Homework No. 4

Due 10:10 am, May 1, 2007

3.50 Use the defining equation for the Fourier series coefficients to evaluate the Fourier series representation of the following signals:

(a)
$$x(t) = \sin(3\pi t) + \cos(4\pi t)$$
 (10%)

(b)
$$x(t) = \sum_{m=-\infty}^{\infty} \delta(t - m/3) + \delta(t - 2m/3)$$
 (10%)

3.51 Use the definition of the Fourier series to determine the time-domain signals represented by the following Fourier series coefficients:

(a)
$$X[k] = j\delta[k-1] - j\delta[k+1] + \delta[k-3] + \delta[k+3], \quad \omega_0 = 2\pi$$
 (10%)

(e)
$$X[k]$$
 as depicted in Figure P3.51(b) of the textbook, $\omega_0 = 2\pi$ (10%)

3.54 Use the defining equation for the Fourier transform to evaluate the frequency-domain representations of the following signals:

(a)
$$x(t) = e^{-2t}u(t-3)$$
 (10%)

(b)
$$x(t) = e^{-4|t|}$$
 (10%)

3.67 Find the frequency response and impulse response of the systems having the output y(t) for the input x(t):

(a)
$$x(t) = e^{-t}u(t)$$
, $y(t) = e^{-2t}u(t) + e^{-3t}u(t)$ (10%)

(c)
$$x(t) = e^{-2t}u(t)$$
, $y(t) = 2te^{-2t}u(t)$ (10%)

3.77 For the Fourier transform $X(\omega)$ shown in Figure P3.77 of the textbook, evaluate the following quantities without explicitly computing x(t):

(a)
$$\int_{-\infty}^{\infty} x(t)dt$$
 (d) $\arg\{x(t)\}$ (4%)

(b)
$$\int_{-\infty}^{\infty} |x(t)|^2 dt$$
 (4%) (e) $x(0)$

(c)
$$\int_{-\infty}^{\infty} x(t)e^{j3t}dt$$
 (4%)