

## HW2

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1. Convert F to the other normal form and standard forms of sum of products and product of sums. (10%)  

$$F(w, x, y, z) = \sum (0,1,4,5,7,11,13,14,15)$$
2. Simplify the following Boolean expressions (do not use K-map) to a minimum number of literals. After simplification, draw the logic diagrams of the circuits that implement the original and simplified expressions, respectively. (10%)
  - (a)  $x'y'z' + x'y'z + x'yz + xy'z' + xy'z$ ,
  - (b)  $(w+x)(w'+y+x')$ .
3. Find the complement of  $F(w,x,y,z) = w'x'y + w'y' + x'yz + w'x'y$ ; then show that  $FF' = 0$  and  $F + F' = 1$ . (10%)
4. Use DeMorgan's theorem to remove the complement outside the braces. (12%)
  - (a)  $((x+w)') + w'y'z + (x+z)'(x+y)'$ ,
  - (b)  $(x(yz' + y'z)') + wy(y' + x'z)'$ ,
  - (c)  $(x+y)' + z'(x'+z)'$ ,
  - (d)  $(xy' + z)'(w + y'z)$ .
5. Implement the function  $F = x' + x(x+y')(y+z')$  using (15%)
  - (a) AND, OR, and inverter gates,
  - (b) AND and inverter gates,
  - (c) OR and inverter gates.
6. For the function  $F(w, x, y, z) = \prod (2,5,6,7,8,9,10,11,14)$ 
  - (a) Obtain its truth table, (3%)
  - (b) Express F in sum-of-minterms and product-of-maxterms forms, (6%)
  - (c) Draw the logic diagram of F, (5%)
  - (d) Use Boolean algebra to simplify the function F to a new function G, with minimum number of literals, (5%)
  - (e) Obtain the truth table of G and compare it with that of F, (5%)
  - (f) Draw the logic diagram of G and compare the number of literals of F and G. (5%)
7. For the Gray code with 4 code numbers ( $g_3g_2g_1g_0$ ), use a 4-bit binary code ( $b_3b_2b_1b_0$ ) as inputs
  - (a) Derive the related truth table, (6%)
  - (b) Find the logic functions for each  $g_i$ . (8%)
8. Feedback: your feedbacks are very valuable that I will adjust the class and the assignments accordingly. Any comments to the class so far?