Homework No. 5

Due 10:10 am, May 3, 2007

3.58 Use the tables of transforms and properties to find the Fourier transforms of the following signals:

(a)
$$x(t) = \sin(2\pi t)e^{-t}u(t)$$
 (8%)

(b)
$$x(t) = te^{-3|t-1|}$$

(c)
$$x(t) = \left\lceil \frac{2\sin(3\pi t)}{\pi t} \right\rceil \left\lceil \frac{\sin(2\pi t)}{\pi t} \right\rceil$$
 (8%)

(d)
$$x(t) = \frac{d}{dt} \left(t e^{-2t} \sin(t) u(t) \right)$$
 (9%)

3.59 Use the tables of transforms and properties to find the inverse Fourier transforms of the following signals:

(a)
$$X(\omega) = \frac{j\omega}{(1+j\omega)^2}$$
 (8%)

(b)
$$X(\omega) = \frac{4\sin(2\omega - 4)}{2\omega - 4} - \frac{4\sin(2\omega + 4)}{2\omega + 4}$$
 (8%)

(c)
$$X(\omega) = \frac{1}{j\omega(j\omega+2)} - \pi\delta(\omega)$$
 (8%)

(d)
$$X(\omega) = \frac{d}{d\omega} \left[4\sin(4\omega) \frac{\sin(2\omega)}{\omega} \right]$$
 (9%)

3.68 Determine the frequency response and the impulse response for the systems described by the following differential equations:

(a)
$$\frac{d}{dt}y(t) + 3y(t) = x(t)$$
 (9%)

(b)
$$\frac{d^2}{dt^2}y(t) + 5\frac{d}{dt}y(t) + 6y(t) = -\frac{d}{dt}x(t)$$
 (9%)

3.75 Evaluate the following quantities:

(b)
$$\sum_{k=-\infty}^{\infty} \frac{\sin^2\left(k\pi/8\right)}{k^2}$$
 (8%)

(c)
$$\int_{-\infty}^{\infty} \frac{8}{\left(\omega^2 + 4\right)^2} d\omega \tag{8\%}$$