Homework No. 6 Due 17:10, May 8, 2008

1. Use the tables of transforms and properties to find the Fourier transforms of the following signals: (20%)

(a)
$$x(t) = \int_{-\infty}^{t} \frac{\sin(2\pi\tau)}{\pi\tau} d\tau$$
.

(b)
$$x(t) = \left(\frac{\sin(t)}{\pi t}\right) * \frac{d}{dt} \left[\frac{\sin(2t)}{\pi t}\right].$$

2. Use the tables of transforms and properties to find the inverse Fourier transforms of the following signals: (30%)

(a)
$$X(w) = \frac{jw}{(1+jw)^2}$$
.

(b)
$$X(w) = \frac{2\sin(w)}{w(jw+2)}$$
.

(c)
$$X(w) = \frac{d}{dw} [4\sin(4w) \frac{\sin(2w)}{w}].$$

3. Determine the frequency response and the impulse response for the systems described by the following differential equations: (20%)

(a)
$$\frac{d}{dt}y(t) + 3y(t) = x(t)$$

(b)
$$\frac{d^3}{dt^3}y(t) - 3\frac{d}{dt}y(t) - 2y(t) = 3\frac{d^2}{dt^2}x(t) + 8\frac{d}{dt}x(t) - 10x(t)$$

4. Consider the system depicted below. Note that h(t) is the impulse response of an LTI system. (20%)

$$x(t)$$
 $h(t)$ $y(t)$ $y(t)$ $y(t)$ $y(t)$ $y(t)$

We have
$$h(t) = \frac{2\cos(4\pi t)\sin(\pi t)}{\pi t}$$
, $x(t) = \sum_{k=0}^{3} \frac{2}{1+k}\cos(k2\pi t)$ and $w(t) = 2\cos(4\pi t)$.

- (a) Find the sketch the FT of h(t).
- (b) Find and sketch the FT of x(t).
- (c) Find and sketch the FT of y(t).
- (d) Find z(t) and sketch the FT of z(t).

5. Evaluate the following quantity: (10%)

$$\sum_{k=-\infty}^{\infty} \frac{\sin^2(k\pi/8)}{k^2}$$