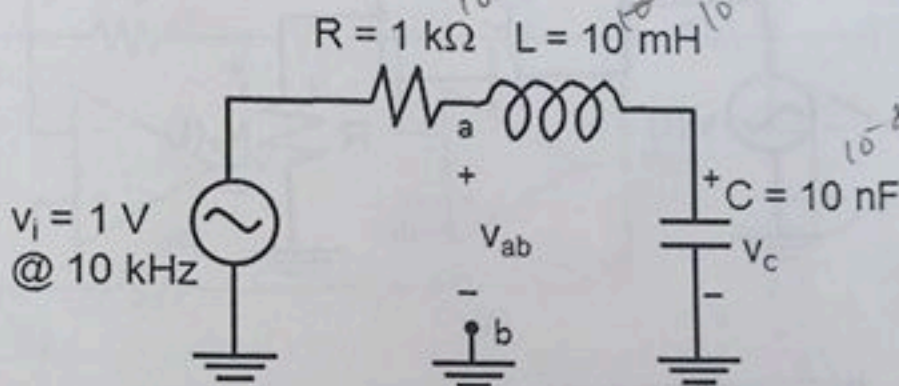


Date: January 14, 2014

1. AC response (10%)

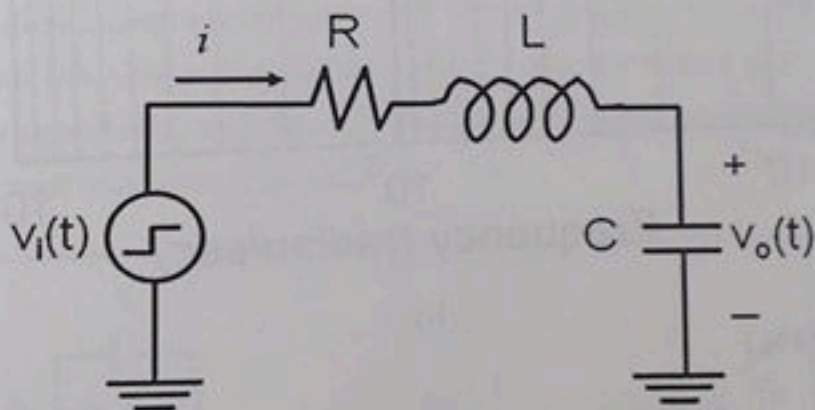
(a) (5%) For the RLC circuit as shown, the input v_i is a sinusoidal signal of 1 V (amplitude) at 10 kHz, please calculate the amplitude of v_{ab} at steady state.

(b) (5%) You are free to adjust the input frequency and observe the output v_c on the capacitor. Please calculate the frequency at which you will observe v_c lags v_i by 90° .



2. Time-domain responses (16%)

Consider the circuit as shown. Let $v_i(t)$ be a square-wave voltage with a minimum value at 0 V and a maximum value at 1 V.



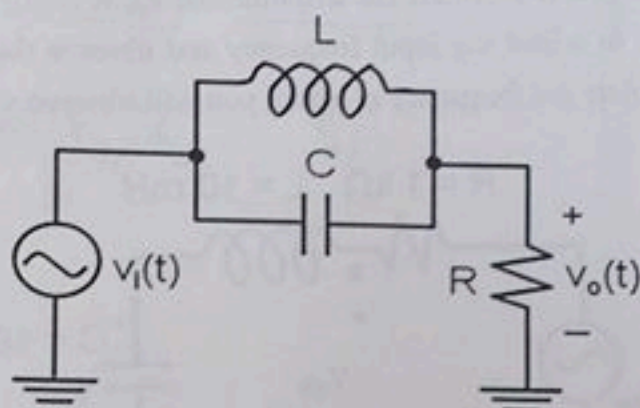
(a) (6%) Please derive the condition (in terms of R, L, C) for the corresponding response of $v_o(t)$ to be underdamped.

(b) (6%) Assume the circuit is underdamped, and the response of $v_o(t)$ exhibit overshoots. Which action(s) below would cause the maximum overshoot to increase? (i) Increase R (ii) Increase L (iii) Increase C (iv) Increase the frequency of $v_i(t)$. Please explain your answer clearly.

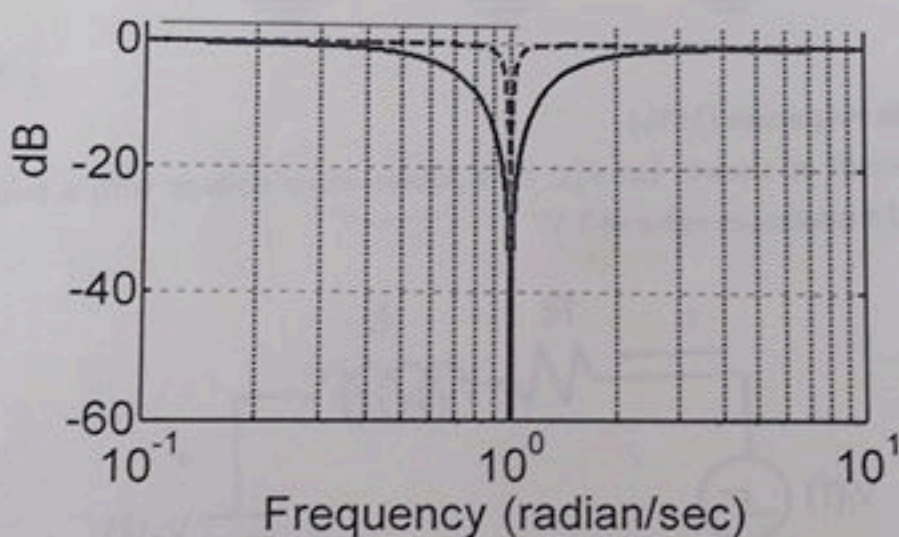
(c) (4%) If the square-wave voltage source exhibit a source resistance compatible to R, will the overshoot increase or decrease? Please explain your answer clearly.

3. Passive filters (8%)

Consider the band-reject filter in Fig.3a. Assume its frequency response is shown by the black solid curve in Fig.3b. If we would like to enhance the selectivity of the filter (i.e. modify the frequency response to be the one shown by the dashed curve in Fig.3b), should R be increased or decreased? Please explain your answer clearly.

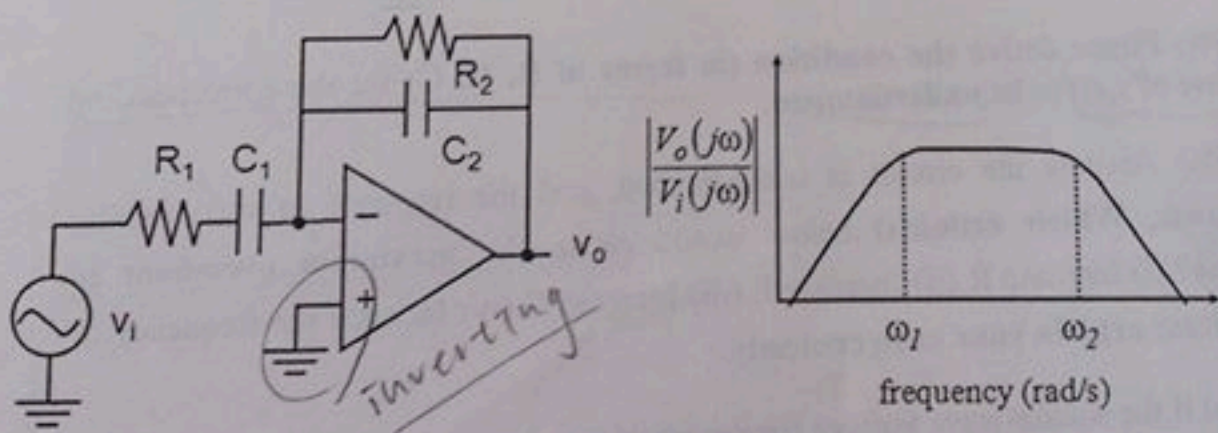


(a)



(b)

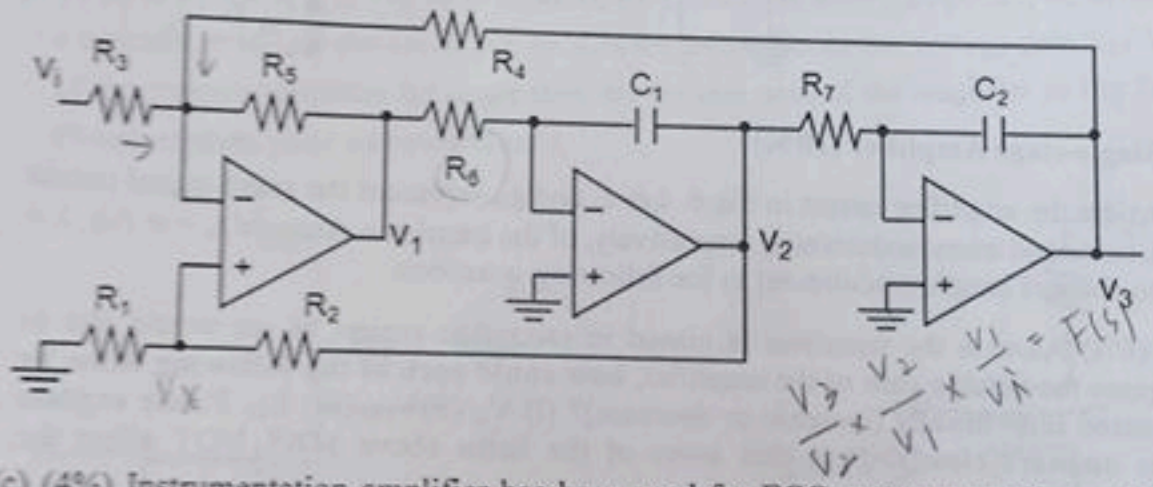
4. Active filter (20%)



(a) (8%) Please derive the transfer function $V_o(s)/V_i(s)$ of the filter as shown above.

$\frac{5C_1R_2}{(5C_1R_1+1)(1+5C_2R_2)}$

The frequency response on the right shows the corner (-3 dB) frequencies ω_1 and ω_2 . For $R_1C_1 > R_2C_2$, please determine ω_1 and ω_2 , respectively.
 (b) (8%) Schematic of the state-variable filter is shown below. Assume the transfer function of $V_3(s)/V_i(s)$ is $F(s)$. Please derive $V_1(s)/V_i(s)$ and $V_2(s)/V_i(s)$ using $F(s)$. Also, if $F(s)$ is known as a low-pass filter, please determine the filter types for $V_1(s)/V_i(s)$ and $V_2(s)/V_i(s)$, respectively (you have to explain and get both $V_1(s)/V_i(s)$ and $V_2(s)/V_i(s)$ correct to receive credits).

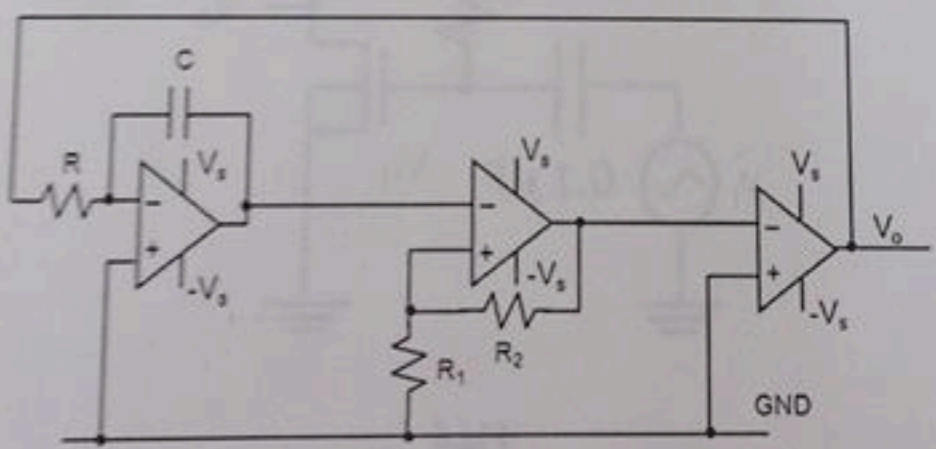


$\frac{V_3}{V_2} = \frac{V_2}{V_1} \times \frac{V_1}{V_i} = F(s)$

(c) (4%) Instrumentation amplifier has been used for ECG measurement in our lab. Please draw the schematic of an instrumentation amplifier with the output v_o related to the inputs (v_1 and v_2) by $v_o = v_1 - v_2$.

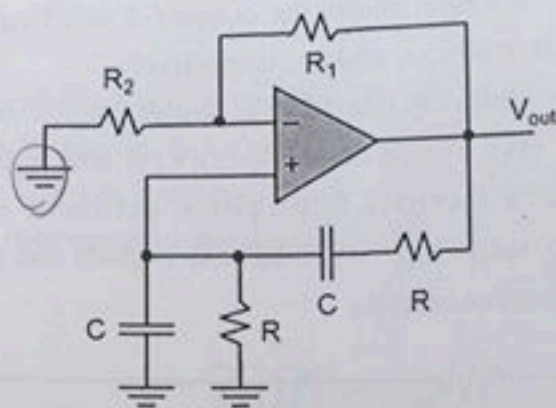
5. Oscillator (20%)

(a) (10%) The following shows the schematic of the triangular, square-wave oscillator circuit used in our lab. Given that all resistor and capacitor values in the circuit are $1 \text{ k}\Omega$ and $1 \mu\text{F}$, respectively, and the final output oscillates between $\pm 20 \text{ V}$, please determine the output oscillation frequency.



(b) (10%) Please derive the condition for the Wien-bridge oscillator (as shown below) to start oscillation and determine the corresponding oscillation frequency.

$\frac{R_1}{R_1 + R_2 + R_3}$
 $\frac{R_1}{R_1 + R_2 + R_3} > 3$
 $R_1 > 2R_2 + 2R_3$



$$\frac{R}{1+sRC} + \frac{1}{sC} + R$$

$$\frac{R \cdot R \cdot sC}{sC + R} = \frac{R}{1+sRC}$$

6. Single-stage Amplifier (10%)

Consider the amplifier circuit in Fig.6. Let r_o and g_m represent the small-signal output resistance and transconductance, respectively, of the transistor. Assume $r_o = \infty$ (i.e. $\lambda = 0$, no channel length modulation) in the following questions.

(a) (6%) Assume the transistor is biased in saturation region. If we would like to increase the voltage gain of the amplifier, how could each of the following items be adjusted individually (increase or decrease)? (i) V_G (ii) V_{DD} (iii) R_D . Please explain your answers clearly. Note that some of the items above MAY NOT affect the voltage gain.

(b) (4%) Assume we take one of the actions you propose in (a). The gain does increase in the beginning, but if we continue to adjust (increase or decrease) a certain item too much, the gain stops increasing and starts to decrease instead. Would you explain why the gain become decreasing?

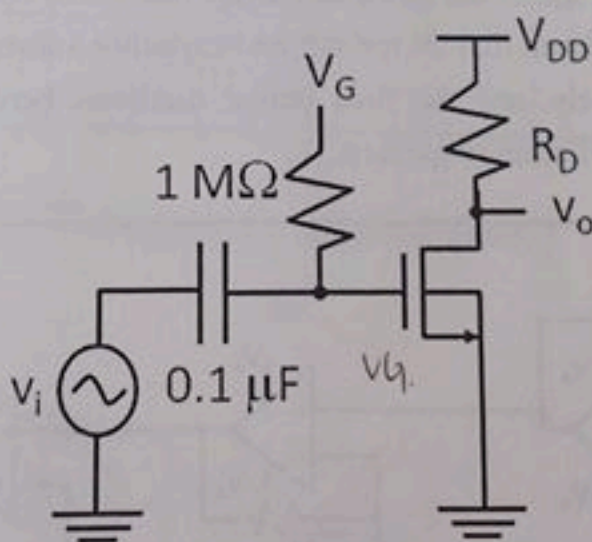


Fig.6

7. MOS Amplifiers (16%)

Consider the amplifier circuits in Fig.7. Let r_o and g_m represent the small-signal output resistance and transconductance, respectively, of **all** transistors. Assume r_o

\propto (i.e. $\lambda = 0$, no channel length modulation) in the following questions.

- (a) (6%) Assume $1/g_m \gg R_{sig}$ in Fig. 7a, please derive the expression for the voltage gain V_o/V_i ?
- (b) (6%) If we would like to increase the voltage gain of the amplifier, how could each of the following items be adjusted individually (increase or decrease)? (i) V_G (ii) V_{DD} (iii) R_L . Please explain your answers clearly. Note that some of the items above MAY NOT affect the voltage gain.
- (c) (4%) If V_i and R_{sig} in Fig. 7a is replaced by a common-source amplifier, we obtain a cascade amplifier shown in Fig. 7b. Let $R_L = R_D$. Would the voltage gain V_o/V_i of the cascade amplifier be larger than the voltage gain of the amplifier in Fig. 7a? Please explain your answers clearly.

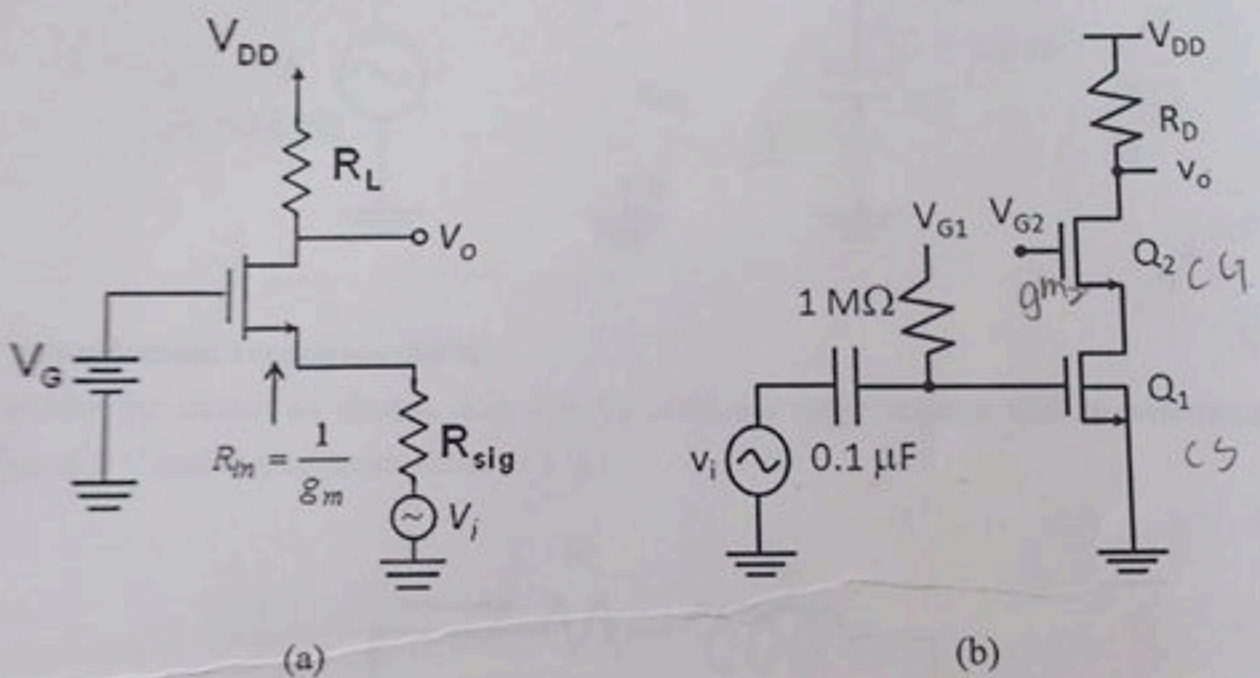
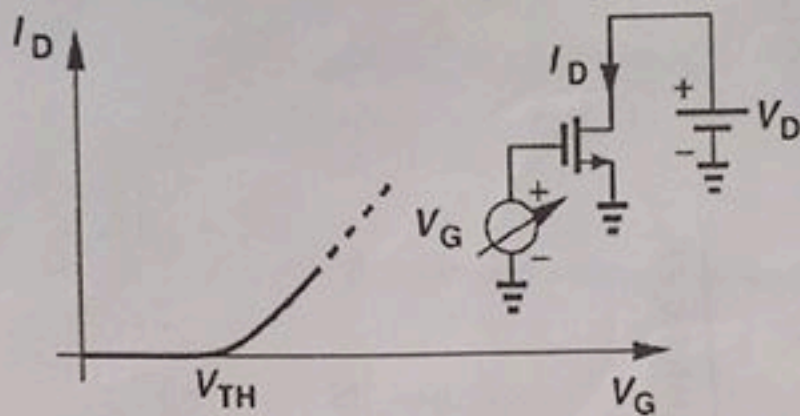


Fig.7

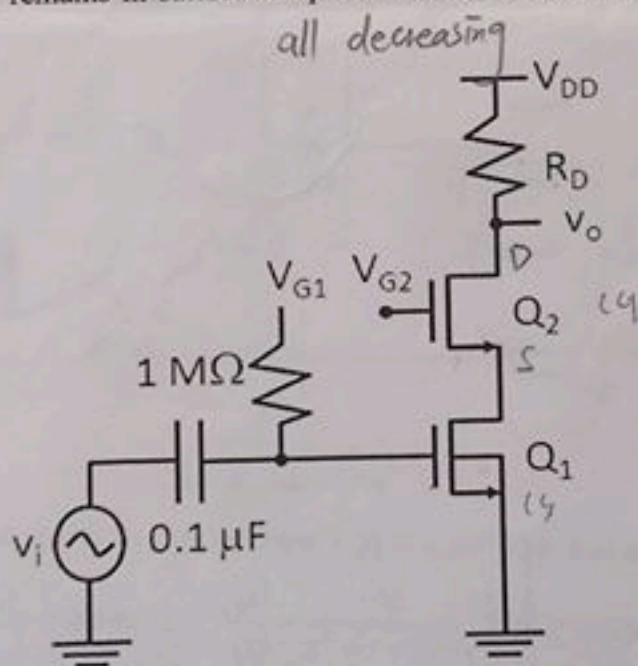


(b)

8. (16%) MOS Amplifier

Consider the MOS amplifier shown below.

- (1) (8%) Assume that the total output resistance at V_O approximates R_D . If we would like to increase the voltage gain V_o/V_i , how could each of the following items be adjusted individually? (increase or decrease?) (i) V_{G1} ; (ii) R_D . Assume that all transistors remain in saturation operation after the adjustment. Please explain your answer clearly. *both decreasing*
- (2) (8%) If we find that Q_2 operate in the triode (linear) region instead of the saturation region, how could each of the following items be adjusted individually (increase or decrease)? (i) V_{G1} ; (ii) V_{G2} ; (iii) R_D . Assume that Q_1 remains in saturation operation after the adjustment. Please explain your answer clearly. *all decreasing*



$$V_{DS} > V_{GS} - V_{th} > 0$$