

EE231002 Introduction to Programming

Lab02. Approximating π

Due: Sep. 24, 2019

The following equation has been proven and as the number of terms approaches infinite it converges to value shown on the right side of the equation.

$$\frac{1}{2 \cdot 3 \cdot 4} - \frac{1}{4 \cdot 5 \cdot 6} + \frac{1}{6 \cdot 7 \cdot 8} - \dots = \frac{1}{4}(\pi - 3).$$

The aim of this lab is to verify the above equation, we define

$$S2 = \frac{1}{2 \cdot 3 \cdot 4} - \frac{1}{4 \cdot 5 \cdot 6},$$
$$S4 = \frac{1}{2 \cdot 3 \cdot 4} - \frac{1}{4 \cdot 5 \cdot 6} + \frac{1}{6 \cdot 7 \cdot 8} - \frac{1}{8 \cdot 9 \cdot 10},$$
$$S6 = \frac{1}{2 \cdot 3 \cdot 4} - \frac{1}{4 \cdot 5 \cdot 6} + \frac{1}{6 \cdot 7 \cdot 8} - \frac{1}{8 \cdot 9 \cdot 10} + \frac{1}{10 \cdot 11 \cdot 12} - \frac{1}{12 \cdot 13 \cdot 14}.$$

Given the partial sums, then we can find the approximated value of π as below.

$$S2 = \frac{1}{4}(PI2 - 3),$$

$$S4 = \frac{1}{4}(PI4 - 3),$$

$$S6 = \frac{1}{4}(PI6 - 3).$$

As the number of terms increases, the value of PI_n should approach π . Your assignment is to write a C program to calculate $PI2$, $PI4$, $PI6$, $PI8$, $PI10$ and $PI12$. The output of your program should have the following format.

```
$ ./a.out
PI2 = 3.13333
PI4 = x.xxxxx
PI6 = x.xxxxx
PI8 = x.xxxxx
PI10 = x.xxxxx
PI12 = x.xxxxx
```

Notes.

1. Create a directory **lab02** and use it as the working directory.
2. Name your program source file as **lab02.c**.

3. The first few lines of your program should be comments as the following.

```
// EE231002 Lab02. Approximating Pi
// ID, Name
// Date
```

4. After finishing editing your source file, you can execute the following command to compile the program,

```
$ gcc lab02.c
```

If no compilation errors, the executable file, **a.out**, should be generated, and you can execute it by typing

```
$ ./a.out
```

5. After you finish verifying your program, you can submit your source code by

```
$ ~ee2310/bin/submit lab02 lab02.c
```

If you see a "submitted" message, then you are done. In case you want to check which file and at what time you submitted your labs, you can type in the following command:

```
$ ~ee2310/bin/subrec lab02
```

It will show the last few submission records.

6. (Challenge, no submission is required.) Since this is a convergent series, the approximation should approach π . You are encouraged to find the value of π as accurate as possible.

