

1. 林彥岑

1. 1 byte = 8 bits  
 1 K =  $2^{10} = 1024$   
 1 G =  $2^{30} = 1024^3 = 1073741824$

(a) 64 K bytes =  $64 \cdot 1024 \cdot 8$  bits  
 = 524288 bits \*

(b) 1.5 G bytes =  $1.5 \cdot 1024^3 \cdot 8$  bits  
 = 12884901888 bits \*

2. 呂政和

2. (36%) Convert the following numbers (all unsigned) from the given base to other three bases listed in the table (to the 4<sup>th</sup> digit after radix point):

Decimal	Binary	Octal	Hexadecimal
53.217	? (1)	? (2)	? (3)
? (4)	1011.1101	? (5)	? (6)
? (7)	? (8)	48.37	? (9)
? (10)	? (11)	? (12)	D9.1A

(1) Decimal 53.217 → Binary 110101.0011

整數：除2取余

53<sub>(10)</sub> → 110101

$$\begin{array}{r} 2 \overline{) 53} \\ \underline{26} \quad \dots 1 \\ 2 \overline{) 27} \quad \dots 0 \\ \underline{16} \quad \dots 1 \\ 2 \overline{) 11} \quad \dots 0 \\ \underline{1} \quad \dots 1 \end{array}$$

小數：乘2取整

0.217<sub>(10)</sub> → 0.00110... ≈ 0.0011

$(0.217 - 0) \times 2 = 0.434 \dots 0$

$(0.434 - 0) \times 2 = 0.868 \dots 0$

$(0.868 - 0) \times 2 = 1.736 \dots 1$

$(1.736 - 1) \times 2 = 1.472 \dots 1$

$(1.472 - 1) \times 2 = 0.944 \dots 0$

∴ 53.217 = 110101.0011

(2)

$$(110101)_2 = (65)_8$$

$$0.217 \times 8 = 1.736 \dots 1 \Rightarrow (53.217)_{10} = (65.157)_8$$

$$(1.736 - 1) \times 8 = 5.888 \dots 5$$

$$(5.888 - 5) \times 8 = 7.104 \dots 7$$

$$(7.104 - 7) \times 8 = 0.832 \dots 0$$

(3)

$$(110101)_2 = (35)_{16}$$

$$0.217 \times 16 = 3.472 \dots 3 \Rightarrow (53.217)_{10} = (35.378d)_{16}$$

$$(3.472 - 3) \times 16 = 7.552 \dots 7$$

$$(7.552 - 7) \times 16 = 8.832 \dots 8$$

$$(8.832 - 8) \times 16 = 13.312 \dots d$$

(4) Binary  $(011.1101)_2 \rightarrow$  Decimal  $11.8125_{(10)}$

$$1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 + 1 \times 2^{-1} + 1 \times 2^{-2} + 0 \times 2^{-3} + 1 \times 2^{-4} \\ = 11.8125$$

(5) Binary  $1011.1101_2 \rightarrow$  Octal  $13.64_{(8)}$

$$\begin{array}{cccc} \underline{001} & \underline{011} & . & \underline{110} & \underline{100} \\ 1 & 3 & . & 6 & 4 \end{array}$$

(6) Binary  $1011.1101_2 \rightarrow$  Hex  $b.d_{(16)}$

$$\begin{array}{ccc} \underline{1011} & . & \underline{1101} \\ b & . & d \end{array}$$

(8) Octal  $48.37 \rightarrow$  Binary

因為在 8 進制，數到 8 要進位，因此沒有答案。

(7) (9) 同理，無解

(1) Hex  $D9.1A_{16} \rightarrow$  Binary  $11011001.0001010$

$\underline{D} \underline{9} . \underline{1} \underline{A}$   
 $11011001.0001010$

$$\begin{aligned} (10) (D9.1A)_{16} &= 13 \times 16^1 + 9 \times 16^0 + 1 \times 16^{-1} + 10 \times 16^{-2} \\ &= (217.1015625)_{10} \\ &= (217.1015)_{10} \end{aligned}$$

(12)

$$(11011001)_2 = (331)_8$$

$$\begin{aligned} 0.1015625 \times 8 &= 0.8125 \dots \boxed{D} \\ (0.8125 - 0) \times 8 &= 6.5 \dots \boxed{6} \\ (6.5 - 6) \times 8 &= 4 \dots \boxed{4} \end{aligned} \Rightarrow (D9.1A)_{16} = (331.064)_8$$

### 3. 陳謙謙

紅色為補位(sign bit)，綠色為補位(防止overflow)，藍色為進位

(1)

$$+37: 100101 \rightarrow 0100101$$

$$+62: 111110 \rightarrow 0111110$$

(2)

$$+37: 100101 \rightarrow 0100101$$

$$-62: (+62) = 0111110 \rightarrow 2' \text{ s complement: } 1000001+1 = 1000010$$

$$-37: (+37) = 0100101 \rightarrow 2' \text{ s complement: } 1011010+1 = 1011011$$

$$(+37)+(-62) \rightarrow 0100101 + 1000010$$

$$\begin{array}{r} 00100101 \\ + 11000010 \\ \hline 11100111 \end{array}$$

$$11100111 \rightarrow 2' \text{ s complement: } 00011000 + 1 = 00011001 = (+25) \Rightarrow 11100111 \text{ 為 } (-25) \text{ 的表示式}$$

$(-37)+(-62) \rightarrow 1011011 + 1000010$

$$\begin{array}{r} 1 \quad 1 \\ 1011011 \\ + 1000010 \\ \hline 10011101 \end{array}$$

$10011101 \rightarrow 2^7$ 's complement:  $01100010 + 1 = 01100011 = (+99) \Rightarrow 10011101$  為  $(-99)$  的表示式

4. 徐浩庭

4. 紅色為補位

(a)

$$\begin{array}{r} \overset{1}{0} \overset{1}{0} \quad \overset{1}{1} \overset{1}{0} \quad \overset{1}{1} \overset{1}{1} \overset{1}{0} \\ + \quad \overset{1}{1} \quad \overset{1}{0} \overset{1}{1} \overset{1}{1} \overset{1}{1} \\ \hline 00 \quad 00 \overset{1}{0} \overset{1}{1} \end{array}$$

藍色為進位

(b)

$$\begin{array}{r} \overset{1}{0} \overset{1}{0} \quad \overset{1}{0} \overset{1}{0} \overset{1}{1} \overset{1}{0} \overset{1}{1} \\ + \quad \overset{1}{1} \quad \overset{1}{0} \overset{1}{0} \overset{1}{0} \overset{1}{1} \overset{1}{0} \\ \hline 11 \quad 10 \overset{1}{0} \overset{1}{0} \overset{1}{0} \overset{1}{1} \end{array}$$

5. 吳東霖

By looking up the corresponding characters in ASCII table,  
 we can find out that  $N=78$ ,  $T=84$ ,  $H=72$ ,  $U=85$ ,  
 $E=69$ ,  $C=67$ ,  $S=83$  (all in decimal).

Then convert everything into binary

$\Rightarrow N=1001110$ ,  $T=1010100$ ,  $H=1001000$ ,  $U=1010101$

$E=1000101$ ,  $C=1000011$ ,  $S=1010011$

Check whether the number of '1' in each character is an even number.

If so, add '0' to MSB, otherwise add '1'.

$\Rightarrow$   $\begin{matrix} N & T & H & U \\ 01001110 & 11010100 & 01001000 & 01010101 \\ E & C & S \\ 11000101 & 11000011 & 11000011 & 01010011 \end{matrix}$

6.林致佑

## Binary Codes for Decimal Numbers

Decimal Digit	BCD 8421	2421	Excess-3	8, 4, -2, -1
0	0000	0000	0011	0000
1	0001	0001	0100	0111
2	0010	0010	0101	0110
3	0011	0011	0110	0101
4	0100	0100	0111	0100
5	0101	1011	1000	1011
6	0110	1100	1001	1010
7	0111	1101	1010	1001
8	1000	1110	1011	1000
9	1001	1111	1100	1111
	1010	0101	0000	0001
Unused bit combinations	1011	0110	0001	0010
	1100	0111	0010	0011
	1101	1000	1101	1100
	1110	1001	1110	1101
	1111	1010	1111	1110

a.  $(\underline{1001} \ \underline{0101})_{\text{BCD}} = (95)_{10}$

b.  $(\underline{1001} \ \underline{0101})_{\text{Excess-3}} = (62)_{10}$

c. 8-bit unsigned number

$$\Rightarrow (2^7 + 2^4 + 2^2 + 2^0)_{10} = (149)_{10}$$

d. 8-bit signed number

$$\Rightarrow (-2^7 + 2^4 + 2^2 + 2^0)_{10} = -(109)_{10}$$

7. (吕依凡)

$$\lceil \log_2 35 \rceil = 6$$

$$2^5 = 32 < 35 < 2^6 = 64$$

$\rightarrow$  we need at least 6 bits.

8. (吕依凡)

For 12 codes

We need 12 codes

$\rightarrow$  we need at least  $\lceil \log_2 12 \rceil = 4$  bits.

$\rightarrow$  MSB of the first  $\frac{12}{2} = 6$  codes are 0, and that of the others are 1.

<b>original code</b> $\{d_3d_2d_1d_0\}$	<b>gray code</b> $\{g_3\}$
0000	0
0001	0
0010	0
0011	0
0100	0
0101	0
0110	1
0111	1
1000	1
1001	1
1010	1
1011	1

$$g_x = \begin{cases} 0, & \text{when } d_{x+1} \text{ and } d_x \text{ contain even number of 1s} \\ 1, & \text{when } d_{x+1} \text{ and } d_x \text{ contain odd number of 1s} \end{cases}$$

*, where  $x = \{2, 1, 0\}$*

Then we have,

original code{ $d_3d_2d_1d_0$ }	gray code{ $g_3g_2g_1g_0$ }
0000	0000
0001	0001
0010	0011
0011	0010
0100	0110
0101	0111
0110	1111
0111	1110
1000	1010
1001	1011
1010	1001
1011	1000

For 10 codes:

We need 10 codes

→ we need at least  $\lceil \log_2 10 \rceil = 4 \text{ bits}$ .

→ MSB of the first  $\frac{10}{2} = 5$  codes are 0, and that of the others are 1.

original code{ $d_3d_2d_1d_0$ }	gray code{ $g_3$ }
0000	0
0001	0
0010	0
0011	0
0100	0
0101	1
0110	1
0111	1
1000	1
1001	1

$$g_x = \begin{cases} 0, & \text{when } d_{x+1} \text{ and } d_x \text{ contain even number of 1s} \\ 1, & \text{when } d_{x+1} \text{ and } d_x \text{ contain odd number of 1s} \end{cases}$$

, where  $x = \{2, 1, 0\}$

Then we have,

original code{ $d_3d_2d_1d_0$ }	gray code{ $g_3g_2g_1g_0$ }
0000	0000
0001	0001
0010	0011
0011	0010
0100	0110
0101	1110
0110	1010
0111	1011
1000	1001
1001	1000