# A 1-V CMOS Pseudo-Differential Amplifier With Multiple Common-Mode Stabilization and Frequency Compensation Loops

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*Abstract—***This paper presents an operational amplifier for a 1-V supply voltage. It comprises three gain stages with ac-boosting and buffered Miller feedback compensation circuits. The implementation uses a standard 0.35-** $\mu$ **m CMOS process (** $V_{TN} = 0.6$  **V and**  $V_{TP} = -0.72$  V). To accommodate maximum voltage headroom **between power rails, a pseudo-differential structure is adopted in this amplifier. The large common-mode gain associated with the structure is suppressed by two common-mode stabilization loops. The amplifier driving 100-pF loads achieves a 4.3-MHz gain–band**width product. The settling time of a  $1-V_{pp}$  input step signal is **1.1**  $\mu$ s. The amplifier consumes 249  $\mu$ W and occupies 0.06-mm<sup>2</sup> **silicon area.**

*Index Terms—***CMOS integrated circuits, frequency compensation, low voltage, operational amplifier.**

# I. INTRODUCTION

**A**MPLIFIERS play an important role in most analog circuits because their behavior dominates the performance of the function blocks. For low-power application with a continuously decreasing supply, low-voltage, high-performance amplifier design becomes challenging. This study attempts to accomplish a 1-V operational amplifier without any special or low threshold voltage devices.

To get high dc gain under a low supply voltage, it is unfeasible to stack multiple devices between power rails. One solution is to cascade multiple gain stages. However, the scheme causes extra stability issues because additional low-frequency poles are introduced. The phase margin might be degraded significantly. Many researches worked on the construction of frequency compensation techniques [1]–[6]. These techniques can cancel the nondominant poles with zeros or shift them to higher frequencies to stabilize the multistage amplifiers. One example is the ac-boosting compensation (ACBC) [4], which provides a parallel gain path to bypass the band-limited intermediate stage. Moreover, to avoid the right-half-plane (RHP) zero generated with the Miller compensation-based structures [7], [8], a buffer stage in series with a compensation capacitor can be used to remove the zero by blocking the feedthrough path at high frequency.

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Fig. 1. Three-stage multiloop compensation scheme.

To survive the limited supply voltage, a pseudo-differential structure is adopted to save the voltage drop across the tail current source in a fully differential alternative. Meanwhile, the problems of the high sensitivity on common-mode voltage should be solved. In this study, we adopt a feedforward technique [9] along with the global feedback loop to stabilize the common-mode level. Its efficiency, especially under device mismatch, will be discussed in Section III.

This paper is organized as follows. Section II elucidates the multiloop compensation scheme. Sections III and IV present the circuit implementations and experimental results, respectively. Finally, Section V draws the conclusions.

#### II. FREQUENCY COMPENSATION SCHEME

#### *A. Multiloop Compensation Scheme*

The topology of the proposed low-voltage amplifier is shown in Fig. 1. Transconductance stages  $g_{m1} - g_{m3}$  comprise the three-stage amplifier.  $R_{1,2}$  and  $C_{1,2}$  represent the output resistance and the lumped parasitic capacitance of the first two stages.  $C_L$  and  $R_L$  are the output loading capacitor and resistor, respectively. The feedforward stage  $g_{mf}$ , along with the last gain stage  $g_{m3}$ , forms the push–pull output stage. A transconductance stage  $g_{ma}$  with the output resistance  $R_a$  is introduced to enhance high-frequency gain.  $C_m$  and  $C_a$  are the Miller compensation capacitor and the ac coupling capacitor, respectively. Transconductance  $g_{mb}$  is an isolation stage to block the feedthrough signal in the Miller compensation path.



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To analyze the stability of the proposed multiloop amplifier, a small-signal transfer function is derived. Based on the practical considerations, the following assumptions are made:

$$
R_1, R_2 \gg R_a
$$
  
\n
$$
g_{m1}R_1, g_{m2}R_2, g_{m3}R_L \gg 1
$$
  
\n
$$
C_L \gg C_m
$$
  
\n
$$
C_a \gg C_1, C_2.
$$

Neglecting the second order terms, the open-loop gain of the circuit in Fig. 1 can be expressed as

$$
A(s) = \frac{A_{dc} \left(1 + \frac{s}{\omega_5}\right) \left(1 + \frac{s}{\omega_6} + \frac{s^2}{\omega_6 \omega_7}\right)}{\left(1 + \frac{s}{\omega_{p1}}\right) \left(1 + \frac{s}{\omega_1} + \frac{s^2}{\omega_1 \omega_2} + \frac{s^3}{\omega_1 \omega_2 \omega_3} + \frac{s^4}{\omega_1 \omega_2 \omega_3 \omega_4}\right)}
$$
\n(1)

where  $A_{dc} = g_{m1} R_1 g_{m2} R_2 g_{m3} R_L$  is the dc voltage gain. The dominant pole is located at the first stage output with the equivalent capacitor equal to the Miller capacitor  $C_m$  amplified by the second and third stages as

$$
\omega_{P1} \approx \frac{1}{R_1 A_2 A_3 C_m} = \frac{1}{R_1 g_{m2} R_2 g_{m3} R_L C_m}.
$$
 (2)

The other poles and zeros in (1) can be expressed as follows:

$$
\omega_1 = \frac{1}{\left(A_{2h} + k_t\right)} \frac{g_{m2}}{C_a} \tag{3}
$$

$$
\omega_2 = (A_{2h} + k_t) \frac{g_{m3}g_{mb}R_1}{C_L} \tag{4}
$$

$$
\omega_3 = \frac{1}{R_1 C_1} \tag{5}
$$

$$
\omega_4 = \frac{1}{R_a C_2} \tag{6}
$$

$$
\omega_5 = \frac{g_{mb}}{C_m} \tag{7}
$$

$$
\omega_6 = \frac{1}{(A_{2h} + k_t)} \frac{g_{m2}}{C_a} \tag{8}
$$

$$
\omega_7 = (A_{2h} + k_t) \frac{1}{k_t R_a C_2} \tag{9}
$$

$$
A_{2h} = (g_{m2} + g_{ma})R_a \tag{10}
$$

$$
k_t = \frac{gmj}{g_{m3}}.\tag{11}
$$

The parameter  $A_{2h}$  can be regarded as the high-frequency gain of the second stage, which includes  $g_{m2}$  and the ac-boosting path  $g_{ma}$ . Parameter  $k_t$  is the transconductance ratio of the feedforward stage to the last gain stage. Since there is usually the same static current in the  $g_{m3}$  and  $g_{mf}$  stages,  $k_t$  is approximately one. Using these design equations, the gain–bandwidth product can be expressed as

$$
\omega_0 = 2\pi \cdot \text{GBW} = A_{dc} \cdot \omega_{P1} = \frac{g_{m1}}{C_m}.\tag{12}
$$

# *B. Pole-Zero Allocation*

To optimize the gain–bandwidth product and the phase margin, pole-zero locations should be properly arranged. Since

 $A_{2h}$  is larger than unity,  $C_1$  and  $C_2$  are parasitic capacitances and thus very small; if the  $C_a$  is properly selected, an assumption can be made as follows:

$$
\omega_1 \ll \omega_2 \ll \omega_3 \ll \omega_4. \tag{13}
$$

The locations of the nondominant poles can be described by the following equations:

$$
p_{nd1} = -\omega_1 = -\frac{1}{(A_{2h} + k_t)} \frac{g_{m2}}{C_a} \tag{14}
$$

$$
p_{nd2} = -\omega_2 = -(A_{2h} + k_t) \frac{g_{m3}g_{mb}R_1}{C_L} \tag{15}
$$

$$
p_{nd3} = -\omega_3 = -\frac{1}{R_1 C_1} \tag{16}
$$

$$
p_{nd4} = -\omega_4 = -\frac{1}{R_a C_2}.\tag{17}
$$

The high-frequency poles  $\omega_3$  and  $\omega_4$  are far away from the unitygain frequency because  $C_1$  and  $C_2$  are small. With the similar assumptions, zeros in (1) can be derived as

$$
z_{LHP1} = -\omega_5 = -g_{mb}/C_m \tag{18}
$$

$$
z_{LHP2} = -\omega_6 = -\frac{1}{(A_{2h} + k_t)} \frac{g_{m2}}{C_a} \tag{19}
$$

$$
z_{LHP3} = -\omega_7 = -(A_{2h} + k_t) \frac{1}{k_t R_a C_2}.
$$
 (20)

The first nondominant pole  $p_{\text{nd1}}$  and the LHP zero  $z_{\text{LHP2}}$  can be completely cancelled according to (14) and (19). Therefore, the first nondominant pole is then  $p_{\text{nd2}}$ . The  $z_{\text{LHP3}}$  is also far away from the unity-gain frequency and thus negligible. Based on these analysis, the overall phase margin can be determined as

$$
PM = 90^{\circ} - \tan^{-1} \frac{2\pi GBW}{|p_{\text{nd}2}} + \tan^{-1} \frac{2\pi GBW}{|z_{\text{LHP1}}|}.
$$
 (21)

#### III. CIRCUIT DESIGNS

#### *A. Pseudo-Differential Input Stage With CMFF*

Fully differential (FD) and pseudo-differential (PD) are two circuit topologies that can be used to achieve differential input stage. The FD amplifier consists of a differential pair with a tail current source, while the PD amplifier has two independent single-ended common source amplifiers. Compared with the FD structure, the PD structure has larger voltage headroom since there is no voltage drop across the tail transistor. This keeps a larger margin for process and temperature variations under low supply voltage. However, since its common-mode gain is the same as its differential gain, the PD amplifier is incapable of rejecting common-mode signal fluctuation. Therefore, a fast and powerful common-mode stabilization circuit is required in the PD amplifier.

Fig. 2 shows the proposed pseudodifferential input stage. It uses a common-mode feedforward circuit to setup the output common mode against the input common-mode variation. The circuit operations can be described as follows. First, the input voltage is decomposed of a common-mode term  $V_{\text{ICM}}$  and a differential term  $v_d$ . They can be expressed as  $V_{ip} = V_{\text{ICM}} + v_d/2$ and  $V_{\text{in}} = V_{\text{ICM}} - v_d/2$ . The input transistors  $M_{11a,b}$ , along



Fig. 2. Circuit diagram of the pseudo-differential input stage.

with the current mirrors  $M_{12a} - M_{13a}$  and  $M_{12b} - M_{13b}$ , convert the input differential voltage to the current signal. The differential currents are summed up at the diode-connected transistor  $M_{14}$  as

$$
I_{\rm CM} = I_{M14} = I_{M15a,b} \tag{22}
$$

$$
=\frac{I_1 + I_2}{2} + I_{bias} \tag{23}
$$

$$
=K_p \left(\frac{W}{L}\right)_{11} \left[ V_{\text{ov}}^2 + \left(\frac{v_d}{2}\right)^2 \right] + I_{\text{bias}} \qquad (24)
$$

where  $V_{\text{ov}} = V_{\text{DD}} - V_{\text{ICM}} - |V_{\text{TP}}|$  is the overdrive voltage of the input transistors  $M_{11a,b}$ .  $I_{bias}$  is a small constant current to keep transistors  $M_{12a,b}$  in the saturation region. After subtracting  $I_{\text{CM}}$  from the drain currents of  $M_{16a}$  and  $M_{16b}$ , the residue current is expressed as

$$
I_{\rm op1} = I_{\rm CM} - (I_1 + I_{\rm bias}) = (I_2 - I_1)/2 \tag{25}
$$

$$
=K_p \left(\frac{W}{L}\right)_{11} \cdot V_{\text{ov}} \cdot \frac{v_d}{2} \tag{26}
$$

$$
= g_{m11} \frac{v_d}{2} = -I_{on1}.
$$
 (27)

The differential output current then becomes

$$
I_{\text{od}} = I_{\text{op1}} - I_{\text{on1}} = I_2 - I_1 = g_{m11}v_d. \tag{28}
$$

By using the feedforward technique, the differential output current of the PD amplifier becomes the function of the input transconductance and the voltage difference of two inputs and is similar to the FD amplifier. If no mismatch exists between two paths, the common-mode gain of the circuit is zero. However, a pseudo-differential structure always suffers from mismatch. It is more severe in a high-gain stage because the offset in the front stage may smear the input small signal and lead to a saturated output voltage in the following gain stages. The post-layout Monte Carlo simulation is adopted here to further confirm the influence of path mismatch. Fig. 3 depicts the common-mode gain distributions at node A and node B for 500 samples with local mismatches of the circuit parameters. The common-mode gain at node A is about  $-11$  dB, while the common-mode gain at node B can decrease to a mean value of  $-69.2$  dB. Although the distribution is sporadic, it can provide at least an order suppression with this technique.



Fig. 3. Statistical distribution of the common-mode gain from 500 Monte Carlo simulations: (a) at node A, (b) at node B in Fig. 2.



Fig. 4. The schematic of the second and the third gain stages. Only a half of differential circuit is depicted for clarity.

# *B. Intermediate and Output Stage With Frequency Compensation and CMFB*

The schematics of the proposed second and third stages are depicted in Fig. 4. The second stage is composed of transistors  $M_{21} - M_{26}$ . Transistors  $M_{a1} - M_{a5}$  and one capacitor  $C_a$  realize the gain-boost path  $g_{ma}$ . The output stage employs a push–pull structure to improve the slew rate. The Miller capacitor  $C_m$  along with the buffer stage  $g_{mb}$  forms the frequency compensation loop, which splits the poles at the input and output stages for closed-loop stability. The buffer can prevent the generation of the RHP zero and the phase response can therefore be improved.

A common-mode feedback (CMFB) circuit is mandatory to set up the common-mode voltage of the two output nodes for a differential amplifier. To attain maximum output swing, the output voltage should be half of the power supply, where 0.5 V is set in this case. Unfortunately, this voltage level is too small to turn on neither p- nor n-type transistors of the adopted technology. To solve this problem, a current-compared CMFB circuit in Fig. 5 is used [10]. The common-mode current is extracted by the resistors  $2R$ . The detected common-mode signal is then compared with a reference signal generated by  $V_{\text{ocm}}$ over  $R$  to produce the feedback voltage  $V_{\rm cmc},$  which results in a voltage change at the gates of  $M_{19a,b}$  in Fig. 2. The dc gain of



Fig. 5. Current-compared CMFB circuit.



Fig. 6. Die photograph of the proposed operational amplifier.

TABLE I CIRCUIT PARAMETERS OF THE PROPOSED AMPLIFIER

$g_{m1}=29\mu S$	$g_{m2} = 150 \mu S$	$g_{m3} = 450 \mu S$
$g_{ma} = 500 \mu S$	$g_{mb} = 150 \mu S$	$g_{m f} = 450 \mu S$
$C_m = 1$ pF	$C_a = 0.55pF$	off-chip $C_L = 100pF$

the common-mode feedback path is determined by the current sensing resistor and the transconductance of  $M_{c7}$ .

#### IV. EXPERIMENTAL RESULTS

A three-stage operational amplifier with multiple frequency compensation and common-mode stabilization loops is designed for a single 1-V supply operation. This amplifier was fabricated in a  $0.35-\mu m$  standard CMOS technology with threshold voltages of nMOS and pMOS equal to 0.6 and  $-0.72$  V, respectively. Fig. 6 shows the photograph of the integrated amplifier. The circuit parameters and other component values are listed in Table I.

The open-loop gain and phase response of the proposed amplifier are plotted in Fig. 7. The simulated dc gain is around 80 dB with a unity-gain frequency of 5.4 MHz and  $71^\circ$  phase margin driving 100-pF loadings. The measured unity-gain frequency is 4.3 MHz and the phase margin is  $68^\circ$ . The measured common-mode rejection ratio (CMRR) at 100 kHz is larger than 45 dB.

For the p-type input stage, 0.1-V bias is selected because the bias level has to be lower than  $V_{\text{DD}} - V_{\text{GS},11}$ . Fig. 8 is the low-voltage bias scheme adopted in this design [10]. Two



Fig. 7. Gain and phase responses of the open-loop measurements.



Fig. 8. Closed-loop connection for low-input voltage biasing.



Fig. 9. Measured unity-gain step response.

TABLE II PERFORMANCE SUMMARY

$A_{dc}$	$80.2dB*$	GBW	4.3MHz	
SR	$1.20/1.22$ V/ $\mu$ s	Phase Margin	$68^{\circ}$	
$\mathrm{V}_{dd}$	1 V	$TS_{+/-}$ (to 0.1%)	$1.17/1.13 \mu s$	
$\mathrm{I}_{dd}$	$249\mu$ A	Power	$249 \mu W$	
THD	$-60.7dB#$	Active Area	$0.06$ mm <sup>2</sup>	

\* derived from post-layout simulation.

# 1- $V_{pp}$ , 200-kHz sine wave.

bias resistors  $R_b$  are connected between the input nodes to the ground to provide the dc paths required by  $R_i$  and  $R_f$ .

Fig. 9 depicts the measured step response in unity-gain configuration. The response to a  $1-V_{\rm pp}$  50-kHz square wave

Design Feature	Blalock'98 [11]	Carrillo'00 [12]	Chatterjee'05 [13]	Bez-Villegas'06 [14]	This Work
Technology	$2\mu$ m CMOS	$1.2\mu$ m CMOS	$0.18 \mu m$ CMOS	$0.5 \mu m$ CMOS	$0.35 \mu m$ CMOS
Supply Voltage (V)			0.5		
Differential Output	NO.	NO.	<b>YES</b>	N <sub>O</sub>	<b>YES</b>
Current (mA)	0.287	0.208	0.150	0.095	0.249
$DC$ Gain $(dB)$	49	70.5	62	60	80
Unity Gain Bandwidth	.3MHz @22pF	$2.1$ MHz $@15pF$	10MHz @20pF	4.1MHz $@15pF$	4.3MHz @100pF
Slew Rate $(V/\mu s)$	0.7/1.6	0.9/1.7	2.0	0.8/0.86	1.2/1.22
FOM <sub>S</sub> (GBW $\times$ C <sub>L</sub> /Power)	100	151	2667	647	1730
FOM <sub>L</sub> (SR <sub>avg</sub> ×C <sub>L</sub> /Power)	88.2	93.8	533	131.1	485.9

TABLE III COMPARISON WITH OTHER LOW-VOLTAGE AMPLIFIERS

demonstrates a slew rate of 1.2  $V/\mu s$  and a settling time of 1.13  $\mu$ s with 0.1% error tolerance. Total power dissipation is 249  $\mu$ W under a single 1-V supply. Table II summarizes the performance. Table III presents the parameters among several state-of-the-art low-voltage amplifiers. This study exhibits competitive figure of merits in both small-signal and large-signal performances.

### V. CONCLUSION

This paper presents the design techniques for a multistage differential amplifier with a supply voltage of 1-V in a  $0.35$ - $\mu$ m standard CMOS technology. The pseudo-differential topology with the common-mode feedforward bias extends the voltage swing of the input stage. The amplifier using the parallel gain booster, buffered Miller feedback, and feedforward frequency compensations exhibits high speed, high linearity, and fast settling with a small increase in circuit complexity and power consumption.

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