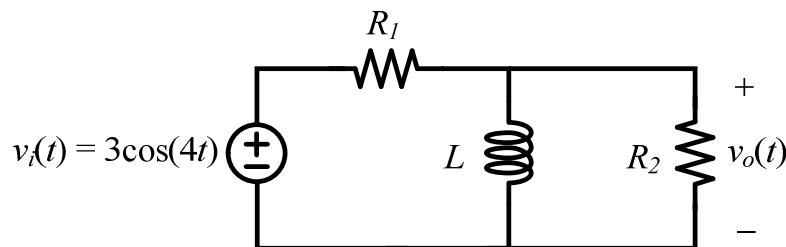


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Find the sinusoidal steady state  $v_o(t)$  for the following circuit by

- (1) convert the  $v_i(t)$  in time domain into the frequency domain  $\mathbf{V}_i$ ,
  - (2) find the transfer function  $\mathbf{H}(j\omega)$  in the frequency domain,
  - (3) find the numerical value of the  $\mathbf{H}(j\omega)$  by plugging the frequency  $\omega$  given in the figure,
  - (4) find the  $\mathbf{V}_o$  in the frequency domain from (1) and (3),
  - (5) convert the  $\mathbf{V}_o$  in the frequency domain into  $v_o(t)$  in time domain.
- (Assuming  $L = 10 \text{ H}$ ,  $R_1 = 120 \Omega$ , and  $R_2 = 60 \Omega$ .)



Solution:

(1)

$$v_i(t) = \operatorname{Re}\{\mathbf{V}_i e^{j\omega t}\}$$

$$\therefore \mathbf{V}_i = |\mathbf{V}_i| e^{j0} = 3\mathbf{V}$$

(2)

$$\mathbf{H}(j\omega) = |\mathbf{H}(j\omega)| e^{j\phi} = \frac{\mathbf{V}_o}{\mathbf{V}_i} = \frac{j\omega L \| R_2}{R_1 + (j\omega L \| R_2)} = \frac{j\omega L R_2}{R_1 R_2 + j\omega L (R_1 + R_2)} = \frac{j \frac{\omega L}{R_1}}{1 + j\omega L \left( \frac{R_1 + R_2}{R_1 R_2} \right)}$$

(3)

$$\mathbf{H}(j\omega) = |\mathbf{H}(j\omega)| e^{j\phi} = \frac{j \frac{\omega L}{R_1}}{1 + j\omega L \left( \frac{R_1 + R_2}{R_1 R_2} \right)}$$

$$|\mathbf{H}(j\omega)|_{\omega=4} = \frac{\frac{\omega L}{R_1}}{\sqrt{1^2 + \left[ \omega^2 L^2 \left( \frac{R_1 + R_2}{R_1 R_2} \right)^2 \right]}} = \frac{\frac{4 \times 10}{120}}{\sqrt{1 + \left( 16 \times 100 \times \frac{1}{1600} \right)}} = \frac{1}{3\sqrt{2}}$$

$$\phi = \frac{\pi}{2} - \tan^{-1} \left[ \frac{\omega L (R_1 + R_2)}{R_1 R_2} \right] = \frac{\pi}{2} - \tan^{-1}(1) = \frac{\pi}{2} - \frac{\pi}{4} = \frac{\pi}{4} \text{ rads}$$

(4)

$$\mathbf{V}_o = \mathbf{V}_i \times \mathbf{H}(j\omega) = 3e^{j0} \times \frac{1}{3\sqrt{2}} e^{j\frac{\pi}{4}} = \frac{1}{\sqrt{2}} e^{j\frac{\pi}{4}} (\mathbf{V})$$

(5)

$$v_o(t) = \operatorname{Re} \left\{ \mathbf{V}_o e^{j\omega t} \right\}_{\omega=4} = \operatorname{Re} \left\{ \frac{1}{\sqrt{2}} e^{j\frac{\pi}{4}} e^{j4t} \right\} = \operatorname{Re} \left\{ \frac{1}{\sqrt{2}} e^{j(4t + \frac{\pi}{4})} \right\} = \frac{1}{\sqrt{2}} \cos \left( 4t + \frac{\pi}{4} \right) (\mathbf{V})$$

(1)  $\mathbf{V}_i = \underline{\hspace{10cm}},$

(2)  $\mathbf{H}(j\omega) = \underline{\hspace{10cm}},$

(3)  $\mathbf{H}(j\omega) = |\mathbf{H}| \angle \phi$   
where  $|\mathbf{H}| = \underline{\hspace{10cm}}$ , and  $\phi = \underline{\hspace{10cm}},$

(4)  $\mathbf{V}_o = \underline{\hspace{10cm}},$

(5)  $v_o(t) = \underline{\hspace{10cm}}.$