

EE 361002 Signal and System HW3

2.22(a,b,d),2.23,2.24,2.32, Plot the impulse response of Eq.P2.32-1 assuming initial at rest (please include your code).

2.22. For each of the following pairs of waveforms, use the convolution integral to find the response $y(t)$ of the LTI system with impulse response $h(t)$ to the input $x(t)$. Sketch your results.

(a) $\left. \begin{aligned} x(t) &= e^{-\alpha t} u(t) \\ h(t) &= e^{-\beta t} u(t) \end{aligned} \right\}$ (Do this both when $\alpha \neq \beta$ and when $\alpha = \beta$.)

(b) $x(t) = u(t) - 2u(t - 2) + u(t - 5)$
 $h(t) = e^{2t} u(1 - t)$

(c) $x(t)$ and $h(t)$ are as in Figure P2.22(a).

(d) $x(t)$ and $h(t)$ are as in Figure P2.22(b).

(e) $x(t)$ and $h(t)$ are as in Figure P2.22(c).

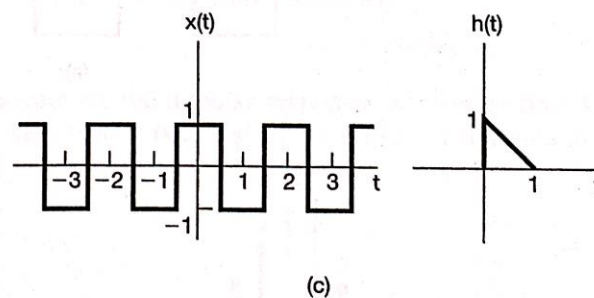
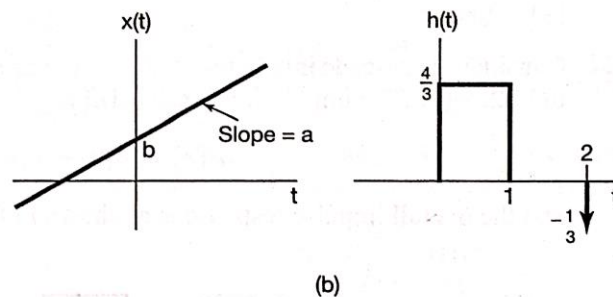
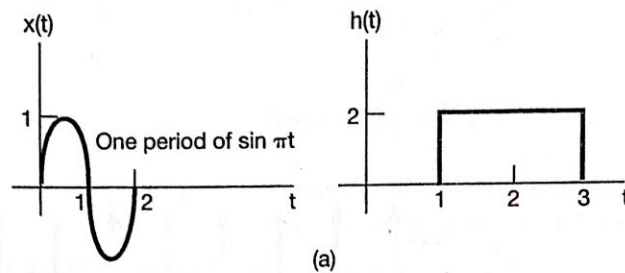


Figure P2.22

2.23. Let $h(t)$ be the triangular pulse shown in Figure P2.23(a), and let $x(t)$ be the impulse train depicted in Figure P2.23(b). That is,

$$x(t) = \sum_{k=-\infty}^{+\infty} \delta(t - kT).$$

Determine and sketch $y(t) = x(t) * h(t)$ for the following values of T :

- (a) $T = 4$ (b) $T = 2$ (c) $T = 3/2$ (d) $T = 1$

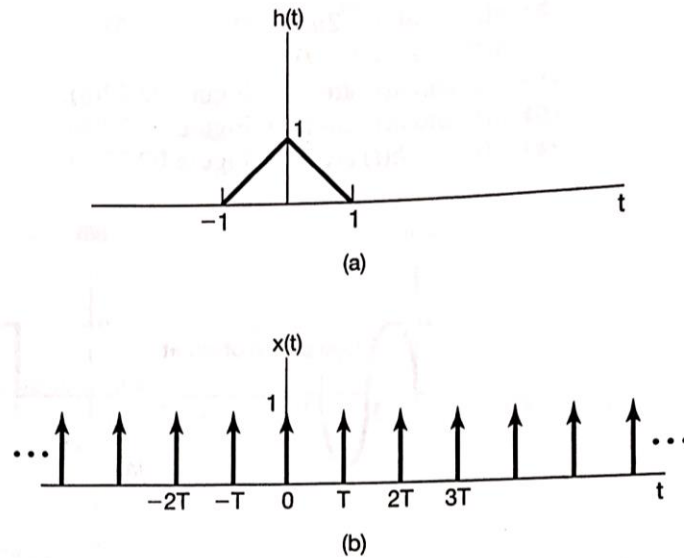


Figure P2.23

2.24. Consider the cascade interconnection of three causal LTI systems, illustrated in Figure P2.24(a). The impulse response $h_2[n]$ is

$$h_2[n] = u[n] - u[n - 2],$$

and the overall impulse response is as shown in Figure P2.24(b).

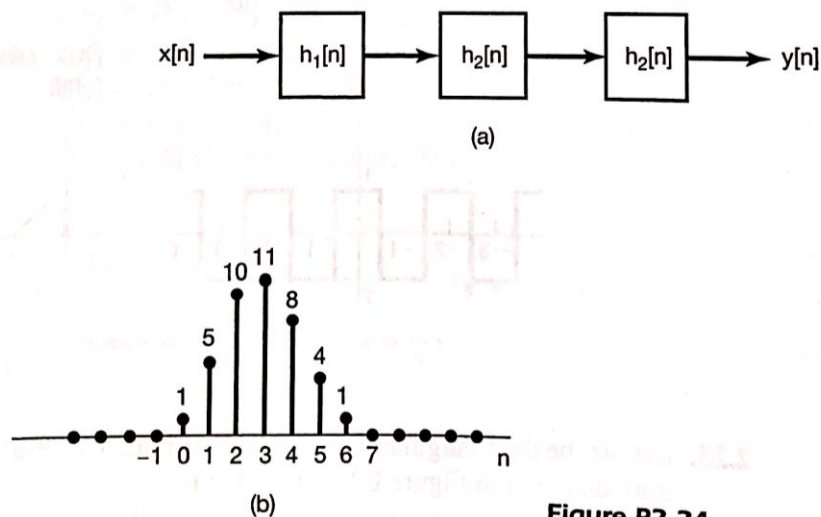


Figure P2.24

- (a) Find the impulse response $h_1[n]$.
 (b) Find the response of the overall system to the input

$$x[n] = \delta[n] - \delta[n - 1].$$

2.32. Consider the difference equation

$$y[n] - \frac{1}{2}y[n - 1] = x[n], \quad (\text{P2.32-1})$$

and suppose that

$$x[n] = \left(\frac{1}{3}\right)^n u[n]. \quad (\text{P2.32-2})$$

Assume that the solution $y[n]$ consists of the sum of a particular solution $y_p[n]$ to eq. (P2.32-1) and a homogeneous solution $y_h[n]$ satisfying the equation

$$y_h[n] - \frac{1}{2}y_h[n - 1] = 0.$$

- (a) Verify that the homogeneous solution is given by

$$y_h[n] = A\left(\frac{1}{2}\right)^n$$

- (b) Let us consider obtaining a particular solution $y_p[n]$ such that

$$y_p[n] - \frac{1}{2}y_p[n - 1] = \left(\frac{1}{3}\right)^n u[n].$$

By assuming that $y_p[n]$ is of the form $B(\frac{1}{3})^n$ for $n \geq 0$, and substituting this in the above difference equation, determine the value of B .

- (c) Suppose that the LTI system described by eq. (P2.32-1) and initially at rest has as its input the signal specified by eq. (P2.32-2). Since $x[n] = 0$ for $n < 0$, we have that $y[n] = 0$ for $n < 0$. Also, from parts (a) and (b) we have that $y[n]$ has the form

$$y[n] = A\left(\frac{1}{2}\right)^n + B\left(\frac{1}{3}\right)^n$$

for $n \geq 0$. In order to solve for the unknown constant A , we must specify a value for $y[n]$ for some $n \geq 0$. Use the condition of initial rest and eqs. (P2.32-1) and (P2.32-2) to determine $y[0]$. From this value determine the constant A . The result of this calculation yields the solution to the difference equation (P2.32-1) under the condition of initial rest, when the input is given by eq. (P2.32-2).