

## HW4-1

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1. (32%) Design a combinational circuit with unsigned four-bit binary input,  $xyzw$  (MSB: $x$ , LSB: $w$ ), and unsigned four-bit binary output,  $ABCD$  (MSB: $A$ , LSB: $D$ ). When the binary input is less than 0101, the binary output is 0011 greater than the input (for example,  $xyzw:0010 \Rightarrow ABCD:0101$ ). When the binary input is greater than 1010, the binary output is 0101 less than the input (for example,  $xyzw:1110 \Rightarrow ABCD:1001$ ). For other values of the binary input, the output equals the input.
  - (a) Derive the truth table. (8%)
  - (b) Derive the simplified Boolean expressions for  $A$ ,  $B$ ,  $C$ ,  $D$  using maps. (16%)
  - (c) Draw the related logic diagram. (8%)
2. (18%) Design a four-bit 2's complementer with simplified Boolean function and logic diagram. (The output generates the 2's complement of the input binary number.)
3. (10%) Design a 3x4 unsigned binary multiplier.