

## Homework #8

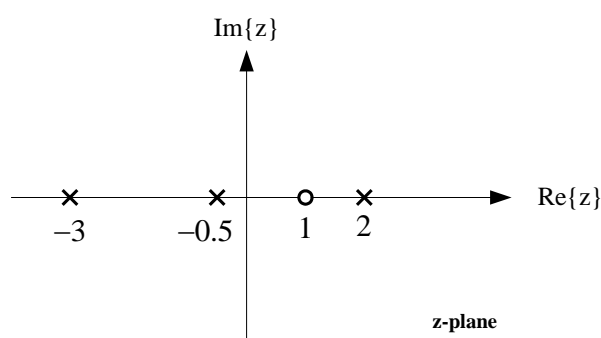
**(For practice only; not to turn in)**

1. Determine the z-transform for each of the following sequences.

(1)  $2^n u[-n] + \left(\frac{1}{4}\right)^n u[n-1]$ . (10%)

(2)  $n\left(\frac{1}{2}\right)^{|n|}$ . (10%)

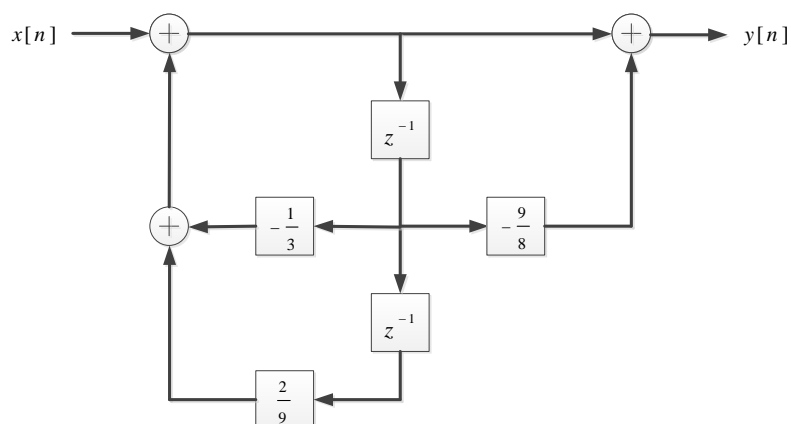
2. Consider a discrete-time LTI system  $H_1(z)$  whose pole-zero plot is shown in the following figure:



(1) How many two-sided impulse responses can be associated with this pole-zero plot? Determine the corresponding ROCs. (10%)

(2) Consider a cascade interconnection of two systems  $H_1(z)$  and  $H_2(z)$ . Determine a possible solution of  $H_2(z)$  such that the overall system is causal and stable. (10%)

3. The input  $x[n]$  and output  $y[n]$  of a causal LTI system are related through the following block-diagram representation:



(1) Determine a difference equation relating  $y[n]$  and  $x[n]$ . (10%)

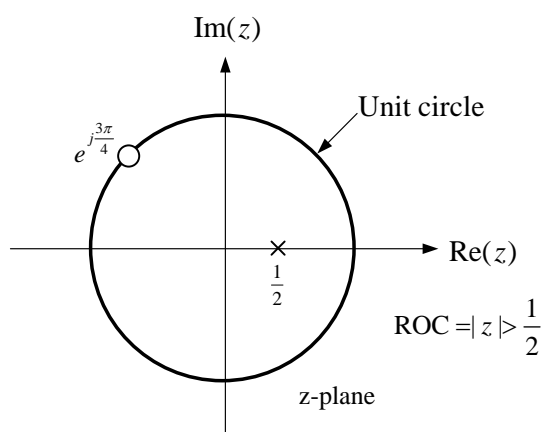
(2) Is this system stable? (10%)

4. Consider a causal and stable discrete-time LTI system with the following system function:

$$H(z) = \frac{1 - z^{-1}}{1 - \frac{1}{4}z^{-2}}.$$

- (1) Find the impulse response  $h[n]$  of the system. (5%)
- (2) Find the output  $y[n]$  of the system when the input is  $x[n] = e^{-j(\pi/2)n}$ . (10%)
- (3) Is there a causal and stable inverse system of  $H(z)$ ? Justify your answer. (5%)

5. Consider a sequence  $x[n]$  with z-transform  $X(z)$  whose pole-zero plot is shown as follows:



Determine the z-transform of each of the following signals in terms of  $X(z)$ . Sketch the pole-zero plot and indicate the ROC for each case.

- (1)  $x_1[n] = x[-n + 4]$ . (10%)
- (2)  $x_2[n] = x[n] \cdot (2e^{-j\pi/4})^n$ . (10%)