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Find the sinusoidal steady state  $v_o(t)$  for the following circuit by

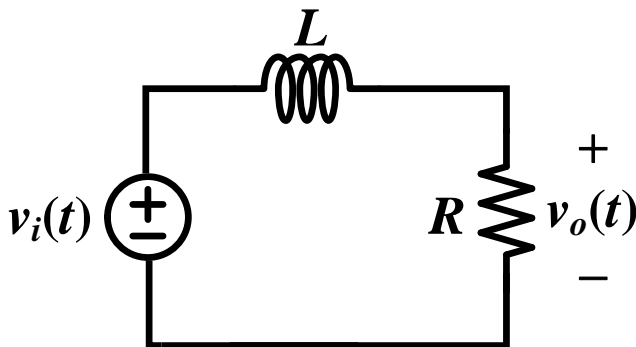
(a) find the transfer function  $\mathbf{H}(j\omega)$ .

(b) find the numerical complex value of the  $\mathbf{H}(j\omega)$  for  $\omega=4$  rad/s and  $\omega=4000$  rad/s.

(c) find  $v_o(t)$  for  $\omega=4$  rad/s and  $v_o(t)$   $\omega=4000$  rad/s.

(d) find  $v_o(t)$ .

(Assuming  $R=4\Omega$ ,  $L=1\text{H}$ , and  $v_i(t)=10\cos(4t)+10\cos(4000t)$  V.)



Solution:

(a)

$$\mathbf{H}(j\omega) = \frac{\mathbf{V}_o}{\mathbf{V}_i}(j\omega) = \frac{R}{R + j\omega L} = \frac{1}{1 + j\omega \frac{L}{R}}$$

(b)

$$\mathbf{H}(j\omega) = |\mathbf{H}| \angle \phi$$

$$|\mathbf{H}(j\omega)| = \frac{1}{\sqrt{1^2 + (\frac{\omega}{4})^2}} \quad \text{and} \quad \phi = \angle \mathbf{H}(j\omega) = -\tan^{-1}(\frac{\omega}{4})$$

$$|\mathbf{H}(j\omega)|_{\omega=4} = \frac{1}{\sqrt{1^2 + (\frac{4}{4})^2}} = \frac{1}{\sqrt{2}} \approx 0.707$$

$$|\mathbf{H}(j\omega)|_{\omega=4000} = \frac{1}{\sqrt{1^2 + (\frac{4000}{4})^2}} = \frac{1}{\sqrt{1000001}} \approx 0.001$$

$$\angle \mathbf{H}(j\omega)_{\omega=4} = -\tan^{-1}\left(\frac{4}{4}\right) = -45^\circ$$

$$\angle \mathbf{H}(j\omega)_{\omega=4000} = -\tan^{-1}\left(\frac{4000}{4}\right) = -89.94^\circ \approx -90^\circ$$

(c)

$$v_o(t)|_{\omega=4} = 5\sqrt{2} \cos(4t - 45^\circ) \text{ V}$$

$$v_o(t)|_{\omega=4000} = 0.01 \cos(4000t - 90^\circ) \text{ V}$$

(d)

$$\begin{aligned} v_o(t) &= v_o(t)|_{\omega=4} + v_o(t)|_{\omega=4000} \\ &= 5\sqrt{2} \cos(4t - 45^\circ) + 0.01 \cos(4000t - 90^\circ) \text{ V} \end{aligned}$$

(a)  $\mathbf{H}(j\omega) =$  \_\_\_\_\_,

(b)  $\mathbf{H}(j\omega) = |\mathbf{H}| \angle \phi$

where  $|\mathbf{H}|$  (at  $\omega = 4$  rad/s) = \_\_\_\_\_,

$|\mathbf{H}|$  (at  $\omega = 4000$  rad/s) = \_\_\_\_\_,

and  $\phi$  (at  $\omega = 4$  rad/s) = \_\_\_\_\_,

$\phi$  (at  $\omega = 4000$  rad/s) = \_\_\_\_\_,

(c)  $v_o(t)$  (for  $\omega = 4$  rad/s) = \_\_\_\_\_,

$v_o(t)$  (for  $\omega = 4000$  rad/s) = \_\_\_\_\_,

(d)  $v_o(t) =$  \_\_\_\_\_.