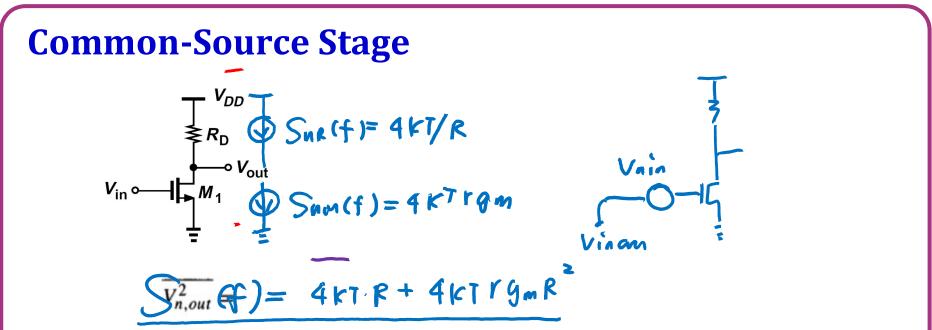
$$EE 4280 = 12$$$$



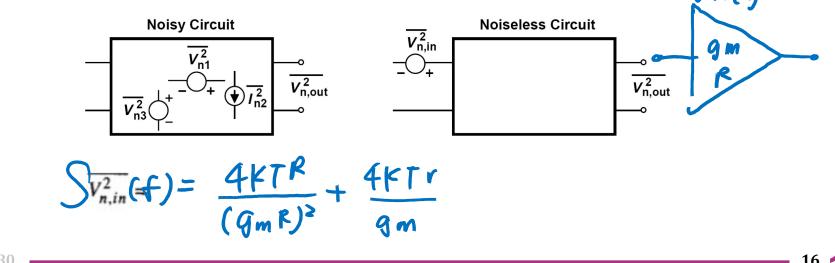
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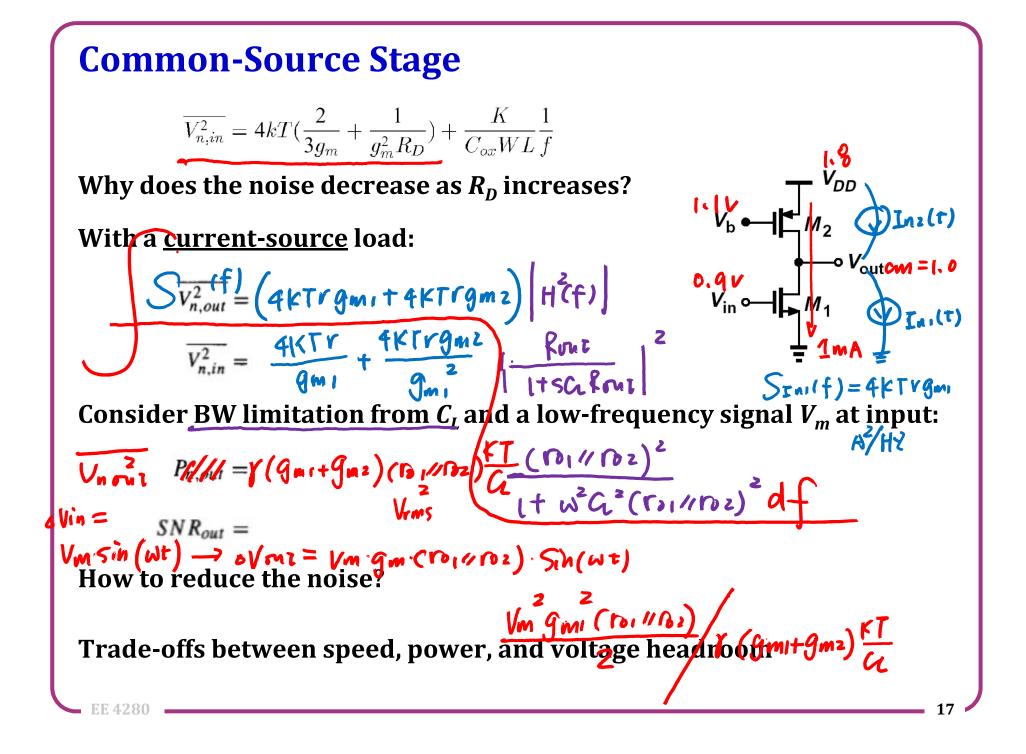


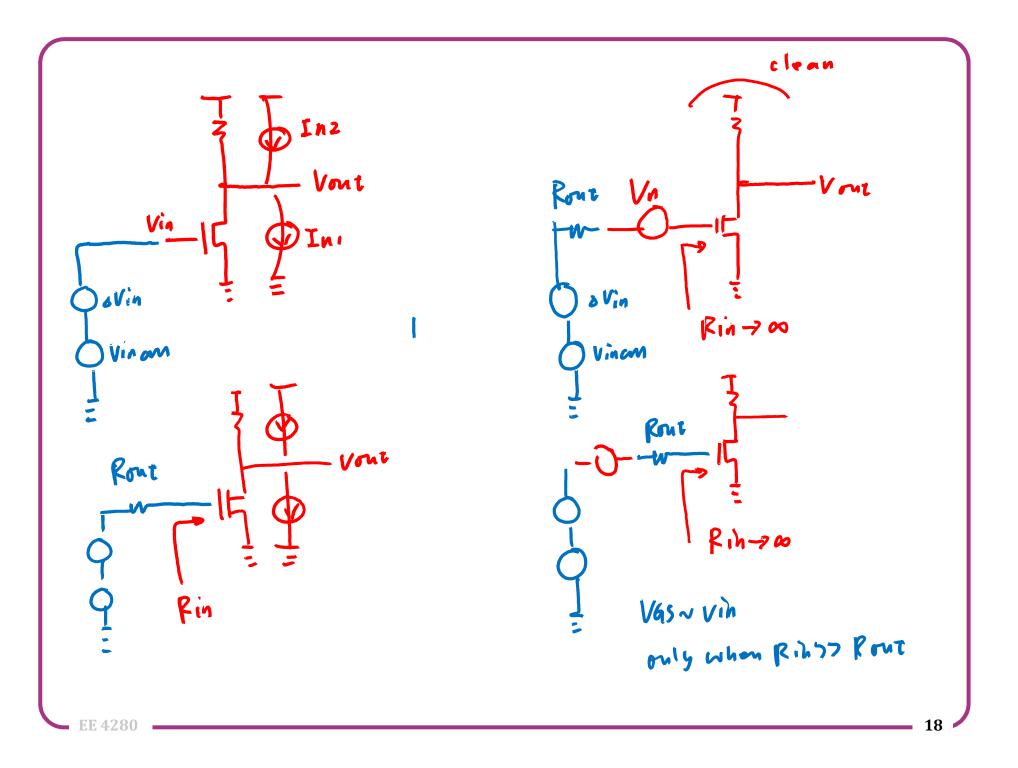


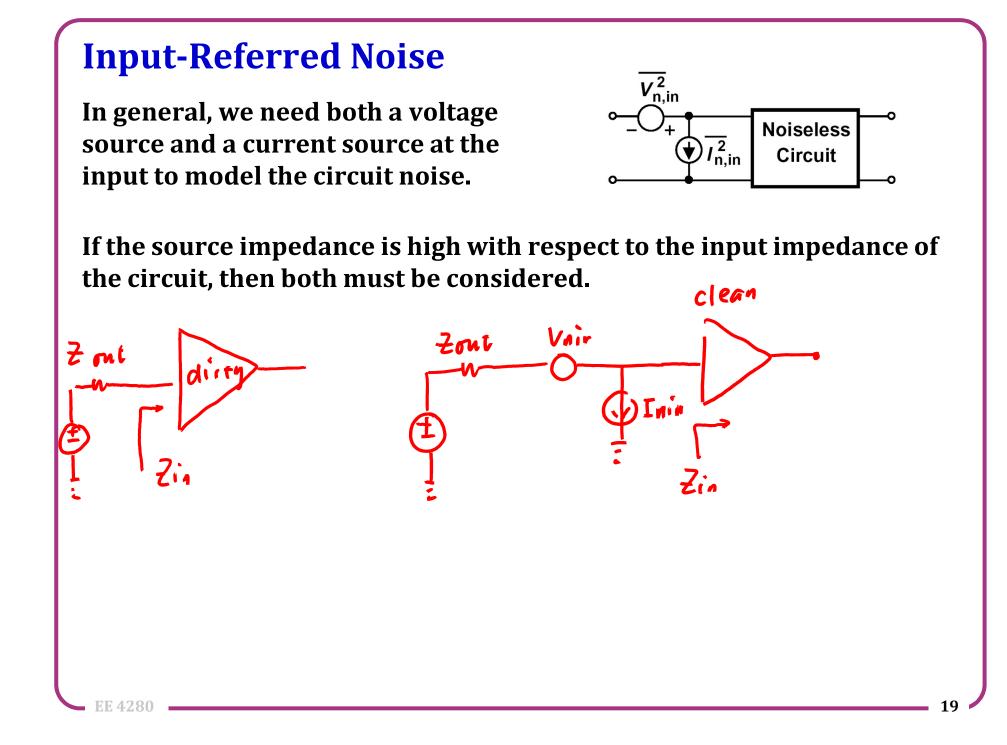


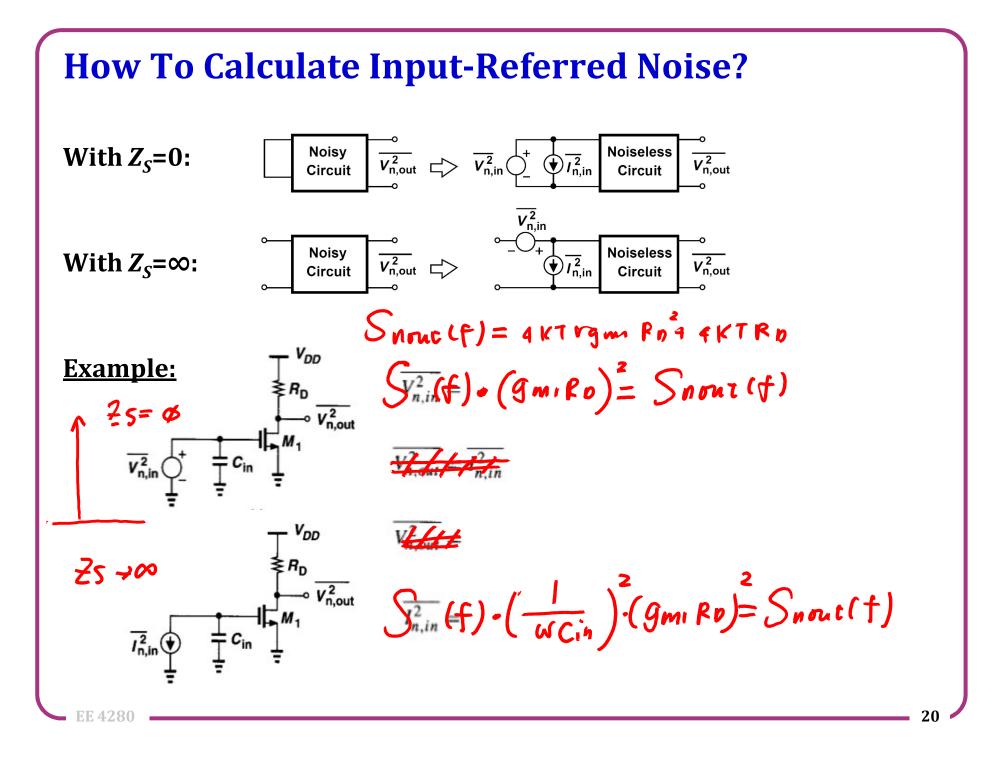
<u>Input-Referred Noise</u> is the noise voltage or current that, when applied to the input of the noiseless circuit, generates the same output noise as the actual circuit does. dirty











Common-Gate Stage

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