

1.

(a)

$$h\nu_0 \sim E_g + \frac{1}{2}kT \Rightarrow E_g = h\nu_0 - \frac{1}{2}kT$$

$$\text{For } \lambda_0 = 822(\text{nm}), T = 25 + 273 = 298(\text{K})$$

$$\begin{aligned} \therefore E_g &= 6.624 \times 10^{-34} \times \frac{3 \times 10^8}{822 \times 10^{-9}} - \frac{1}{2} \times 1.38 \times 10^{-23} \times 298 = 2.398 \times 10^{-19} (\text{J}) \\ &= 1.499 (\text{eV}) \end{aligned}$$

(b)

$$\text{For } E_g = 1.499 (\text{eV}) \Rightarrow 1.424 + 1.266X + 0.266X^2 = 1.499$$

$$\Rightarrow 0.266X^2 + 1.266X - 0.075 = 0$$

$$\Rightarrow X = \frac{-1.266 \pm \sqrt{1.266^2 - 4 \times 0.266 \times (-0.075)}}{0.266 \times 2}$$

$$\text{取正值} \Rightarrow X = 0.059$$

\therefore The composition of LED is $\text{Al}_{0.059}\text{Ga}_{0.941}\text{As}$

2.

(a)

$$\eta_{\text{IQE}} = \frac{\frac{1}{\tau_r}}{\frac{1}{\tau_r} + \frac{1}{\tau_{\text{nr}}}} = \frac{\frac{1}{\tau_r}}{\frac{1}{\tau}} = \frac{\tau}{\tau_r}$$

$$\eta_{\text{IQE}} f_c = \frac{\tau}{\tau_r} \times \frac{1}{2\pi\tau} = \frac{1}{2\pi\tau_r}$$

For a material, the life time of radiative process is fixed, and

so is $\eta_{\text{IQE}} f_c$, η_{IQE} is inversely proportional to f_c

$$(b) \eta_{\text{IQE}} = \frac{\frac{1}{\tau_r}}{\frac{1}{\tau_r} + \frac{1}{\tau_{\text{nr}}}} = \frac{\frac{1}{10 \times 10^{-9}}}{\frac{1}{10 \times 10^{-9}} + \frac{1}{50 \times 10^{-9}}} = 0.833 \quad f_c = \frac{1}{2\pi\tau} = \frac{\frac{1}{\tau_r} + \frac{1}{\tau_{\text{nr}}}}{2\pi} = \frac{\frac{1}{10 \times 10^{-9}} + \frac{1}{50 \times 10^{-9}}}{2\pi} = 1.91 \times 10^7 (\text{Hz})$$

For $\tau_{\text{nr}} = 25(\text{ns})$:

$$\eta_{\text{IQE}} = \frac{\frac{1}{10 \times 10^{-9}}}{\frac{1}{10 \times 10^{-9}} + \frac{1}{25 \times 10^{-9}}} = 0.714 \quad f_c = \frac{\frac{1}{10 \times 10^{-9}} + \frac{1}{25 \times 10^{-9}}}{2\pi} = 2.228 \times 10^7 (\text{Hz})$$

3.

$$(a) \text{ For } \Phi_V = P_{\text{out}} \times 683 \times V(528\text{nm})$$

$$\Rightarrow P_{\text{out}} = \frac{92}{683 \times 0,8} = 0,168 \text{ (W)}$$

$$\eta_{\text{PCE}} = \frac{P_{\text{out}}}{IV} = \frac{0,168}{(350 \times 10^{-3}) \times 3,4} = 0,141 \%$$

$$\eta_{\text{EQE}} = \frac{\Phi_{\text{out}}}{I/e} = \frac{P_{\text{out}}/h\nu}{I/e} = \frac{0,168 \times 1,6 \times 10^{-19}}{6,626 \times 10^{-34} \times \frac{3 \times 10^8}{528 \times 10^{-9}} \times 350 \times 10^{-3}} = 0,204 \%$$

$$\eta_{\text{LE}} = \frac{\Phi_V}{IV} = \frac{92}{350 \times 10^{-3} \times 3,4} = 77,311 \text{ (lm/W)} \%$$

(b)

$$\eta_{\text{IQE}} = \frac{1/\epsilon_r}{1/\epsilon_r + 1/\epsilon_{\text{nr}}} = \frac{1/25 \times 10^{-9}}{1/25 \times 10^{-9} + 1/100 \times 10^{-9}} = 0,8$$

$$\eta_{\text{PCE}} = \frac{P_{\text{out}}}{IV} = \frac{6,5 \times 10^{-3}}{30 \times 10^{-3} \times 1,35} = 0,16$$

$$\eta_{\text{EQE}} = \frac{P_{\text{out}}/h\nu}{I/e} = \frac{6,5 \times 10^{-3} \times 1,6 \times 10^{-19}}{30 \times 10^{-3} \times 6,626 \times 10^{-34} \times \frac{3 \times 10^8}{870 \times 10^{-9}}} = 0,152 \%$$

$$\eta_{\text{EE}} = \frac{P_{\text{out}}/h\nu}{\eta_{\text{IQE}} \times I/e} = \eta_{\text{EQE}} \times \frac{1}{\eta_{\text{IQE}}} = 0,152 \times \frac{1}{0,8} = 0,19 \%$$