

# Transconductance With Capacitances Feedback Compensation for Multistage Amplifiers

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**Abstract**—A new performance-boosting frequency compensation technique is presented, named Transconductance with Capacitances Feedback Compensation (TCFC). A transconductance stage and two capacitors introduce negative feedback to a three-stage amplifier, which significantly improves the performance such as gain-bandwidth product, slew rate, stability and sensitivity.

An optimized TCFC amplifier has been implemented, and fabricated in a 0.35- $\mu\text{m}$  CMOS process. The TCFC amplifier driving a 150-pF load capacitor achieved 2.9-MHz gain-bandwidth product dissipating only 45- $\mu\text{W}$  power with a 1.5 V supply, which shows a significant improvement in MHz  $\cdot$  pF/mA performance.

**Index Terms**—Amplifier, compensation, low power, multistage.

## I. INTRODUCTION

As the supply voltage continues to scale down, multistage amplifiers are becoming more and more essential. The methodologies to design multistage amplifiers are much in demand. Due to the complexity of a multistage amplifier, the stabilization is difficult to achieve. A special frequency compensation measure must be taken to ensure stability. For this purpose, some frequency-compensation topologies such as Nested Miller Compensation (NMC) [1] have been used to implement multistage amplifiers. In these amplifiers, although the stability problem has been basically solved, the enormous power dissipation and bandwidth reduction remain a serious problem. In order to minimize the power-consuming effect of the Miller capacitances on multistage amplifiers, a new topology, Transconductance with Capacitances Feedback Compensation (TCFC) is presented in this paper. As demonstrated later, a transconductance stage and two capacitors are added to introduce negative feedback to a three-stage amplifier achieving stability, such that the power dissipation is considerably reduced while the frequency characteristics and transient response are improved significantly.

## II. REVIEW OF NESTED MILLER COMPENSATION

In the three-stage NMC topology, there are two Miller capacitors  $C_{m1}$  and  $C_{m2}$  connected from the output to the output of each stage, respectively, forming two negative feedback loops. They stabilize the amplifier but seriously reduce the high-frequency gain. As a result, extra power is needed to compensate this gain reduction. Moreover, the Miller capacitor  $C_{m2}$  that shorts the last stage gives the additional disadvantages that the

phase shift reaches  $180^\circ$  as frequency increases, leading to a positive-feedback loop involving  $C_{m1}$ ,  $g_{m2}$ , and  $C_{m2}$ , which is a serious source of instability. Therefore, the transconductance  $g_{m3}$  must be large enough to counter this shorting effect. To ensure stability, the last-stage transconductance  $g_{m3}$  required in a three-stage NMC amplifier is given by

$$g_{m3} \geq 4(2\pi \text{ GBW})C_L. \quad (1)$$

Apparently, in a NMC amplifier, the required transconductance for the last stage alone is four times the transconductance for a single-stage amplifier. It is thus not suited for low-power applications. Obviously, this power-consuming effect is mainly caused by the inner Miller capacitor  $C_{m2}$ . The first Miller capacitor  $C_{m1}$  causes the slope to be  $-20$  dB per decade in frequency, as in any amplifier. Hence, it is the second Miller capacitor  $C_{m2}$  which causes an unnecessary reduction in high-frequency gain such that a large transconductance  $g_{m3}$  is needed for the last stage.

In some topologies such as NGRNMC [2], a nulling resistor is added to ease the high-frequency-gain reduction and the shorting effect on the last stage caused by the inner Miller capacitor. However, the performance improvement is not sufficient since the nulling resistance has to be kept small enough to keep the Miller capacitance to be effective for pole splitting.

Based on these considerations, it becomes clear that taking away the inner Miller capacitor  $C_{m2}$  could be a possible way to achieving better performance. However in this case the first nondominant pole would be determined by parasitic capacitances, resulting in layout-sensitive circuits. Moreover, a safe gain margin would not be ensured due to the effects of the zeros caused by the parasitic capacitances. Besides, since the second-stage dc gain  $A_{v2}$  appears in the expression of the first nondominant pole as a multiplier to other parameters, the sensitivity must be high.

For sake of comparison, the case that the inner Miller capacitor is excluded from the three-stage NMC topology is discussed first and presented in the next section.

## III. UNIQUE MILLER COMPENSATION

The case that the inner Miller capacitor is excluded from the three-stage NMC topology is referred to as Unique Miller Compensation (UMC), which is shown in Fig. 1.

In Fig. 1,  $g_{m1-3}$  and  $R_{1-3}$  represent the transconductance and output resistance of each stage, respectively.  $C_{1-3}$  symbolize the lumped parasitic capacitance of each stage.  $C_{m1}$  is the unique Miller capacitor, accomplishing the frequency compensation.  $C_L$  is the load capacitor.

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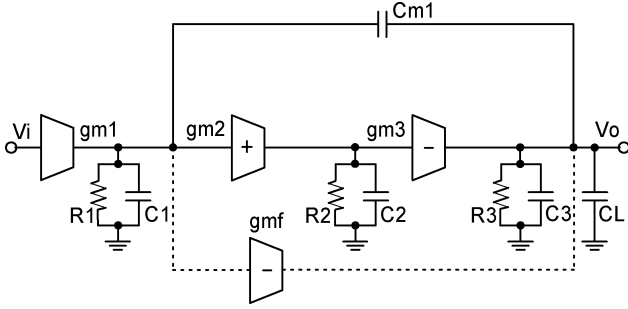


Fig. 1. Unique Miller compensation (UMC) topology.

The small-signal transfer function of the open-loop gain of the UMC amplifier is given by

$$A_v(s) = \frac{A_{dc} \left(1 + \frac{s}{\omega_3} + \frac{s^2}{\omega_3\omega_4}\right)}{\left(1 + \frac{s}{|p_{-3dB}}\right) \left(1 + \frac{s}{\omega_1} + \frac{s^2}{\omega_1\omega_2}\right)}. \quad (2)$$

where  $A_{dc}$  and  $p_{-3dB}$  are the dc gain and the dominant pole, respectively, which are given as

$$A_{dc} = g_{m1}g_{m2}g_{m3}R_1R_2R_3 \quad (3)$$

$$p_{-3dB} = -\frac{1}{g_{m2}g_{m3}R_1R_2R_3C_{m1}}. \quad (4)$$

Another important frequency factor  $\omega_0$ , which represents the gain-bandwidth product (GBW), is given by

$$\omega_0 = 2\pi \text{GBW} = A_{dc}|p_{-3dB}| = \frac{g_{m1}}{C_m}. \quad (5)$$

$\omega_{1-2}$  and  $\omega_{2-3}$  are the frequency factors in the denominator and the numerator of (2) respectively. They are given by

$$\omega_1 = A_{v2} \frac{g_{m3}}{C_L} \quad (6)$$

$$\omega_2 = \frac{1}{R_2C_2} \quad (7)$$

$$\omega_3 = -A_{v2} \frac{g_{m3}}{C_m} \quad (8)$$

$$\omega_4 = \frac{1}{R_2C_2}. \quad (9)$$

in which  $A_{v2} (= g_{m2}R_2)$  is the gain of the second stage.

Although  $C_2$  is a lumped parasitic capacitance, the frequency factor  $\omega_2$  cannot be kept high since the second-stage output resistance  $R_2$  is large with regard to the other small equivalent resistance  $1/g_m$ . Consequently, this results in a complex-pole arrangement for the nondominant poles. In this case, both the frequency factors  $\omega_1$  and  $\omega_2$  determine the location of the first nondominant pole. Therefore, in the unity-feedback configuration, to ensure a third-order Butterworth frequency response with the damping ratio  $\zeta = (1/2Q) = 0.707$ , the stability conditions are given by

$$\omega_0 = 2\pi\text{GBW} = \frac{1}{2}\omega_1 = \frac{1}{2}A_{v2} \frac{g_{m3}}{C_L} = \frac{1}{4}\omega_2 = \frac{1}{4} \frac{1}{R_2C_2}. \quad (10)$$

Clearly, the stability conditions given in (10) are hard to maintain, since both  $A_{v2}$  and  $R_2$  cannot be accurately specified. They are greatly dependent on the operating points of the rel-

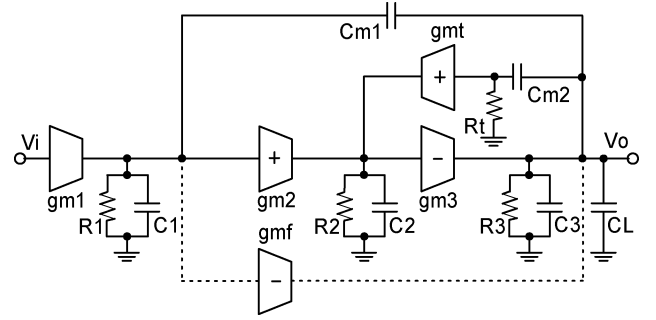


Fig. 2. TCFC topology.

evant transistors. Moreover, the lumped parasitic capacitance  $C_2$ , which is also imprecise, can inevitably lead to vulnerable layout-dependent circuits. In conclusion, with the three imprecise values:  $A_{v2}$ ,  $R_2$ , and  $C_2$ , the stability condition (10) cannot be reliably ensured in practical implementations.

Even if the feed-forward stage  $g_{mf}$ , as shown by dotted lines in Fig. 1, is taken into account, the effects of the imprecise parameters are still in existence. As such the problem remains unsolved.

Therefore, other topologies have to be devised. The NMC has accomplished this by employing another Miller capacitor  $C_{m2}$ . However, due to the loading and shorting impact of the inner Miller capacitor, the high-frequency gain and the gain-bandwidth product are badly reduced. Although the use of the nulling resistor can ease this impact, the performance improvement is still limited since the nulling resistance cannot be too large to keep the Miller capacitance effective.

In order to further supplement the techniques on implementing low-power multistage amplifiers and further overcome the disadvantages of the sensitivity and the stability uncertainty as well as the operation unreliability due to the imprecise parameters in designing multistage amplifiers, the new topology, TCFC, is proposed and described in the next section

#### IV. TRANSCONDUCTANCE WITH CAPACITANCES FEEDBACK COMPENSATION

##### A. Topology

The three-stage TCFC topology, using transconductance with capacitance feedback as a compensation technique, is shown in Fig. 2.

The transconductance stages  $g_{m1}$ ,  $g_{m2}$  and  $g_{m3}$  compose the conventional three-stage amplifier. The output resistance and the lumped parasitic capacitance of each stage are represented by  $R_{1-3}$  and  $C_{1-3}$ , respectively.  $C_L$  is a load capacitor.

$C_{m1}$  is the Miller capacitor forming the outer feedback loop. Capacitance  $C_{m2}$  along with the transconductance stage  $g_{mt}$  makes up the internal feedback loop. As  $C_{m2}$  is separated from the internal node by the transconductance stage  $g_{mt}$ , the high-frequency shorting effect on the last stage is avoided. Therefore, positive-feedback phenomena cannot be present and the stability can be well ensured even with a small transconductance in the last stage. Moreover, since only parasitic capacitances are connected to the internal node, the second-stage high-frequency gain reduction is minimized. Furthermore, the param-

eters of the feedback loop involving  $g_{mt}$  and  $C_{m2}$  can be adequately adapted, as a consequence, a suitable gain reduction above the unity-gain frequency is generated, achieving a sufficient gain margin. In this way, the effects of the parasitic device parameters are eliminated due to the negative feedback, minimizing the sensitivity and dependability to device parameters and layout variability.

To improve the large-signal performance such as slew rate, a feed-forward stage  $g_{mf}$ , with which the last stage constitutes a push-pull output stage, is easily included in the TCFC topology as shown by the dotted lines in Fig. 2.

### B. Transfer Function

The small-signal transfer function of the open-loop gain of the TCFC amplifier shown in Fig. 2 can be obtained by means of analyzing its equivalent small-signal circuit.

For simplification, we assume that the dc gain and the output resistance of each stage are large enough, all the compensating capacitances are much larger than the relevant parasitic capacitances and far smaller than the load capacitance, as given by

$$g_{m1}R_1, g_{m2}R_2, g_{m3}R_3 \gg 1 \quad (11)$$

$$C_{m1} \gg C_1, C_{m2} \gg C_2 \quad (12)$$

$$C_{m1}, C_{m2} \ll C_L. \quad (13)$$

Also, for simplicity, the following relation is presumed:

$$R_t = \frac{1}{g_{mt}}. \quad (14)$$

Thus, the small-signal transfer function of the open-loop gain of the TCFC amplifier can then be expressed by a fourth-order expression which is given by

$$A_v(s) = \frac{A_{dc} \left( 1 + \frac{s}{\omega_4} + \frac{s^2}{\omega_4\omega_5} + \frac{s^3}{\omega_4\omega_5\omega_6} \right)}{\left( 1 + \frac{s}{|p_{-3dB}|} \right) \left( 1 + \frac{s}{\omega_1} + \frac{s^2}{\omega_1\omega_2} + \frac{s^3}{\omega_1\omega_2\omega_3} \right)}. \quad (15)$$

In (15), all the symbols are defined by (16)–(24) and explained afterwards.

$$A_{dc} = g_{m1}g_{m2}g_{m3}R_1R_2R_3 \quad (16)$$

$$p_{-3dB} = -\frac{1}{C_{m1}g_{m2}g_{m3}R_1R_2R_3} \quad (17)$$

$$\omega_1 = \frac{1}{1+k_t} \frac{g_{m2}}{C_{m2}} \quad (18)$$

$$\omega_2 = (1+k_t) \frac{C_{m2}}{C_2} \frac{g_{m3}}{C_L} \quad (19)$$

$$\omega_3 = \frac{1}{k_t} \frac{g_{m2}}{C_{m2}} \quad (20)$$

$$\omega_4 = \frac{1}{k_t} \frac{g_{m2}}{C_{m2}} \quad (21)$$

$$\omega_5 = -k_t \frac{C_{m2}}{C_2} \frac{g_{m3}}{g_{m1}} \omega_0 \quad (22)$$

$$\omega_6 = \frac{1}{k_t} \frac{g_{m2}}{C_{m2}} \quad (23)$$

$$k_t = \frac{g_{m2}}{g_{mt}}. \quad (24)$$

$A_{dc}$  is the low-frequency gain.  $p_{-3dB}$  is the dominant pole.  $\omega_{1-3}$  and  $\omega_{4-6}$  represent frequency factors in the denominator and numerator of (15), respectively. Finally,  $k_t$  is a transconductance ratio of the second stage  $g_{m2}$  to the feedback stage  $g_{mt}$ . In this design, its value is 2.

In (22),  $\omega_0$  is another important frequency factor, which represents the gain-bandwidth product and is given by

$$\omega_0 = 2\pi \text{GBW} = A_{dc}|p_{-3dB}| = \frac{g_{m1}}{C_m}. \quad (25)$$

### C. Stability and Gain-Bandwidth Product

The stability is studied on the closed-loop transfer function in the unity-gain feedback configuration, which can be given by (26) after neglecting the zeros. In fact, there is one effective left half plane (LHP) zero since  $C_m$  is much smaller than  $C_L$ . Moreover, as the order of the numerator of  $A_{cl}(s)$  is less than that of the denominator, the stability depends on the denominator [10].

$$A_{cl}(s) = \frac{1}{1 + \frac{s}{\omega_0} + \frac{s^2}{\omega_0\omega_1} + \frac{s^3}{\omega_0\omega_1\omega_2} + \frac{s^4}{\omega_0\omega_1\omega_2\omega_3}}. \quad (26)$$

By applying Routh stability criterion, the stability conditions can be obtained as

$$\omega_3 = \frac{1}{k_t} \frac{g_{m2}}{C_{m2}} > \omega_1 = \frac{1}{1+k_t} \frac{g_{m2}}{C_{m2}} \quad (27)$$

$$\omega_0 = 2\pi \text{GBW} < \frac{C_{m2}}{C_2} \frac{g_{m3}}{C_L}. \quad (28)$$

Obviously, the condition (27) is always satisfied when  $k_t > 0$ . Remember that  $k_t$  is the transconductance ratio of  $g_{m2}$  to  $g_{mt}$ , which is always a positive value. Therefore, the other condition (28) becomes the key limitation of the gain-bandwidth product. According to (28), for a specific transconductance  $g_{m3}$  driving a given load capacitance  $C_L$ , the achievable gain-bandwidth product GBW depends on the ratio  $C_{m2}/C_2$ . Obviously, this ratio can be made large, since  $C_2$  is a lumped parasitic capacitance which is rather small compared with the compensation capacitance  $C_{m2}$ . Hence, this proves theoretically that the gain-bandwidth product of the TCFC amplifier can be extended significantly with respect to that of the NMC amplifier.

### D. Design Constraints

The design constraints are usually dependent on the pole-zero locations of the open-loop small-signal transfer function. In order to optimize the gain-bandwidth product as well as the phase margin, it is important to arrange properly the pole-zero locations.

Since the ratio  $C_{m2}/C_2$  can be made large, it can be supposed that  $\omega_2$  is sufficiently higher than  $\omega_1$ , as given by

$$\omega_1 = \frac{1}{1+k_t} \frac{g_{m2}}{C_{m2}} \ll \omega_2 = (1+k_t) \frac{C_{m2}}{C_2} \frac{g_{m3}}{C_L}. \quad (29)$$

Thus, the first nondominant pole is determined by  $\omega_1$ , which is given by

$$p_{nd1} = -\omega_1 = -\frac{1}{1+k_t} \frac{g_{m2}}{C_{m2}}. \quad (30)$$

The first nondominant pole given in (30) is obviously independent of imprecise parasitic capacitances. Moreover, since the other nondominant poles are far higher than the first nondominant pole, their effects on phase margin are insignificant. In a similar way, the zeros can be determined as well. Since the ratio  $C_{m2}/C_2$  is large and  $g_{m3}$  is usually larger than  $g_{m1}$ , the frequency factor  $\omega_5$  is much larger than  $\omega_0$  or  $2\pi\text{GBW}$ . The following condition can thus be well satisfied:

$$\omega_4 = \frac{1}{k_t} \frac{g_{m2}}{C_{m2}} \ll |\omega_5| = k_t \frac{C_{m2}}{C_2} \frac{g_{m3}}{g_{m1}} \omega_0. \quad (31)$$

Due to the very large frequency factor  $\omega_5$ , two zeros only show up at very high frequencies. As a consequence, only one LHP zero is left, which is given by

$$z_{\text{LHP1}} \approx -\omega_4 = -\frac{1}{k_t} \frac{g_{m2}}{C_{m2}} = \frac{1+k_t}{k_t} p_{nd1}. \quad (32)$$

According to (32), the LHP zero  $z_{\text{LHP1}}$  which improves the phase margin, is obviously located higher than the first nondominant pole. This leads to the desired open-loop frequency response and does not deteriorate the gain margin.

Based on these considerations, the overall phase margin can be given by

$$\text{PM} \approx 90^\circ - \arctan \frac{2\pi \text{GBW}}{|p_{nd1}|} + \arctan \frac{2\pi \text{GBW}}{|z_{\text{LHP1}}|}. \quad (33)$$

A similar compensation scheme has been used before on two-stage amplifiers [13]. It does not provide the same precise positioning of the LHP zero, however.

### E. Finite Output Resistance

In practice, the output resistances of each stage are not infinitely high. In the TCFC amplifier, the finite output resistance  $R_2$  may affect the high-frequency behavior. The influence of this finite output resistance  $R_2$  is considered next.

First, the frequency factors  $\omega_{1-3}$  that determine the nondominant poles are examined, which are given by

$$\omega_1 \approx \frac{1}{1+k_t + \frac{1}{A_{v2}} \frac{C_L}{C_{m2}}} \frac{g_{m2}}{C_{m2}} \quad (34)$$

$$\omega_2 \approx \frac{1+k_t + \frac{1}{A_{v2}} \frac{C_L}{C_{m2}}}{1 + \frac{k_t}{A_{v2}} \frac{C_{m2}}{C_2}} \frac{C_{m2}}{C_2} \frac{g_{m3}}{C_L} \quad (35)$$

$$\omega_3 \approx \frac{1}{k_t} \frac{g_{m2}}{C_{m2}} + \frac{1}{R_2 C_2}. \quad (36)$$

Herein,  $A_{v2}$  is the second-stage low frequency gain, which is given by

$$A_{v2} = g_{m2} R_2. \quad (37)$$

Comparing these frequency factors  $\omega_{1-3}$  with those given in (18) – (20), it is seen that  $\omega_3$  tends to shift upwards while  $\omega_1$  which determines the first nondominant pole goes downwards. The frequency factor  $\omega_2$  may also move downwards but not as far as  $\omega_1$  does. This means that the nondominant poles are separated even further compared to the case of the infinite second-stage output resistance  $R_2$  discussed before. Consequently, the

stability condition  $\omega_3 > \omega_1$  is satisfied more sufficiently. Moreover, the assumption  $\omega_2 \gg \omega_1$ , which is supposed to minimize the sensitivity, can still be well ensured.

In a similar way, the frequency factors  $\omega_{4-6}$  which determine the zeros are examined and given by

$$\omega_4 \approx \frac{1}{k_t - \frac{1}{A_{v2}} \frac{C_{m1}}{C_{m2}}} \frac{g_{m2}}{C_{m2}} \quad (38)$$

$$\omega_5 \approx \frac{\frac{1}{A_{v2}} \frac{C_{m1}}{C_{m2}} - k_t}{1 + \frac{k_t}{A_{v2}} \frac{C_{m2}}{C_2}} \frac{C_{m2}}{C_2} \frac{g_{m3}}{g_{m1}} 2\pi\text{GBW} \quad (39)$$

$$\omega_6 \approx \frac{1 + \frac{k_t}{A_{v2}} \frac{C_{m2}}{C_2}}{k_t} \frac{g_{m2}}{C_{m2}}. \quad (40)$$

Apparently, the frequency factor  $\omega_4$  is larger than  $\omega_1$ . The first LHP zero  $z_{\text{LHP1}}$  is thus located higher than the first nondominant pole  $p_{nd1}$ . This is desired and is the same case as discussed in the case of infinite second-stage output resistance  $R_2$ .

It can also be proven that the other zeros are still located high enough to be neglected, since  $|\omega_5|$  is much larger than  $2\pi\text{GBW}$ . Moreover, the geometric average of the frequency factor  $\omega_5$  and  $\omega_6$  is in fact little changed, which is given by

$$\begin{aligned} \sqrt{|\omega_5 \omega_6|} &\approx \sqrt{\frac{k_t - \frac{1}{A_{v2}} \frac{C_{m1}}{C_{m2}}}{k_t} \frac{g_{m2}}{C_2} \frac{g_{m3}}{g_{m1}} 2\pi\text{GBW}}{\approx \sqrt{\frac{g_{m2}}{C_2} \frac{g_{m3}}{g_{m1}} 2\pi\text{GBW}}}. \end{aligned} \quad (41)$$

The geometric average of the frequency factor  $\omega_5$  and  $\omega_6$  is definitely far above the unity-gain frequency, since  $g_{m3} > g_{m1}$  and  $g_{m2}/C_2 \gg 2\pi\text{GBW}$  can be readily satisfied.

Thus, it has been shown that the stability can still be well ensured in the case of a finite output resistance  $R_2$  of the second stage of the TCFC amplifier.

### F. Slew Rate

Like most multistage amplifiers, the overall slew rate of the TCFC amplifier is limited by the slowest stage in the amplifier.

For the second stage of the TCFC amplifier, the capacitance load is the lumped parasitic capacitance  $C_2$ , which is much smaller than the compensating capacitances  $C_{m1}$  and the load capacitance  $C_L$ . Therefore, the overall slew rate is determined by the first stage which needs to drive the capacitance  $C_{m1}$  or the last stage which has to drive the capacitances  $C_L$ ,  $C_{m1}$  and  $C_{m2}$ .

Since the load capacitance is much larger than the other capacitances, the overall slew rate of the TCFC amplifier can be simplified as in

$$\text{SR} = \min \left( \frac{I_1}{C_{m1}}, \frac{I_3}{C_L} \right) \quad (42)$$

where  $I_1$  and  $I_3$  represent the currents in the first stage and the last stage, respectively.

Because the load capacitance  $C_L$  is much larger than the outer Miller capacitance  $C_{m1}$ , the second term in (42) tends to be the main limitation of the overall slew rate especially for low-power applications. Nonetheless, this limitation can be overcome by addition of a feed-forward stage  $g_{mf}$  as shown in Fig. 2. In

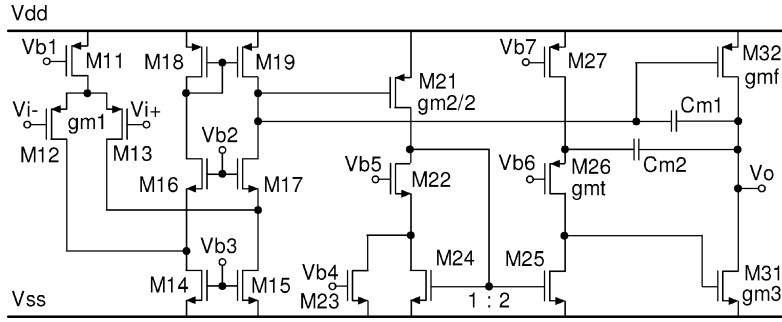


Fig. 3. Schematic of the TCFC amplifier.

TABLE I  
PARAMETERS OF THE TCFC AMPLIFIER

$g_{m1} = 24 \mu\text{S}$	$g_{m2} = 128 \mu\text{S}$	$g_{m3} = 128 \mu\text{S}$
	$g_{mt} = 64 \mu\text{S}$	$g_{mf} = 128 \mu\text{S}$
$C_{m1} = 1.1 \text{ pF}$	$C_{m2} = 0.92 \text{ pF}$	off-chip $C_L = 150 \text{ pF}$

TABLE II  
MEASURED RESULTS OF THE TCFC AMPLIFIER

$C_L$	150pF	$A_{dc}$	>100dB
GBW	2.85MHz	Phase Margin	58.6°
Power	0.045mW	Gain Margin	22dB
$V_{dd}$	1.5V	$I_{dd}$	0.03mA
SR $_{+/-}$	0.96/1.11 V/ $\mu\text{S}$	TS $_{+/-}$ (to 1%)	2.8/1.7 $\mu\text{S}$

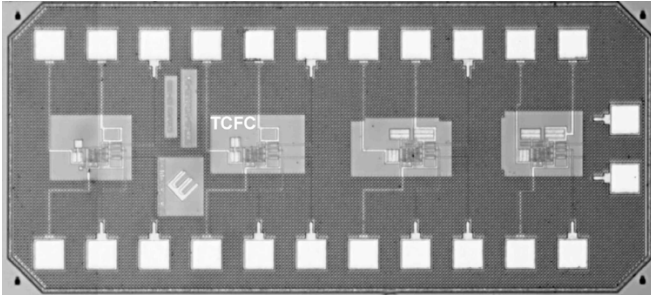


Fig. 4. Microphotograph of the implemented TCFC amplifier.

this case, the last stage forms a push-pull output stage which slews fast in both directions. Therefore, the first stage driving the Miller capacitance becomes the dominant limitation of the overall slew rate (SR), which can also be given and further derived as

$$\text{SR} = \frac{I_1}{C_m} \propto \frac{g_{m1}}{C_m} (V_{GS1} - V_{T1}) = 2\pi \text{GBW} (V_{GS1} - V_{T1}). \quad (43)$$

It can be seen that the overall slew rate is proportional to the gain-bandwidth product. As GBW is being improved, simultaneously the overall slew rate is being extended accordingly. It can thereby be concluded that for the TCFC amplifier with the feed-forward stage  $g_{mf}$ , increasing the gain-bandwidth product leads to a corresponding improvement of the slew rate.

## V. IMPLEMENTATION

The schematic of the implemented three-stage TCFC amplifier is shown in Fig. 3.

The first stage is a classical folded cascode OTA. It consists of transistors M11–M19, which ensure that the common mode input range can reach the lower rail voltage  $V_{ss}$ . The differential pair M11 and M12 generates the transconductance  $g_{m1}$ .

The transistor M21 provides half the second-stage transconductance  $g_{m2}$ , which is doubled by the transistor M25 via the current mirror composed by M24 and M25.

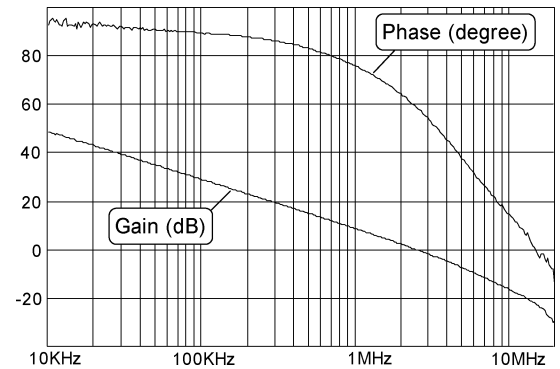
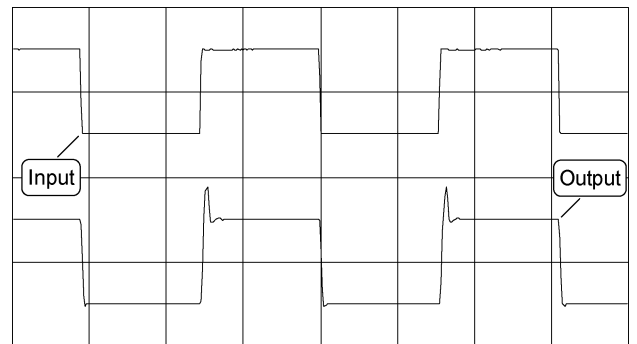


Fig. 5. Measured open-loop gain-frequency responses.

Fig. 6. Measured transient response (Xdiv: 10  $\mu\text{S}$ , Ydiv: 0.5 V).

The feedback transconductance  $g_{mt}$  is generated by the transistor M26, which also acts as a cascoding stage in the second stage. Obviously, with this configuration, the benefits are that the output resistance of the second stage shunted by  $r_{o25}$  is increased and the overall dc gain is boosted while no extra power is needed for implementing the feedback transconductance  $g_{mt}$ .

TABLE III  
 PERFORMANCE COMPARISON OF DIFFERENT AMPLIFIERS

		$A_{dc}$	$C_L$	$V_{dd}$	$I_{dd}$	Power	GBW	SR	FOM <sub>S</sub>	FOM <sub>L</sub>	IFOM <sub>S</sub>	IFOM <sub>L</sub>
		dB	pF	V	mA	mW	MHz	V/ $\mu$ S	$\frac{\text{MHz}\cdot\text{pF}}{\text{mW}}$	$\frac{\text{V}/\mu\text{S}\cdot\text{pF}}{\text{mW}}$	$\frac{\text{MHz}\cdot\text{pF}}{\text{mA}}$	$\frac{\text{V}/\mu\text{S}\cdot\text{pF}}{\text{mA}}$
NMC	[3]	100	100	8.0	9.50	76	60	20	79	26	632	211
MNMC	[3]	100	100	8.0	9.50	76	100	35	132	46	1053	368
NGCC	[4]	100	20	2.0	0.34	0.68	0.61	2.5	18	74	36	148
NCCF	[5]	90	12	2.5	5.6	14	250	-	214	-	535	-
NMCFNR	[6]	>100	100	2.0	0.20	0.406	1.8	0.79	443	195	886	390
ETC	[7]	102	40	3.0	2.30	6.90	47	69	272	400	817	1200
DFCFC	[8]	>100	100	2.0	0.21	0.42	2.6	1.32	619	314	1238	629
PFC	[9]	>100	130	1.5	0.19	0.275	2.7	1.0	1276	473	1915	709
AFFC	[10]	>100	120	2.0	0.20	0.40	4.5	1.49	1350	447	2700	894
DLPC	[11]	>100	120	1.5	0.22	0.33	7.0	3.3	2545	1200	3818	1800
ACBC <sub>F</sub>	[12]	>100	500	2.0	0.162	0.324	1.90	1.0	2932	1543	5864	3086
TCFC	this work	>100	150	1.5	0.03	0.045	2.85	1.035	9500	3450	14250	5175

In order to minimize the lumped parasitic capacitance  $C_2$ , the last-stage transconductance  $g_{m3}$  is realized with a nMOS transistor M31, while the transistor M32 acts as the feed-forward transconductance stage  $g_{mf}$ .

$C_{m1}$  is the Miller capacitor establishing the outer feedback loop.  $C_{m2}$  is the other feedback capacitor which along with the feedback transconductance  $g_{mt}$  accomplishing the internal feedback loop.  $C_L$  is an off-chip load capacitor.

The circuit parameters of the implemented TCFC amplifier are given in Table I.

The TCFC amplifier was fabricated in a 0.35- $\mu$ m CMOS process. A microphotograph of the implemented amplifiers is shown in Fig. 4. The active area for a TCFC amplifier is smaller than 0.02 mm<sup>2</sup>.

## VI. EXPERIMENTAL RESULTS

### A. Measured Results

The implemented TCFC amplifier was measured for both dc and ac specifications. The measured results, which are obtained using an HP3577A network analyzer and a Tektronix TDS680B oscilloscope, are summarized in Table II. The frequency characteristic and the transient response are shown in Figs. 5 and 6, respectively. It can be seen that a sufficient gain margin 22 dB is obtained due to the use of the specific compensation strategy.

### B. Performance Comparison

To quantitatively evaluate different amplifiers, usually two formulas are used as given by

$$\text{FOM}_S = \frac{\text{GBW} \cdot C_L}{\text{power}} \quad (44)$$

$$\text{FOM}_L = \frac{\text{SR} \cdot C_L}{\text{power}}. \quad (45)$$

However, as both the GBW and SR depend on the currents flow in the relevant transistors rather than the power itself, It is more reasonable to use two other formulas defined by

$$\text{IFOM}_S = \frac{\text{GBW} \cdot C_L}{I_{dd}} \quad (46)$$

$$\text{IFOM}_L = \frac{\text{SR} \cdot C_L}{I_{dd}}. \quad (47)$$

The comparison results of applying these formulas on the different amplifiers are given in Table III. Obviously, the TCFC amplifier shows the most outstanding performance.

## VII. CONCLUSION

A new frequency compensation topology, Transconductance with Capacitances Feedback Compensation topology for multistage amplifiers, has been presented and proven to be well suited for low-voltage low-power applications. It has been shown that by adequate application of negative feedback, the stability can be well ensured while the high-frequency behavior is not degraded. As demonstrated, the remarkable improvements for both small- and large-signal performance have been accomplished in an optimized low-power three-stage TCFC amplifier powered by low-voltage supplies.

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