

$$F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{d^2} \dots \mathbf{1}$$

$$F_A = \frac{Q}{4\pi\epsilon_0} \frac{-Q}{0^2+9^2+12^2} = \frac{Q^2}{4\pi\epsilon_0} \frac{-1}{225} \dots \mathbf{1}$$

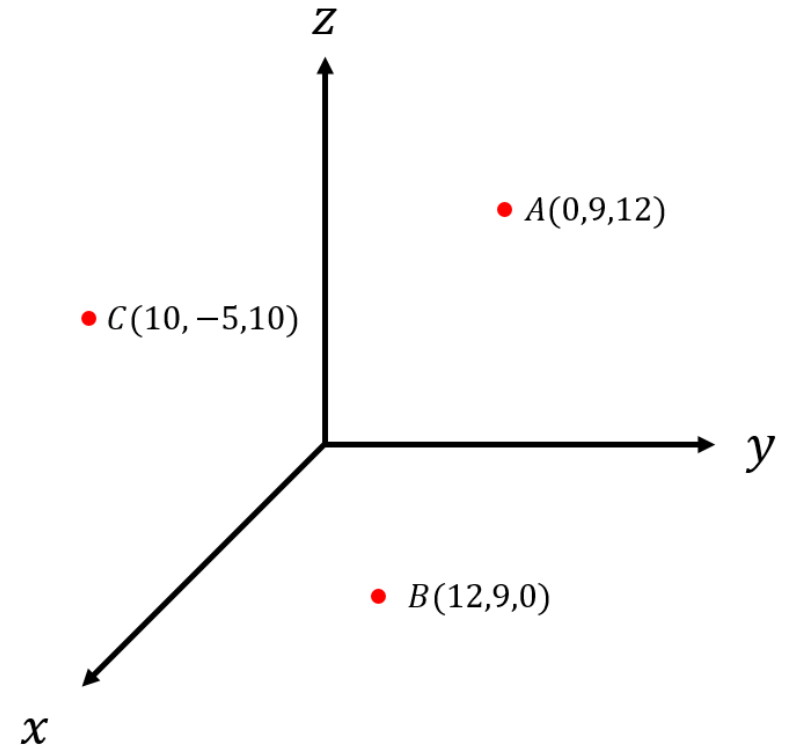
$$F_B = \frac{Q}{4\pi\epsilon_0} \frac{Q}{12+9^2+0^2} = \frac{Q^2}{4\pi\epsilon_0} \frac{1}{225} \dots \mathbf{1}$$

$$F_C = \frac{Q}{4\pi\epsilon_0} \frac{Q}{10^2+(-5)^2+10^2} = \frac{Q^2}{4\pi\epsilon_0} \frac{1}{225} \dots \mathbf{1}$$

$$F_{net_x} = \frac{-Q^2}{4\pi\epsilon_0} \frac{1}{225} \left(-1 \cdot \frac{0}{15} + 1 \cdot \frac{12}{15} + 1 \cdot \frac{10}{15} \right) = \frac{Q^2}{4\pi\epsilon_0} \frac{1}{225} \left(\frac{-22}{15} \right) \dots \mathbf{2}$$

$$F_{net_y} = \frac{-Q^2}{4\pi\epsilon_0} \frac{1}{225} \left(-1 \cdot \frac{9}{15} + 1 \cdot \frac{9}{15} + 1 \cdot \frac{-5}{15} \right) = \frac{Q^2}{4\pi\epsilon_0} \frac{1}{225} \left(\frac{1}{3} \right) \dots \mathbf{2}$$

$$F_{net_z} = \frac{-Q^2}{4\pi\epsilon_0} \frac{1}{225} \left(-1 \cdot \frac{12}{15} + 1 \cdot \frac{0}{15} + 1 \cdot \frac{10}{15} \right) = \frac{Q^2}{4\pi\epsilon_0} \frac{1}{225} \left(\frac{2}{15} \right) \dots \mathbf{2}$$



Q.2 In Figure 2, there is a charged particle q lies on the z -axis along with the centers of two uniformly charged rings.

The location of q is $z = 6 \text{ m}$, the center of the green ring is $z = 0 \text{ m}$ and blue ring is $z = -6 \text{ m}$. The radius of the green ring $R1 = 8 \text{ m}$ and blue ring $R2 = 5 \text{ m}$. If we know the total charge of the green ring is -8π (Coulomb) and the net electric field at q is zero. What is the linear charge density of the blue ring? (10 points)

the linear charge density of the green ring $\lambda_G = \frac{-8\pi \text{ C}}{2\pi \cdot 8 \text{ m}} = -\frac{1}{2} \text{ C/m}$

$$\begin{aligned} \vec{E}_{G \rightarrow q} &= \frac{6\text{m} \cdot (-\frac{1}{2} \text{ C/m}) \cdot (2\pi \cdot 8\text{m})}{4\pi \epsilon_0 ((6\text{m})^2 + (8\text{m})^2)^{3/2}} (+\hat{z}) \\ &= -\vec{E}_{B \rightarrow q} \\ &= -\frac{12\text{m} \cdot \lambda_B \cdot (2\pi \cdot 5\text{m})}{4\pi \epsilon_0 ((12\text{m})^2 + (5\text{m})^2)^{3/2}} (+\hat{z}) \end{aligned}$$

$$\Rightarrow \lambda_B = \frac{6\text{m} \cdot (-\frac{1}{2} \text{ C/m}) \cdot 8\text{m}}{(10\text{m})^3} \cdot \left(-\frac{(13\text{m})^3}{12\text{m} \cdot 5\text{m}}\right) = \frac{4394}{5000} \text{ C/m}$$

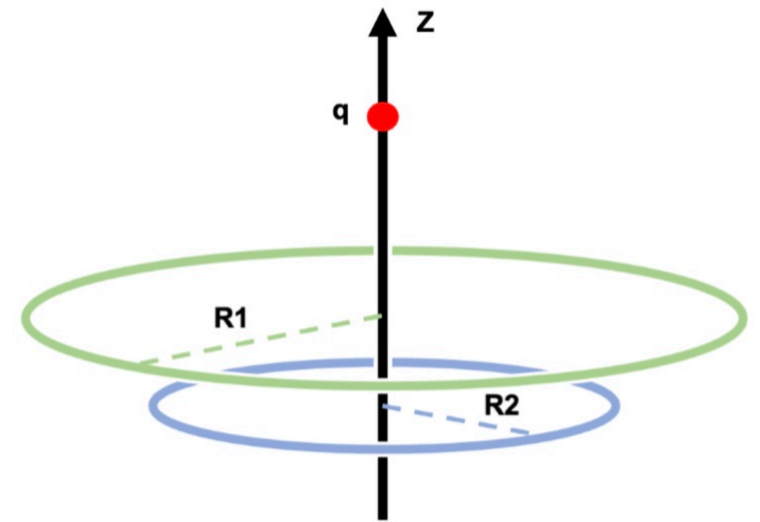


Figure 1: one charged particle and two rings