

2017 Fall EE203001 Linear Algebra - Quiz 3

Name:

ID:

1. Let $A = \begin{bmatrix} 1 & 2 & 2 & 3 \\ 2 & 4 & 5 & 7 \\ 4 & 8 & 9 & 13 \end{bmatrix}$. Please find:

(a) Reduced row echelon form of A

(b) Reduced row echelon form of A can be expressed as $\begin{bmatrix} I & F \\ 0 & 0 \end{bmatrix}$, Please find the block matrix F

(c) Rank of A

(d) Special Solution for $Ax = 0$

sol:

1. :

(a) $A = \begin{bmatrix} 1 & 2 & 2 & 3 \\ 2 & 4 & 5 & 7 \\ 4 & 8 & 9 & 13 \end{bmatrix}$, Because Row3 = Row1 + Row2

$$\text{So } A = \begin{bmatrix} 1 & 2 & 2 & 3 \\ 2 & 4 & 5 & 7 \\ 0 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 2 & 2 & 3 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 2 & 0 & 1 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix} = A_R$$

(b) $A_R = \begin{bmatrix} 1 & 0 & 2 & 1 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$, So $F = \begin{bmatrix} 2 & 1 \\ 0 & 1 \end{bmatrix}$

(c) Pivot of A is 2, So Rank of A is 2

(d) $\text{column2} = 2\text{column1} + 0\text{column3} \Rightarrow \text{column2} - 2\text{column1} - 0\text{column3} = 0$
 $\text{column4} = 1\text{column1} + 1\text{column3} \Rightarrow \text{column4} - 1\text{column1} - 1\text{column3} = 0$

$$\text{So, Special Solution is } \begin{bmatrix} -2 \\ 1 \\ 0 \\ 0 \end{bmatrix}, \begin{bmatrix} -1 \\ 0 \\ -1 \\ 1 \end{bmatrix}$$