

## HW2

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1. Simplify the following Boolean expressions (do not use K-map) to a minimum number of literals. After simplification, draw the logic diagrams of the circuits that implement the original and simplified expressions, respectively.
  - (a)  $x'y'z+xy'z+xyz+x'yz,$
  - (b)  $(y'z+xw')(xw+y'z).$
2. Find the complement of  $F=(x+y'+z')(y+z)(x'+z)$ ; then show that  $FF'=0$  and  $F+F'=1$ .
3. Use DeMorgan's theorem to remove the complement outside the braces:
  - (a)  $((x+w')y+wy'z+xz(x+y))',$
  - (b)  $((x(y+z)+y'z(x+w))',$
  - (c)  $(x(y'+y(z+w))',$
  - (d)  $(xy+y(x+z))'.$
4. We can perform logical operations on strings of bits by considering each pair of corresponding bits separately (called *bitwise* operation). Given two eight-bit strings  $A=11000101$  and  $B=01010101$ , evaluate the eight-bit result after the following logical operations:
  - (a) AND,
  - (b) XNOR,
  - (c) NOT A.
5. List the truth table of the function  $F=x'y+xy'+yz'$ , and implement the function
  - (a) with AND, OR, and inverter gates,
  - (b) with AND and inverter gates,
  - (c) with OR and inverter gates.
6. Obtain the truth table of function  $F=x'yz'+w'y+wyz'$  and express it in sum-of-minterms and product-of-maxterms forms.
7. For the Boolean function  $F=x'y'z+xy'z+xyz+x'yz,$ 
  - (a) Obtain the truth table of F.
  - (b) Draw the logic diagram for F.
  - (c) Use Boolean algebra to simplify the function F to a new function, G, with minimum number of literals.
  - (d) Obtain the truth table of G and show it is the same as that of F.
  - (e) Draw the logic diagram for G and compare the number of literals and gates with those of F.

8. Convert  $F$  to the other normal form and standard forms of sum of products and product of sums.

$$F(A, B, C, D) = \sum (0, 1, 3, 5, 7, 9, 13, 14, 15)$$

-. " : YXVUW. i nci f ZYXVUWgUFYj Yfmj Ui UVYh Uh=k ]`UXi ghYdUWcZh YWUggUbX`cUXcZ hYUgg[ ba YblgUWfX]b[ `m'5bmWa a Yblg'lc h YWUggYggc ZF3