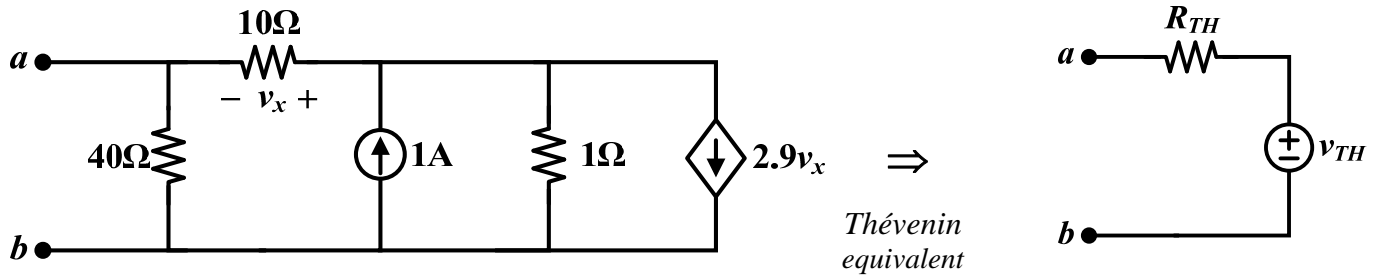


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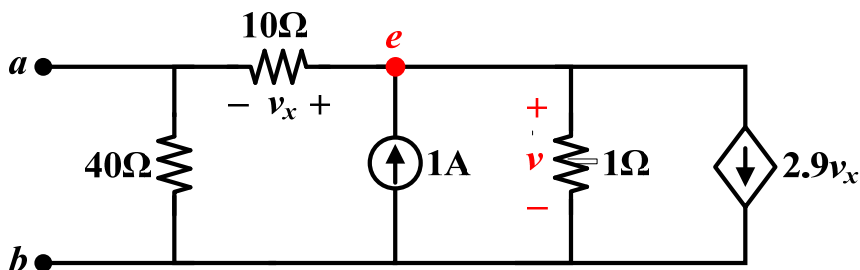
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Find the Thévenin equivalent parameters, v_{TH} and R_{TH} , for the port ab of the network shown in the following figure.



Solutions:

(1) Thévenin equivalent voltage v_{TH}



The open circuit voltage at port ab is the Thévenin equivalent voltage v_{TH} .

To find the Thévenin equivalent voltage v_{TH} , Let us first apply KCL at node e :

$$1 - \frac{v_x}{10} - \frac{v}{1} - 2.9v_x = 0$$

$$\Rightarrow 10v + 30v_x = 10 \dots (i)$$

Then, apply KCL at node a :

$$-\frac{v - v_x}{40} + \frac{v_x}{10} = 0$$

$$\Rightarrow v = 5v_x \dots (ii)$$

By solving (i) and (ii) simultaneously, v and v_x can be found.

$$\Rightarrow v_x = \frac{1}{8} \text{ V and } v = \frac{5}{8} \text{ V}$$

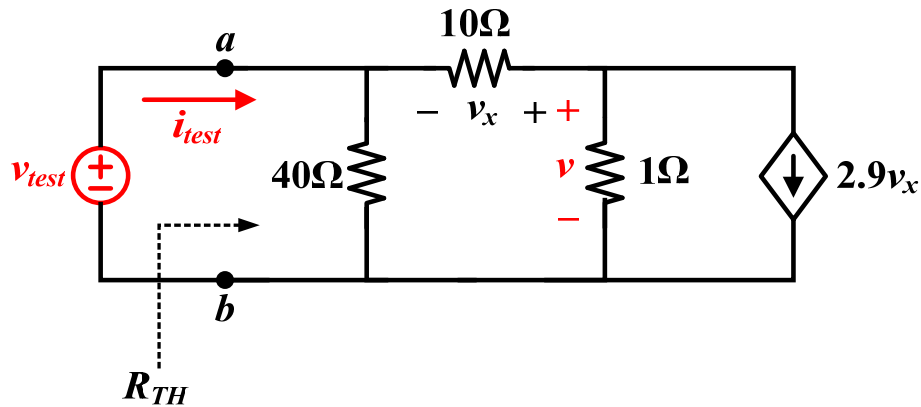
$$\therefore v_{TH} = v_{ab} = v - v_x = 0.5 \text{ V}$$

(2) Thévenin equivalent resistance R_{TH}

Let us set all independent sources inside the network to zero first.

Then we force current i_{test} into a . and find the voltage v_{test} across ab . The Thévenin equivalent resistance is

$$\text{simply } R_{TH} = \frac{v_{test}}{i_{test}}$$



$$R_{TH} = \frac{v_{test}}{i_{test}} = \frac{v - v_x}{\frac{v_{test}}{40} - \frac{v_x}{10}} = \frac{-40v_x}{\frac{-v_x}{10} - \frac{v_x}{10}} = \frac{40}{2} = 20\Omega$$

Note: The relation of v and v_x can be found by applying KCL to node e .

$$-\frac{v}{1} - \frac{v_x}{10} - 2.9v_x = 0$$

$$\Rightarrow v = \frac{-30}{10}v_x$$

$v_{TH} = \underline{\quad 0.5V \quad}, R_{TH} = \underline{\quad 20\Omega \quad}.$