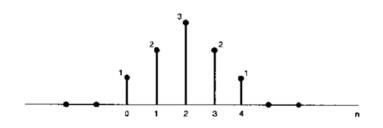
## Homework No. 5 Due 18:10, Dec 30, 2010

1. Consider a non-recursive filter with the impulse response shown in the following figure. What is the group delay as a function of frequency for this filter?



- 2. A causal LTI filter has the frequency response  $H(j\omega) = -2j\omega$ . For each of the input signals given below, determine the filtered output signal y(t).
  - (a)  $x(t) = e^{jt}$
  - (b)  $x(t) = \sin(\omega_0 t)u(t)$

(c) 
$$X(j\omega) = \frac{1}{2+j\omega}$$

3. A system has the indicated transfer function H(s). Determine the impulse response, assuming (a) that the system is causal and (b) that the system is stable. (10%)

$$H(s) = \frac{2s^2 + 2s - 2}{s^2 - 1}$$

- 4. Find the Laplace transform of following signals; indicate the ROC of each signal with figure also. (15%)
  - (a)  $x(t) = -e^{-at}u(t)$ .
  - (b)  $x(t) = e^{-2t}u(t) + e^{-t}(\cos 3t)u(t)$
  - (c)  $x(t) = \delta(t) \frac{4}{3}e^{-t}u(t) + \frac{1}{3}e^{2t}u(t)$