

Analog Integrated Circuits Analysis and Design Midterm

Answer ver.1

1.

(a) A process of depositing films by reacting chemical vapors to produce a film on a substrate.

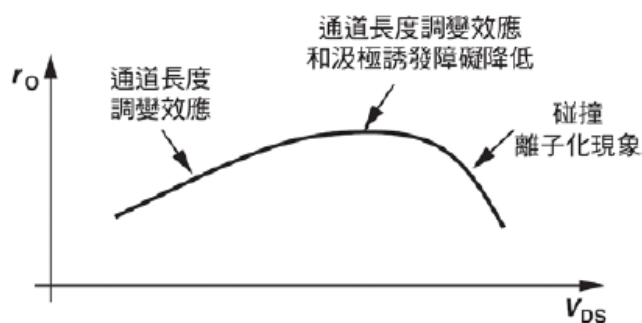
(b) DIBL: In short channel devices, the drain voltage makes the surface more positive by creating a two-dimensional field depletion region. The barrier to the flow charge and hence the V_{TH} are decreased.

(c) The number of transistors on a chip doubles every 18 months (12 months).

(d) High vertical electrical field E_{ver} between the gate and the channel confines the charge carriers to a narrow region below the oxide-silicon interface, leading to more scattering and hence lower mobility.

(e) Carriers may reach a saturated velocity $v = uE$ at some point along the channel. In the case carriers experience velocity saturation along the entire channel. The current is proportional to the V_{ov} only and does not depend on the length. Devices with $L < 1 \mu\text{m}$ reveal velocity saturation because equal increments in $V_{GS} - V_{TH}$ result in roughly equal increments in I_D . The transconductance is a weak function of the I_D and channel length.

2.

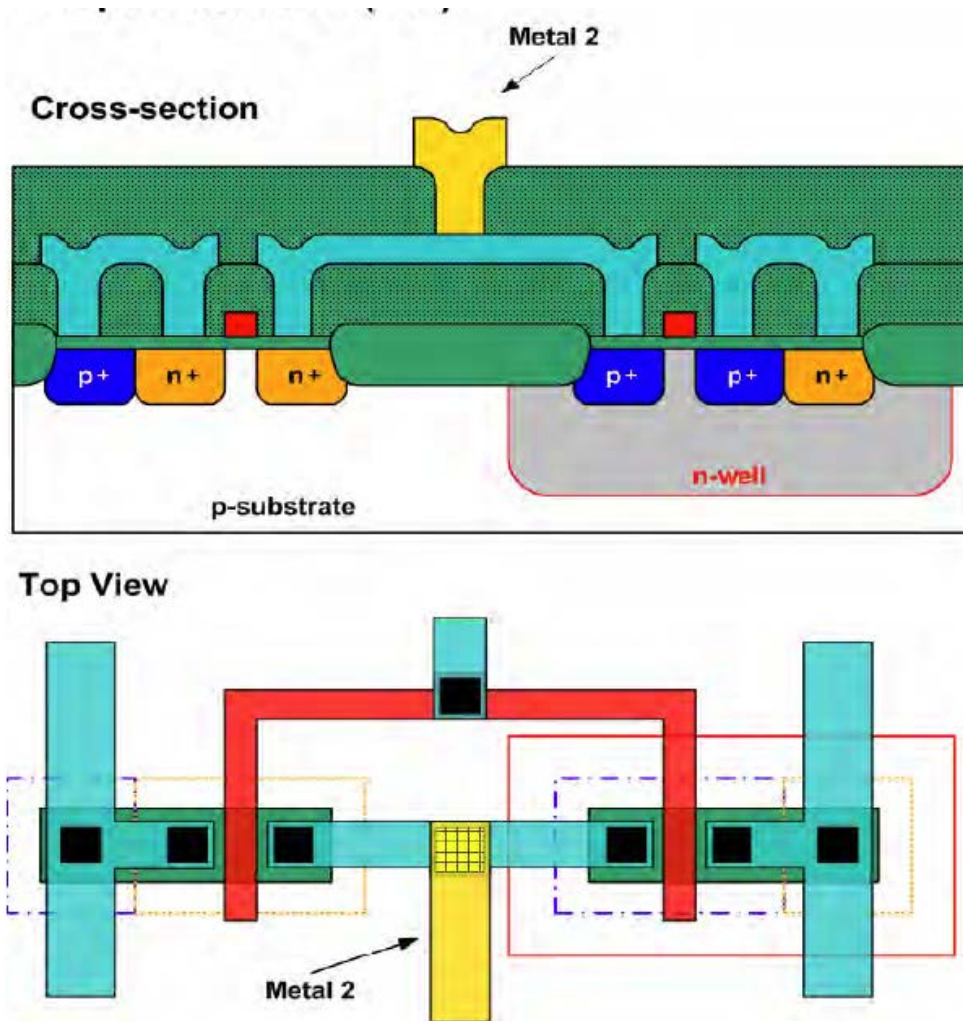


Region I: Channel length modulation --> r_{o1} 變大

Region II: Channel length modulation --> r_{o1} 變大 , DIBL --> r_{o1} 變小

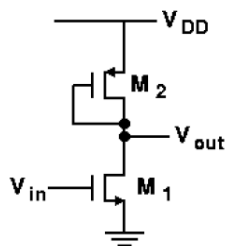
Region III: Impact ionization --> r_{o1} 變小

3.



(5% no partition)

4.

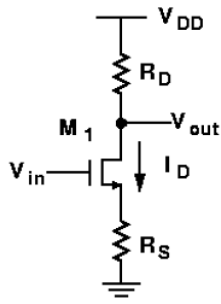


$$A_v \approx -g_{m1} \left(\frac{1}{g_{m2}} \parallel r_{o1} \parallel r_{o2} \right)$$

5.

$$A_v = -g_{m1} \times (r_{o1} // r_{o2})$$

6.



$$A_v = -G_m R_D = \frac{-g_m R_D}{1 + g_m R_S} = -\frac{R_D}{1/g_m + R_S}$$

7.

$$A_v = \frac{g_{m1} \times R_S}{1 + (g_{m1} + g_{mb1})R_S} = \frac{R_S // \frac{1}{g_{mb1}}}{\frac{1}{g_{m1}} + (R_S // \frac{1}{g_{mb1}})} = g_{m1} \times \left(\frac{1}{g_{m1}} // \frac{1}{g_{mb1}} // R_S \right)$$

8.

$$R_{out} = \{ [1 + (g_m + g_{mb})r_o]R_S + r_o \} // R_D$$

(5%)

9.

$$V_{gs}(V_{sg}) = |V_{ov}| + |V_{th}| = 0.9V$$

$$V_{b1} = |V_{ov1}| + V_{gs2} = 1.1V \quad (1.5\%)$$

$$V_{b2} = V_{DD} - |V_{ov4}| - V_{sg3} = 0.7V \quad (1.5\%)$$

$$|V_{ov1}| + |V_{ov2}| < V_{out} < V_{DD} - |V_{ov3}| - |V_{ov4}| \rightarrow 0.4V < V_{out} < 1.4V$$

$$\text{Max } V_{out} \text{ swing} = 1V \quad (2\%)$$

10.

(a)

$$-\sqrt{2 * 0.9} \leq V_{id} \leq \sqrt{2 * 0.9}$$

** or

$$-\sqrt{2} \leq V_{id} \leq \sqrt{2}$$

(b)

$$V_{CMmax} = V_t + V_{dd} - (I/2 * R_D) = 1.5$$

$$V_{CMmin} = V_{ov} + V_t + V_{ov} = 1.1$$

11.

(a)

$$\frac{V_{out1} - V_{out2}}{V_{in1} - V_{in2}} = A_{dm} = -g_m(R_D // r_o) = -10^{-3} \times 50 \times 10^3 = -50 \text{ V/V} \quad (2.5\%)$$

(b)

$$A_{cm} = -\frac{g_m R_D}{1 + 2g_m R_{SS}}$$

$$V_{out1} = -\frac{g_m R_{D1}}{1 + 2g_m r_o} V_{icm} \quad V_{out2} = -\frac{g_m R_{D2}}{1 + 2g_m r_o} V_{icm}$$

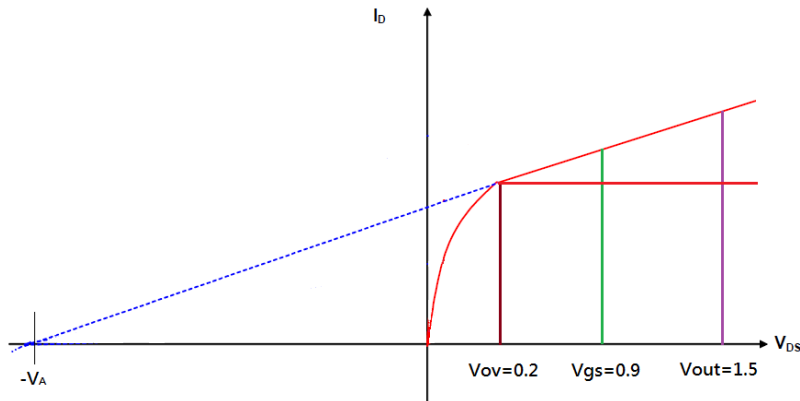
$$\begin{aligned} \frac{V_{out1} - V_{out2}}{V_{icm}} &= -\frac{g_m(R_{D1} - R_{D2})}{1 + 2g_m r_o} = -\frac{10^{-3} \times (110 - 100) \times 10^3}{1 + 2 \times 10^{-3} \times 100 \times 10^3} \\ &= -0.04975 \text{ V/V} \quad (2.5\%) \end{aligned}$$

12.

(a) In order to operate as a current mirror correctly, MOSFET have to work in saturation region.

Minimal $V_{out}=0.2\text{V}$

(b)



$$\begin{cases} I_{out} = Kn' \times 4 \times \left(\frac{W}{L}\right) \times (V_{GS} - V_{th})^2 \times \left(\frac{10 + 1.5}{10 + 0.2}\right) \\ I_{REF} = Kn' \times \left(\frac{W}{L}\right) \times (V_{GS} - V_{th})^2 \times \left(\frac{10 + 0.9}{10 + 0.2}\right) \end{cases}, I_{out} = 4 \times \left(\frac{10 + 1.5}{10 + 0.9}\right) \times I_{REF}$$

$$= 42.2\mu\text{A}$$

13.

(a) $V_b = 1.4V$. $V_{out,min} = V_b - V_{th} + V_{ov}$. $V_{out,min} = 1.4 - 0.7 + 0.2 = 0.9 V$.

(b) At matching, $V_{out} = V_X = 0.9V$. With early effect, $\Delta i_{out} = \Delta V_{out} / R_{out}$. $\Delta i_{out} = (1.5 - 0.9) / 1M = 0.6 \mu A$. $I_{out} = 40\mu A + 0.6\mu A = 40.6 \mu A$.

14.

(a) $V_{in,dc min} = V_{ov} + V_{GS} = 2V_{ov} + V_{th} = 0.4 + 0.7 = 1.1 V$

(b) $V_{out,max} = V_{DD} - V_{ov4} = 1.6V$. $V_{out,min} = V_{ov5} + V_{ov2} = 0.4V$ $V_{out,swing} = 1.6 - 0.4 = 1.2V$.

(c) $A_{id} = g_m(r_{o2} // r_{o4}) = 10^{-3} * 5k = 5 V/V$

(d) $A_{id} = 5 V/V$ $A_{cm} = 1/(1+2g_m r_o) = 1/20$ or $1/21 V/V$. $CMRR = |A_{id}/A_{cm}| = 100$ or $105 V/V$.

15.

(a)~(j) T F F T F F F F T F

16.

(a)~(j) F T F F T F T T F F