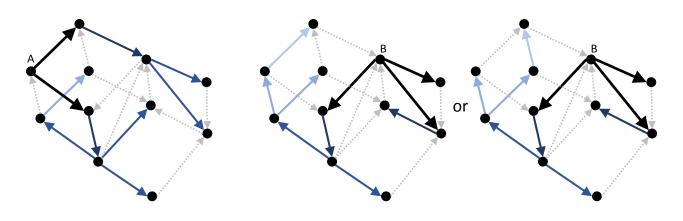
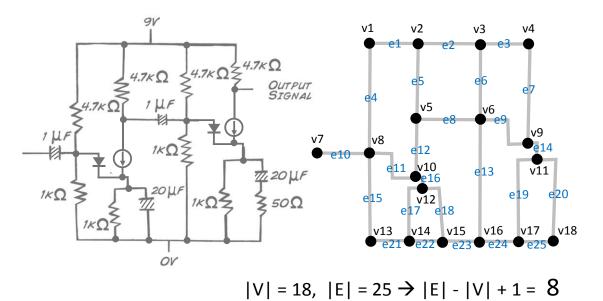
國立清華大學電機系 106 學年度下學期 (2017 Spring) NTHU EE 10520EE241000 Data Structures Final Exam 3:30pm-5:20pm (110 minutes), June. 12, 2017

#:	Student ID:	Name:

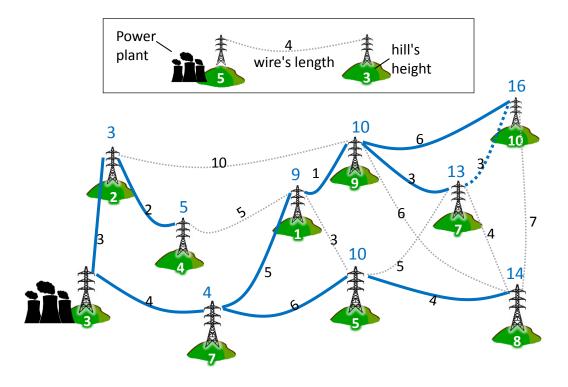
- ♦ Read each question carefully before you start answering it. 看清題目再作答。
- ♦ You can use both ballpoint pens and pencils.
- If there are more than one answers for a problem, just answer one of them. If there is any question on the problems, ask or use reasonable assumptions to solve the problems.
- ♦ There are 12 problems, each being 10 points. You can obtain up to 120 points.
- 1. Please use solid lines to display the breadth-first search (**BFS**) trees starting from vertices A and B, respectively.



How many independent cycles are there in the following circuit? Hint: view the circuit as a graph.

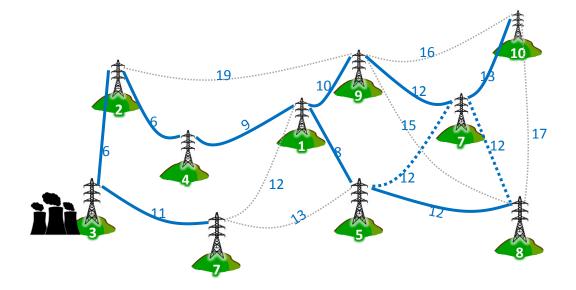


- 3. The Power Company wants to build a power distribution tree spanning several hills.
 - If we want every path from the power plant to every hill to be as short as possible, please use thick solid lines to depict what the company should do.

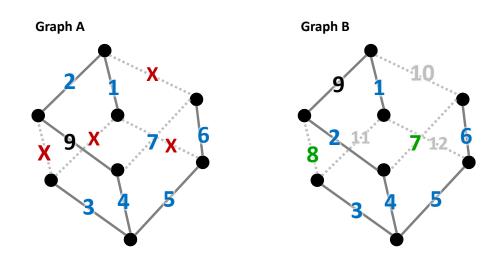


- (2) Considering the following cost functions:
 - Cost of building a tower = hill's height
 - Cost of building a link = wire's length + maximum hill's height of the two ends.

If we only want to **minimize the overall cost** of building the power distribution tree, please **use thick solid lines to depict** what the company should do.



4. Please assign <u>1, 2, 3, ..., 12</u> to the 12 edges of each of the following two graphs (9 is already assigned) so that the minimum-cost span trees (MSTs) of the graphs match what are indicated by the solid lines. Please give a brief explanation if such an assignment does not exist.



The cost of any of X edges in Graph A cannot
≤ 8. Otherwise, one of the X edges would
be part of the MST according to the Kruskal's
algorithm
→ An assignment does not exist for Graph A.

- 5. Consider a Bloom filter with a 10-bit vector and the following three hash functions:
 h1(x) = x % 10
 h2(x) = x² % 10
 - $h_2(x) = x^3 \% 10$ $h_3(x) = x^3 \% 10$
 - (1) Please show the bit vector status after three keys, 12, 16, and 17, are inserted.

0										
0	0	1	1	1	0	1	1	1	1	

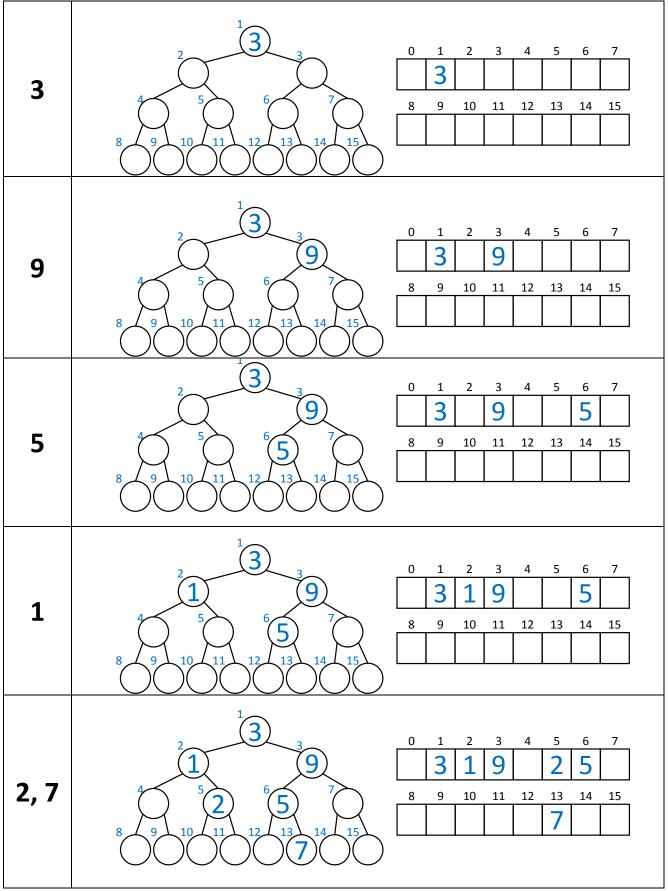
(2) Given the above bit vector status, how many false-positive keys are there in the range of **0**, **1**, **2**, ..., **99**?

(10x+2), (10x+6), (10x+7)	x = 0, 2 ~ 9	→ 3*9 = 27 個
(10x+3), (10x+4), (10x+8)	x = 0 ~ 9	→ 3*10 = 30 個

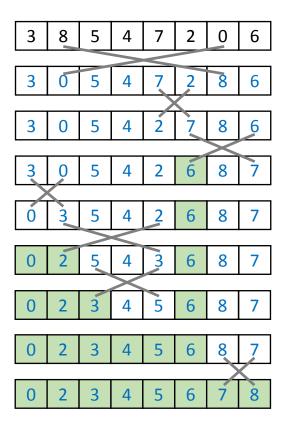
Ans: <u>57</u>

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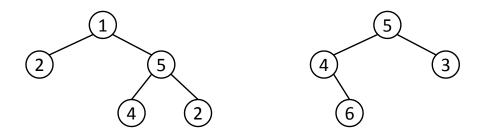
Please show the tree and associated heap statuses after one progressively inserts 3, 9, 5, 1, 2, 7 into an empty binary search tree.



7. Please show the process of Quick Sort (in an ascending order, 由小到大) that always selects the **right-most** entry as the pivot. Each step only swaps two items.



8. Please design a **hash function** that can map **any binary tree of integers** to an integer between 0 and 15. Please also show the hash values for the following two trees.



Example 1:

Hash(any binary tree) = (Sum of all integers in the tree) % 16

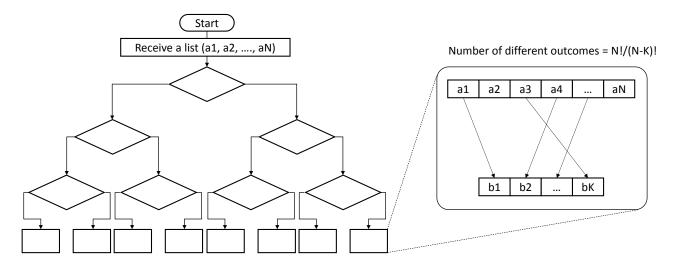
The hash values of the two trees are 14 and 2 respectively.

Example 2:

Hash(any binary tree) = (The root integer) % 16

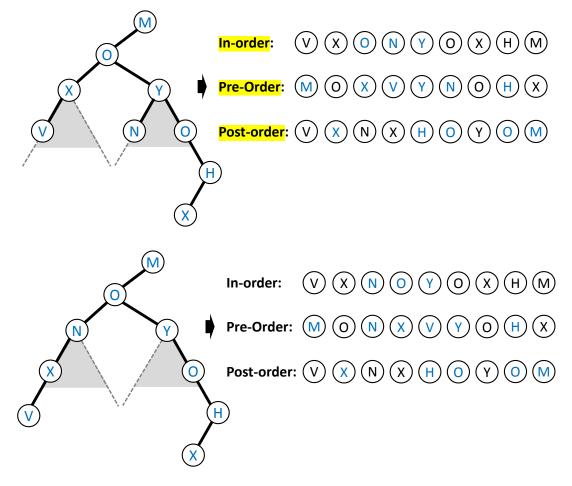
The hash values of the two trees are 1 and 5 respectively.

9. Please analyze the **worst-case number of comparisons** required for **Partial Sort** that receives an N-entry list and produces an <u>ordered list</u> consisted of the K largest entries among the N entries.

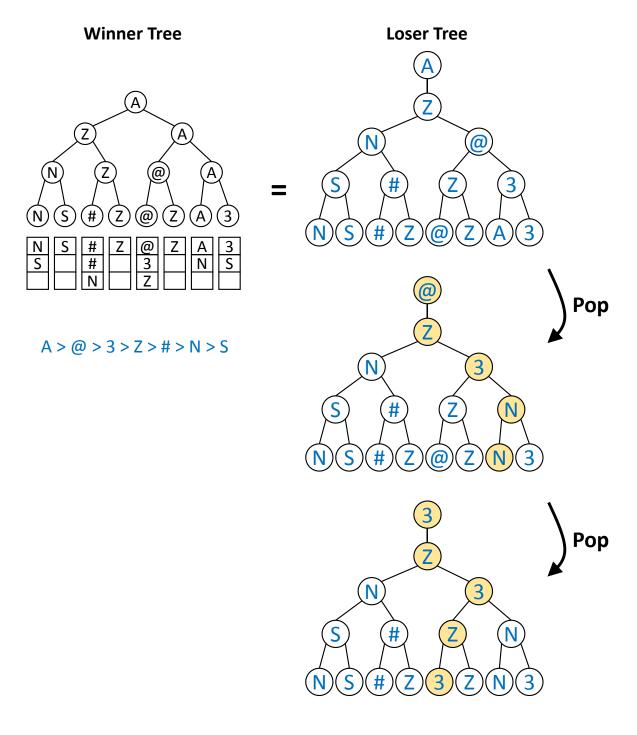


The longest path is at least log₂(N!/(N-K)!)

Please plot the tree and complete its tree traversals. Hint: 1) As you can see in the traversals, there are duplicated entries in the tree, such as X and O. 2) Some trial and error may be necessary.



11. Given a winner tree, please show the associated loser trees.



Please write a recursive function, TreeToChain(), to read all the entries in a binary search tree and return a pointer pointing to an ascending-order, singly-linked chain.
 Please show your algorithm concretely enough. You can use the LastNode() function.

```
struct TreeNode{
  int data;
  TreeNode * left, * right;
};
struct ChainNode{
  int data;
  ChainNode * next;
}
// return a pointer pointing to the last node of the input chain.
ChainNode * LastNode(ChainNode * head);
// return a pointer pointing to the first node of the generated chain.
ChainNode * TreeToChain(TreeNode * root)
{
  ChainNode * ret, * last;
  if(root->left != 0) {
    ret = TreeToChain(root->left);
    last = LastNode(ret);
  }else{
    ret = 0;
  }
  ChainNode * tmp = new ChainNode;
  tmp->data = root->data;
  tmp->next = 0;
  if(ret == 0) ret = tmp;
  else last->next = tmp;
  if(root->right != 0)
    tmp->next = TreeToChain(root->right);
  }
  return ret;
```