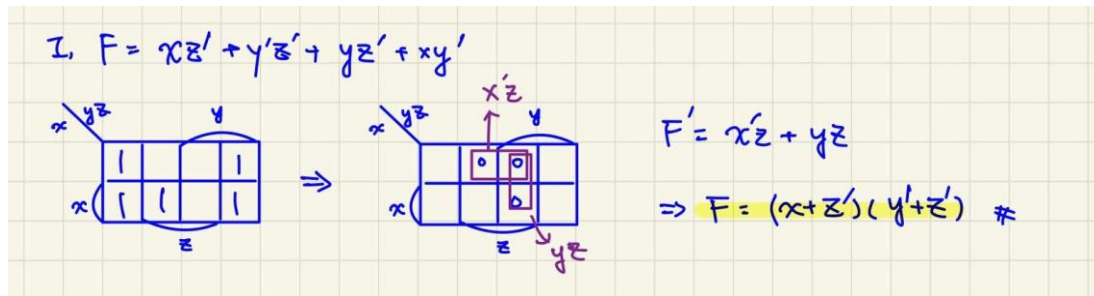


1. Simplify the Boolean expression $F(x, y, z) = xz' + y'z' + yz' + xy'$ to the form of product-of-sums. (15%)



2. Design a combinational circuit with unsigned four-bit binary input, $xyzw$ (MSB: x , LSB: w), and unsigned four-bit binary output, $ABCD$ (MSB: A , LSB: D). When the binary input is less than 0101, the binary output is 0011 greater than the input (for example, $xyzw:0010 \Rightarrow ABCD:0101$). When the binary input is greater than 1010, the binary output is 0101 less than the input (for example, $xyzw:1110 \Rightarrow ABCD:1001$). For other values of the binary input, the output equals the input.
- (a) Derive the truth table. (10%)
- (b) Derive the simplified Boolean expressions for A, B, C, D using maps. (16%)
- (c) Draw the related logic diagram using NAND and NOT gates only. (10%)

2,
(a)

| x | y | z | w | A | B | C | D |
|---|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| 0 | 0 | 0 | 1 | 0 | 1 | 0 | 0 |
| 0 | 0 | 1 | 0 | 0 | 1 | 0 | 1 |
| 0 | 0 | 1 | 1 | 0 | 1 | 1 | 0 |
| 0 | 1 | 0 | 0 | 0 | 1 | 1 | 1 |
| 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 0 | 0 | 1 | 1 | 0 |
| 0 | 1 | 1 | 1 | 1 | 0 | 1 | 1 |
| 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| 1 | 0 | 0 | 1 | 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 0 | 1 | 0 | 1 | 0 |
| 1 | 0 | 1 | 1 | 0 | 1 | 1 | 0 |
| 1 | 1 | 0 | 0 | 0 | 1 | 1 | 1 |
| 1 | 1 | 0 | 1 | 1 | 0 | 0 | 0 |
| 1 | 1 | 1 | 0 | 1 | 0 | 0 | 1 |
| 1 | 1 | 1 | 1 | 1 | 0 | 1 | 0 |

B:

| xy \ zw | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | 0 | 1 | 1 | 1 |
| 01 | 1 | 1 | 1 | 1 |
| 11 | 1 | 0 | 0 | 0 |
| 10 | 0 | 0 | 1 | 0 |

$$B = \bar{x}w + \bar{x}z + yz + yz\bar{w}$$

C:

| xy \ zw | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | 1 | 0 | 1 | 0 |
| 01 | 1 | 0 | 1 | 1 |
| 11 | 1 | 0 | 1 | 0 |
| 10 | 0 | 0 | 1 | 1 |

$$C = \bar{x}z\bar{w} + yz\bar{w} + \bar{x}yz + xz + yz + zw$$

D:

| xy \ zw | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | 1 | 0 | 0 | 1 |
| 01 | 1 | 1 | 1 | 0 |
| 11 | 1 | 0 | 0 | 1 |
| 10 | 0 | 1 | 0 | 0 |

$$D = \bar{x}z\bar{w} + \bar{x}y\bar{w} + \bar{x}yw + xz + yz + zw$$

(b)

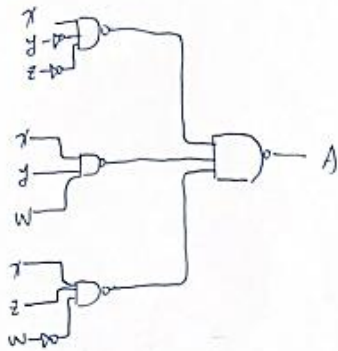
A:

| xy \ zw | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | 0 | 0 | 0 | 0 |
| 01 | 0 | 0 | 0 | 0 |
| 11 | 0 | 1 | 1 | 1 |
| 10 | 1 | 0 | 1 | 1 |

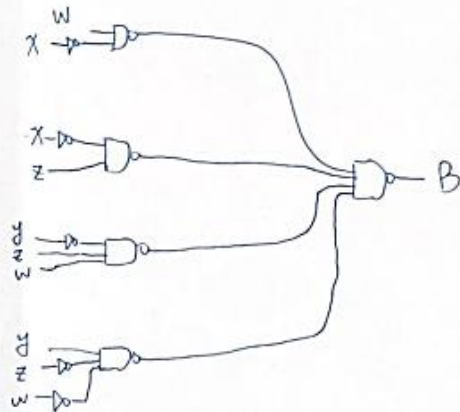
$$A = x\bar{y}\bar{z} + xyw + xz\bar{w}$$

(C)

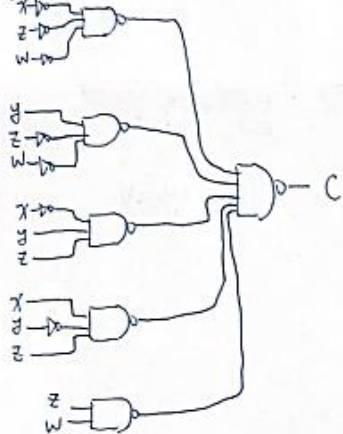
A:



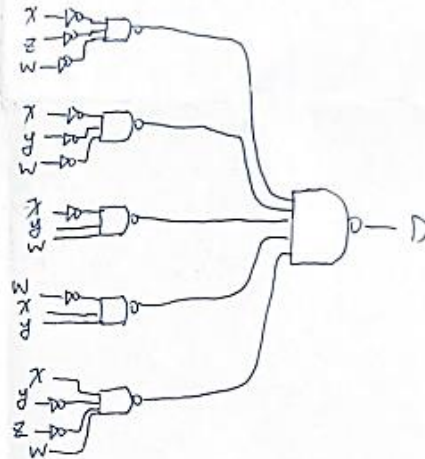
B:



C:



D:



3. Draw the OR-NAND implementation of the Boolean function, $F(x, y, z) = xz' + y'z' + yz' + xy'$. (15%)

$$F(x, y, z) = xz' + y'z' + yz' + xy'$$

| $x \backslash yz$ | 00 | 01 | 11 | 10 |
|-------------------|----|----|----|----|
| 0 | 1 | | | 1 |
| 1 | 1 | 1 | | 1 |

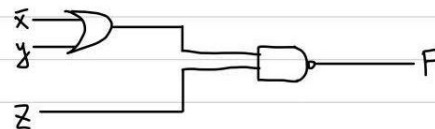
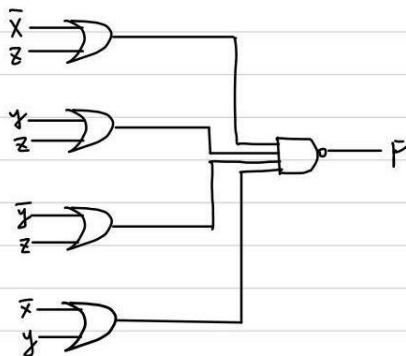
$$= \left((x' + z) \cdot (y + z) \cdot (y' + z) \cdot (x' + y) \right)'$$

$$\stackrel{\text{simplify}}{=} xy' + z'$$

$$= \left((x' + y) \cdot z \right)'$$

Original

simplified



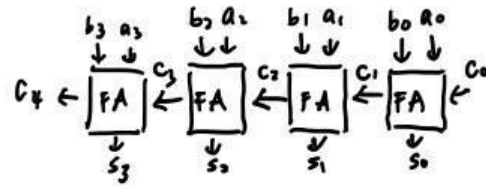
4. A full adder adds three binary inputs (a, b, c), and produce two outputs, sum (s) and carry (co).
- Derive the truth table of a full adder. (8%)
 - Derive the Boolean expressions of s and co in the simplest sum-of-products forms. (8%)
 - Find the prime implicants and essential prime implicants of the outputs s and co. (8%)

4.

(a.)

| a | b | c | S | Co |
|---|---|---|---|----|
| 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 | 0 |
| 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 | 1 |
| 1 | 0 | 0 | 1 | 0 |
| 1 | 0 | 1 | 0 | 1 |
| 1 | 1 | 0 | 0 | 1 |
| 1 | 1 | 1 | 1 | 1 |

(d.)



(b.1) S

| a \ bc | 00 | 01 | 11 | 10 |
|--------|----|----|----|----|
| 0 | 0 | 1 | 0 | 1 |
| 1 | 1 | 0 | 1 | 0 |

Co

| a \ bc | 00 | 01 | 11 | 10 |
|--------|----|----|----|----|
| 0 | 0 | 0 | 1 | 0 |
| 1 | 0 | 1 | 1 | 1 |

$$S = a \oplus b \oplus c$$

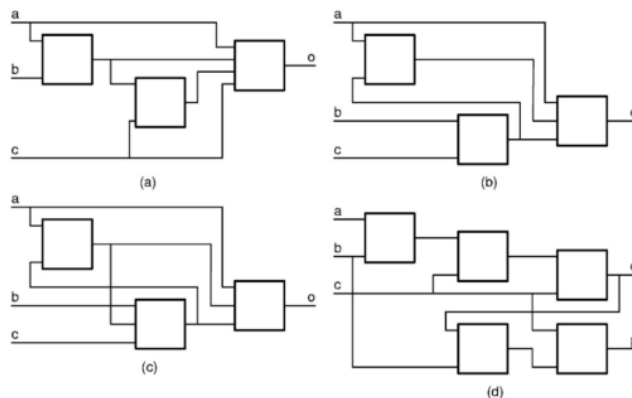
$$= ab'c' + a'b'c + abc + a'bc'$$

$$C_0 = ac + ab + bc$$

$$= ab + c(a \oplus b)$$

- (c.) $PI(S) = abc', a'b'c, abc, a'bc'$
 $EPI(S) = abc', a'b'c, abc, a'bc'$
 $PI(C_0) = ac, ab, bc$
 $EPI(C_0) = ac, ab, bc$

5. Which of the following circuits are combinational circuits? Each box is itself a combinational circuit. (10%)



Ans: (a) , (b) , (d) are combinational circuit.

(c) is sequential circuits. Because $d(t+1)$ is depend on present input b c and previous ouput $d(t)$.

